

Efficient and Robust Circle Grids for Fiducial Detection

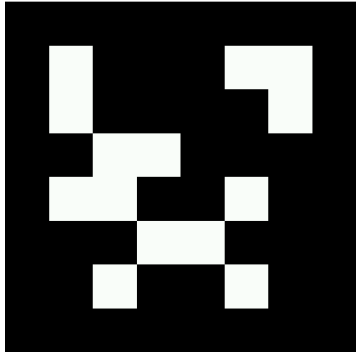
Master's Colloquium

Michael Loipföhrer

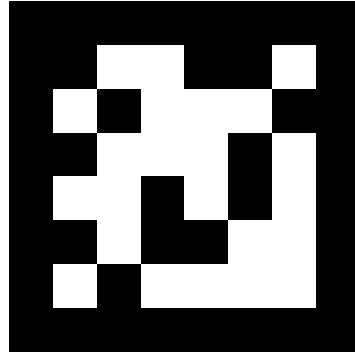
Department of Informatics

May 23, 2022

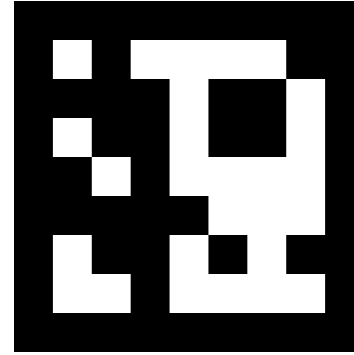
What are fiducial markers?



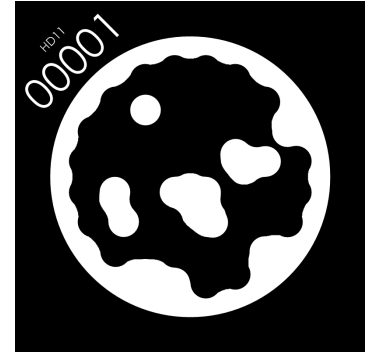
ARToolkitPlus [1]



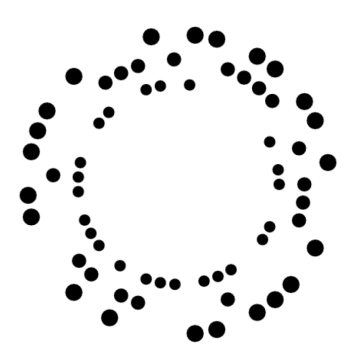
AprilTag [2], [3]



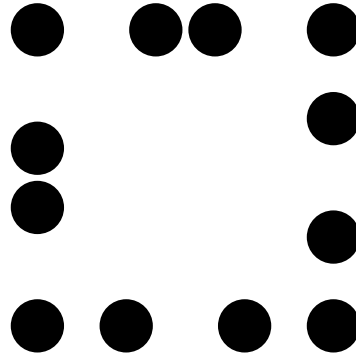
ArUco [4]



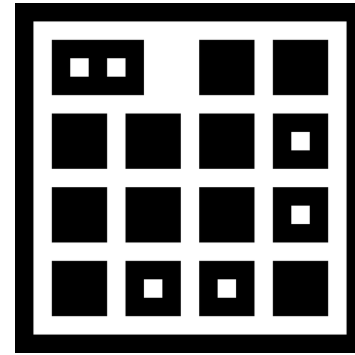
STag [5]



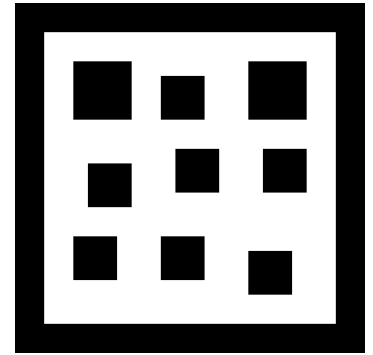
RuneTag [6]



Pi-Tag [7]

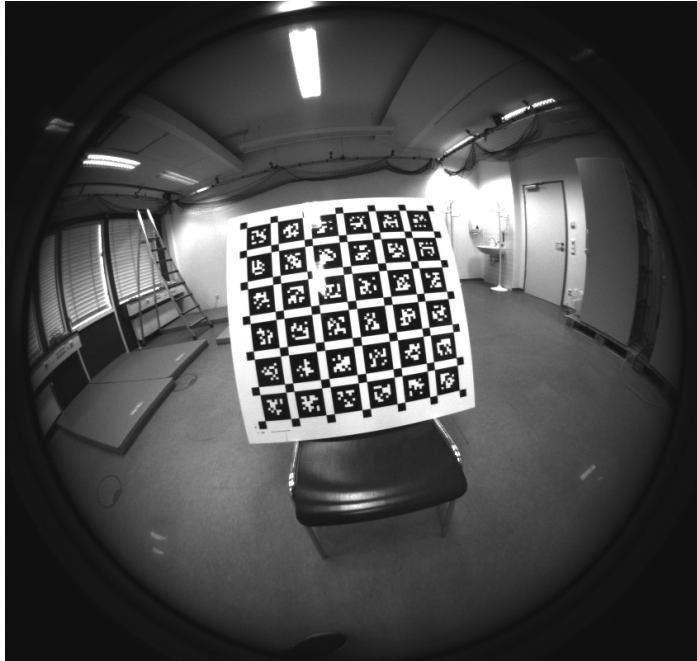


TopoTag [8]



LFTag [9]

What are fiducial markers?



Camera Calibration



Robotic Applications¹



Augmented Reality²

¹ AprilTag website. URL: <https://april.eecs.umich.edu/software/apriltag> (visited on 05/16/2022).

² Researchgate. URL: https://www.researchgate.net/figure/Circular-marker-for-Augmented-Reality_fig1_259752709 (visited on 05/21/2022).

What are fiducial markers?



Designed for

- robust detections
- stable 3D pose recovery
- unique marker identifiers

Motivation

Existing methods do not work well in very distorted images

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Goals of this Thesis

Design a novel fiducial marker system based on circle grids that specifically

- provides robust detections
- achieves stable pose recovery
- works well with distorted fisheye cameras
- can be composed into larger marker grids

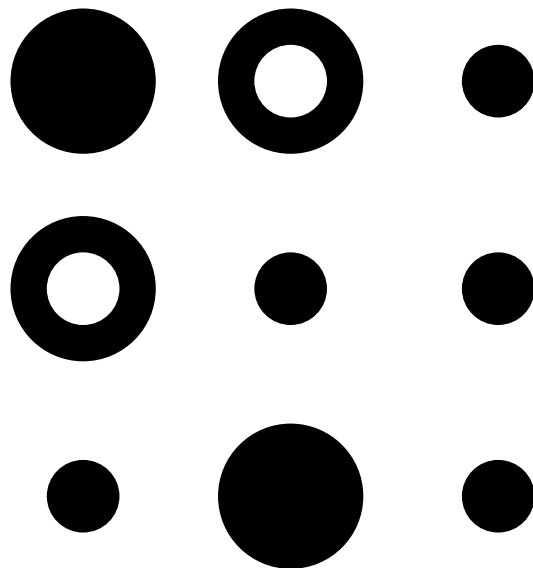
- 1 Introduction
- 2 Marker Design
- 3 Marker Grids
- 4 Evaluation
- 5 Live Demo
- 6 References

Circles

- robust detections even with high distortion
- subpixel accuracy

3 × 3 Grid

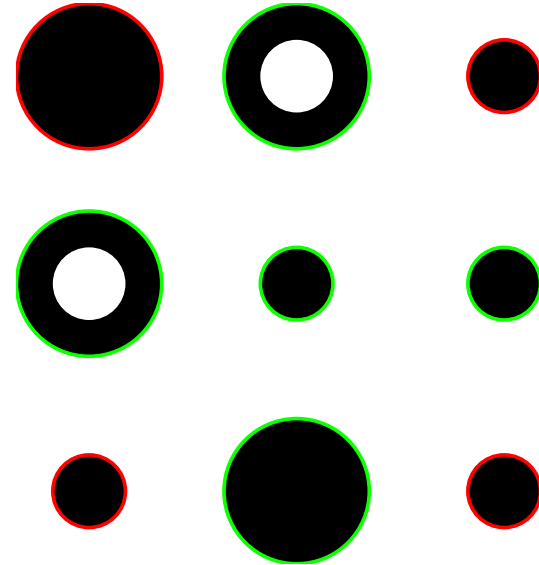
- compact layout
- regular geometry helps detection scheme



Example Marker

Marker Payload

- recover the orientation of a tag
- discard erroneous detections



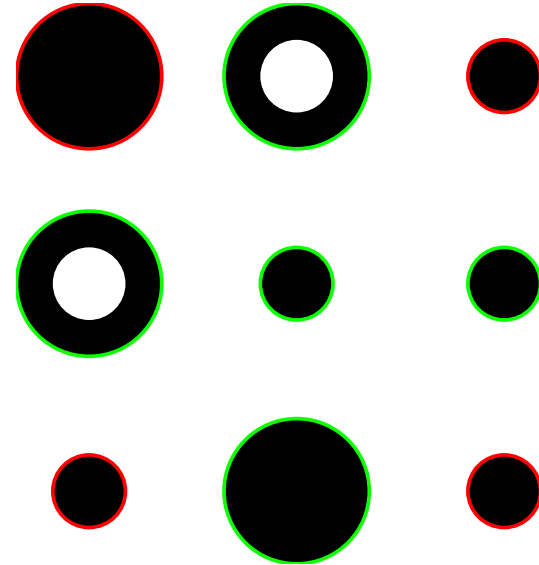
Corners: 0111, Full payload: 021110121

Marker Payload

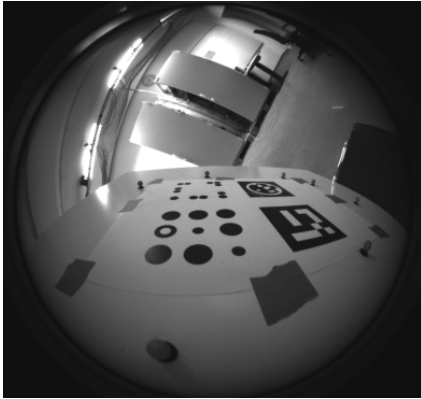
- recover the orientation of a tag
- discard erroneous detections

Coding Scheme

- Lyndon words for rotational uniqueness in corners
- remaining 5 digits for arbitrary error detection



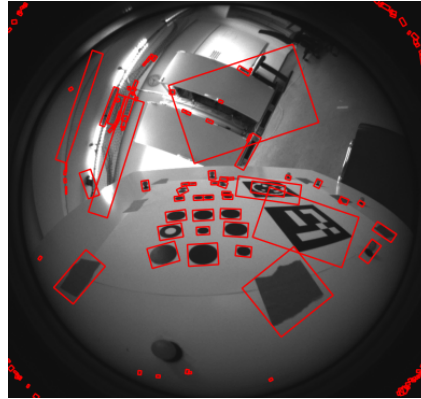
Corners: 01111, Full payload: 021110121



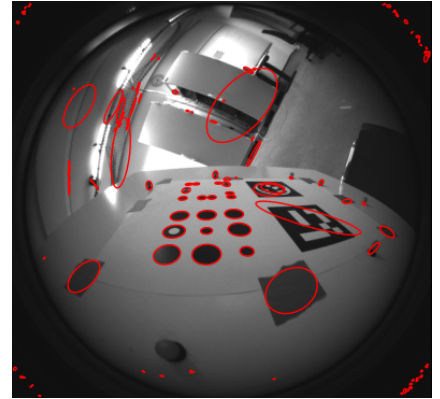
Original image



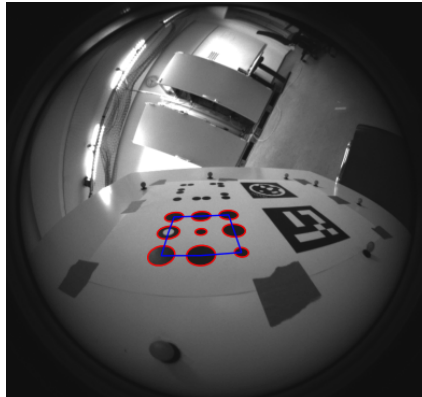
Thresholded image



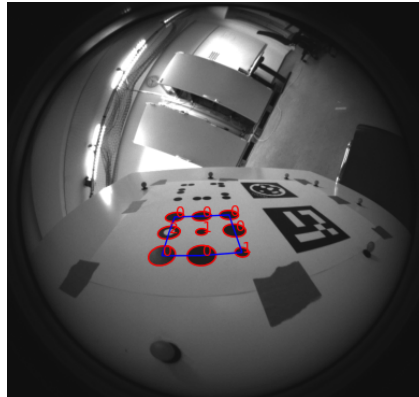
Ellipse candidates



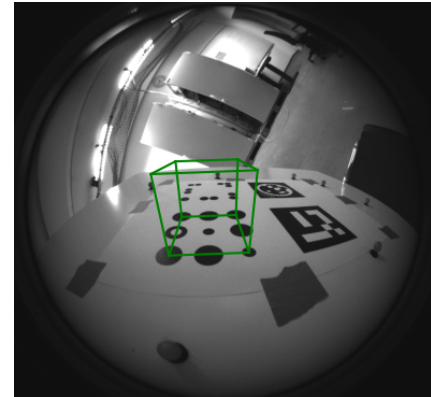
Detected ellipses



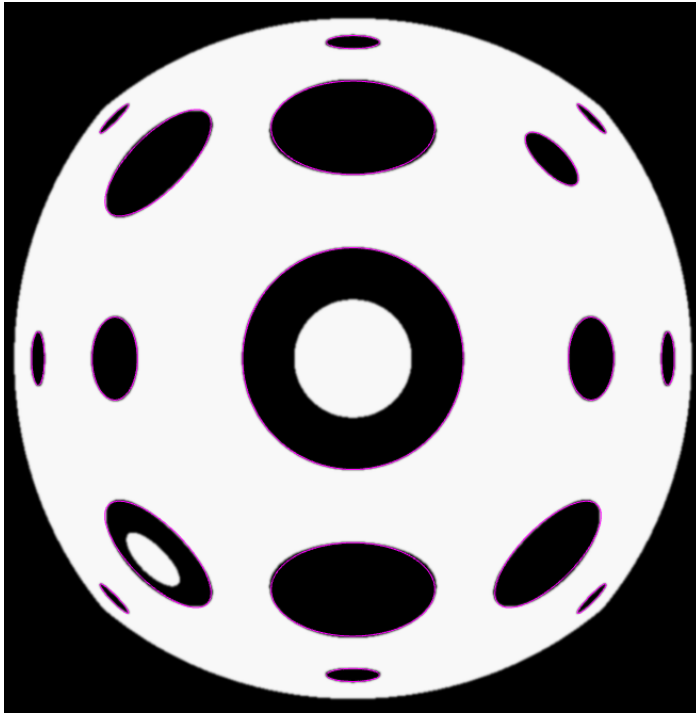
Marker candidates



Valid markers



Pose Estimation

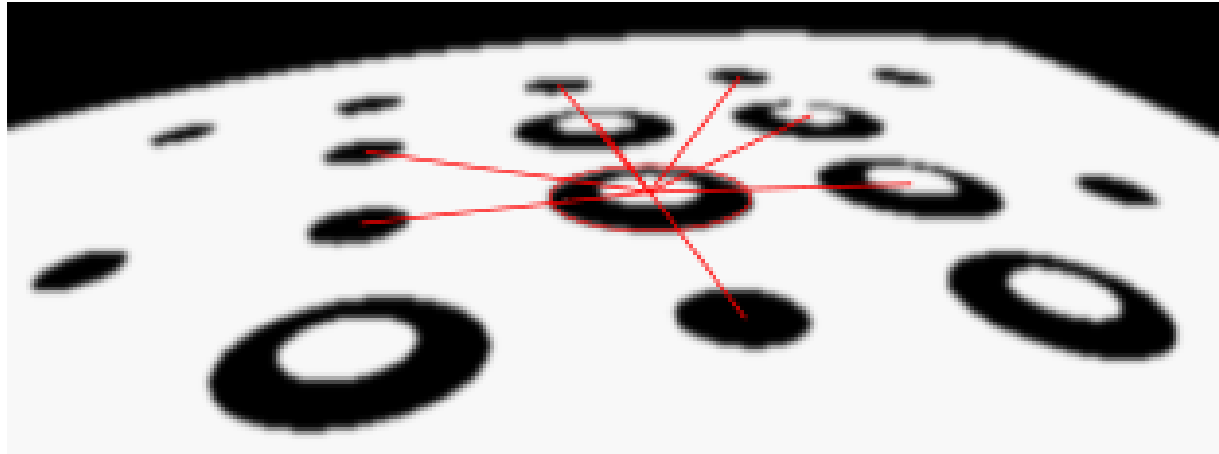


Basic Idea

- perform a KNN-search for every ellipse
- check if the 8 nearest neighbors fit a 3×3 grid

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- perform a KNN-search for every ellipse
- check if the 8 nearest neighbors fit a 3×3 grid
- KNN-search with $k \geq 8$
- geometric heuristics based on angles and distances between ellipses to filter out invalid marker geometries



Ellipse Type Decoding

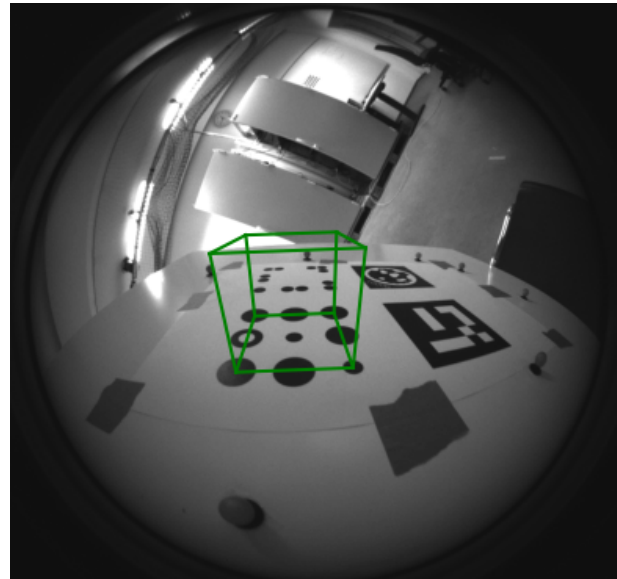
- relate relative distances between ellipses with measured sizes
- compare to known true sizes of different ellipse types

Payload Check

- recovery of rotation using payload of corner points
- validity check of any error detection schemes

Method

- all 9 ellipses used as 2D - 3D point correspondences
- UPNP [12] and KNEIP [13] used as initializations
- non-linear optimization for pose refinement

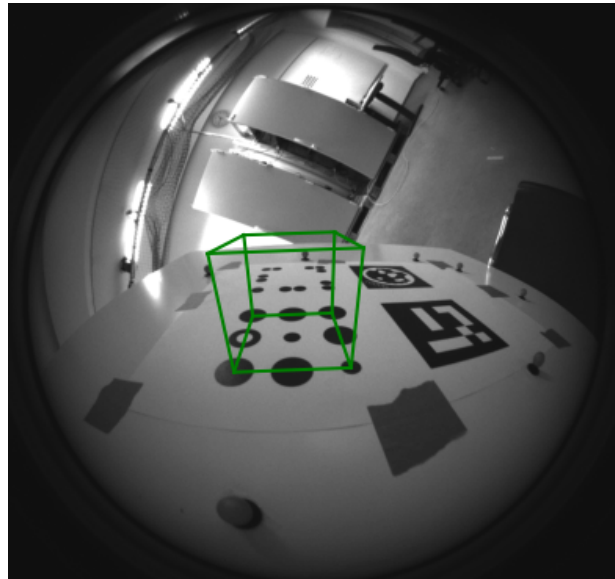


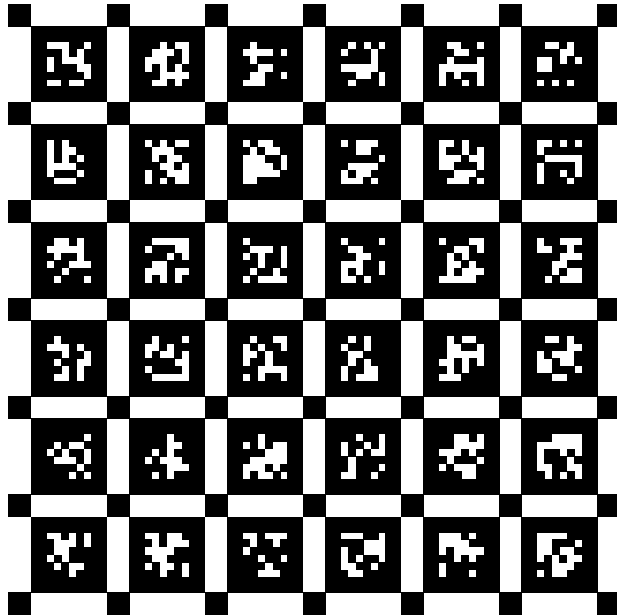
Method

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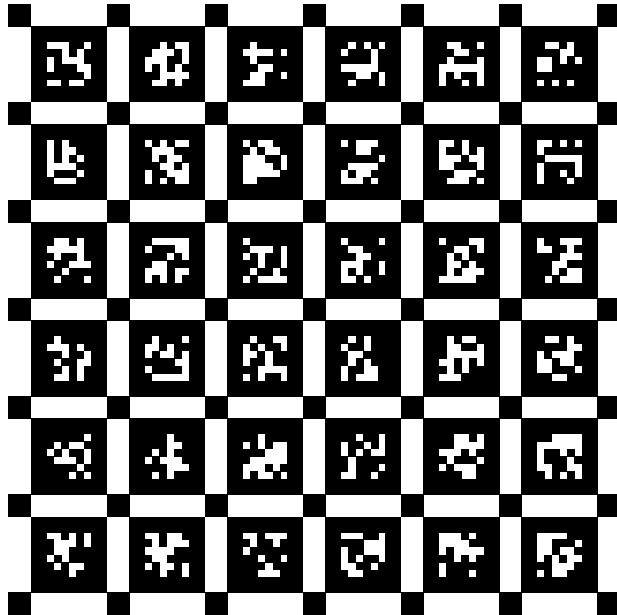
Benefits of our method

- ellipse detection produces accurate 2D feature points
- more correspondences leads to more stable poses

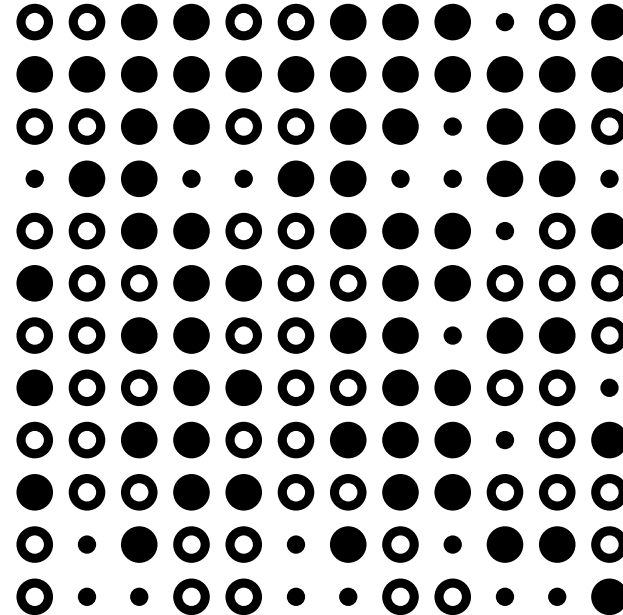




AprilGrid



AprilGrid



Ours

Camera Calibration

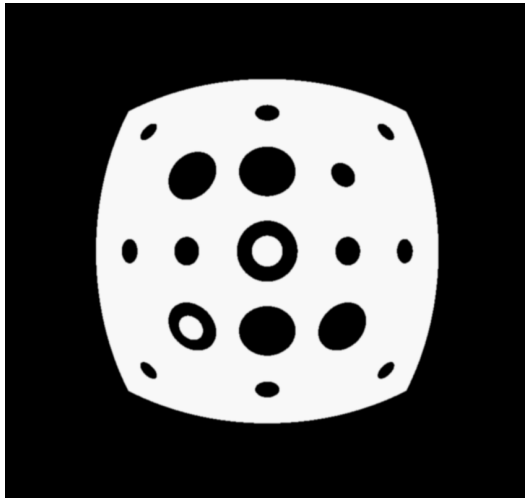
- good performance for fisheye cameras
- more robust to detection errors than AprilGrid

Grids as Fiducials

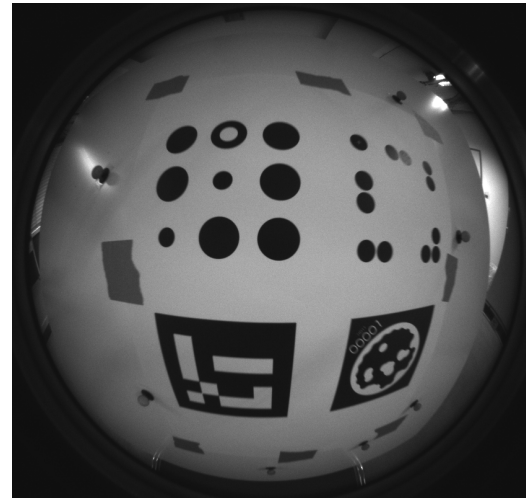
- large number of unique marker identifiers
- more options for error detection and correction

Evaluation of

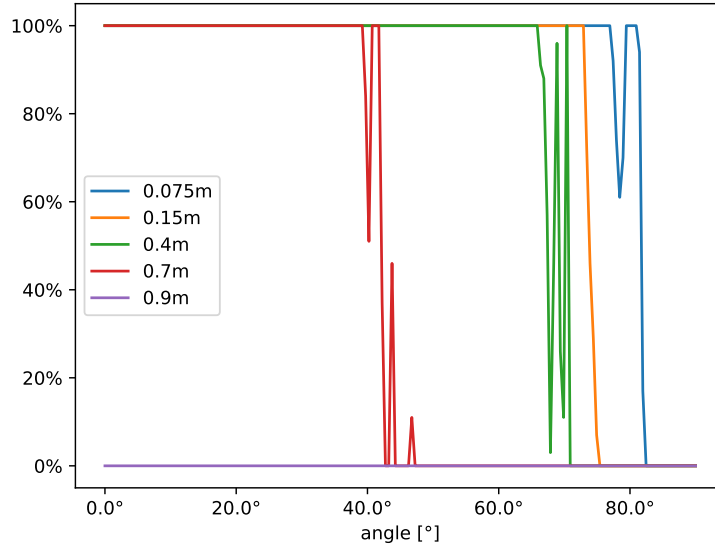
- detection precision and recall
- pose estimation accuracy
- in real world and simulated images



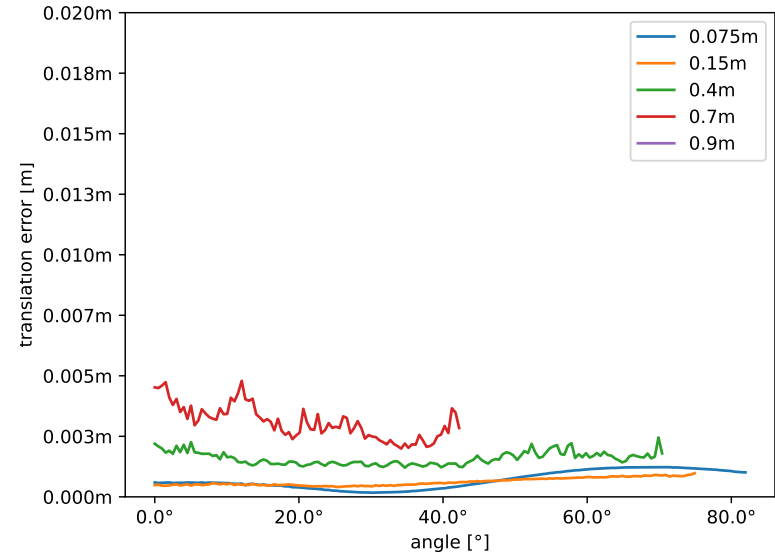
Simulation



Real World



Detection Recall



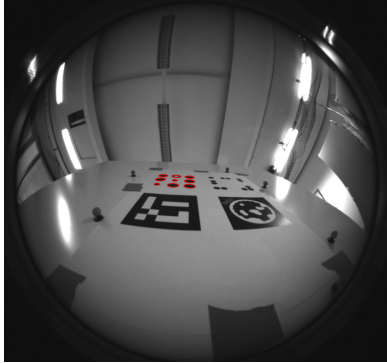
Pose Translation Error

Marker System	distance	low angle close	pan tilt close	mixed	planar close
ArUco	56.35%	83.37%	55.65%	89.78%	54.88%
S-Tag	37.88%	63.00%	60.58%	86.69%	62.80%
Pi-Tag	10.38%	39.87%	7.68%	0.00%	0.26%
Ours	39.04%	82.34%	71.01%	88.11%	66.23%

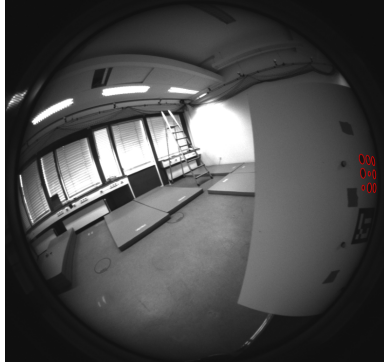
Detection Recall

Marker System	distance	low angle close	pan tilt close	mixed	planar close
ArUco	0.3334	0.0077	0.0458	0.2227	0.0236
S-Tag	0.1969	0.1013	0.0850	0.1319	0.1204
Pi-Tag	0.0900	0.0212	0.0229	nan	nan
Ours	0.0468	0.0024	0.0044	0.0325	0.0051

Root Mean Translation Error



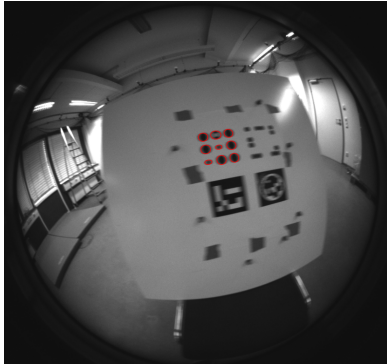
Low viewing angle



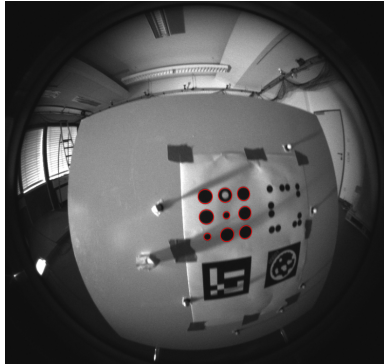
Large image distortion



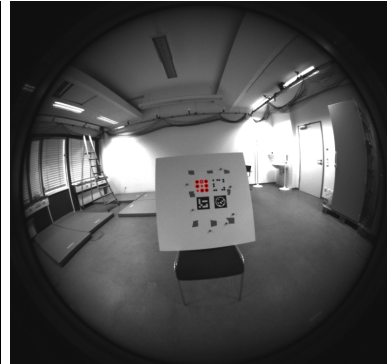
Large image distortion



Significant motion blur



Difficult lighting



Large viewing distance

Marker System	LabelMe	Indoor Scene Recognition
ArUco	110 (3.77%)	193 (1.24%)
STag	293 (10.03%)	308 (1.97%)
Ours	2672 (91.51%)	3146 (20.15%)

False positive detections on the LabelMe [14] and indoor scene recognition [15] datasets.



Examples of false positive detections.





Questions?

- [1] D. Wagner and D. Schmalstieg. “Artoolkitplus for pose tracking on mobile devices”. In: (2007).
- [2] J. Wang and E. Olson. “AprilTag 2: Efficient and robust fiducial detection”. In: *Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*. Oct. 2016.
- [3] J. Wang and E. Olson. “AprilTag 2: Efficient and robust fiducial detection”. In: *2016 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*. IEEE. 2016, pp. 4193–4198.
- [4] F. J. Romero-Ramirez, R. Muñoz-Salinas, and R. Medina-Carnicer. “Speeded up detection of squared fiducial markers”. In: *Image and Vision Computing* 76 (2018), pp. 38–47.
- [5] B. Benligiray, C. Topal, and C. Akinlar. “STag: A stable fiducial marker system”. In: *Image and Vision Computing* 89 (2019), pp. 158–169.
- [6] F. Bergamasco, A. Albarelli, E. Rodolà, and A. Torsello. “RUNE-Tag: A high accuracy fiducial marker with strong occlusion resilience”. In: *CVPR 2011*. 2011, pp. 113–120.
- [7] F. Bergamasco, A. Albarelli, and A. Torsello. “Pi-Tag: A fast image-space marker design based on projective invariants”. In: *Machine Vision and Applications* 24 (Aug. 2013).
- [8] G. Yu, Y. Hu, and J. Dai. “TopoTag: A Robust and Scalable Topological Fiducial Marker System”. In: *IEEE Transactions on Visualization and Computer Graphics (TVCG)* 27.9 (2021), pp. 3769–3780.

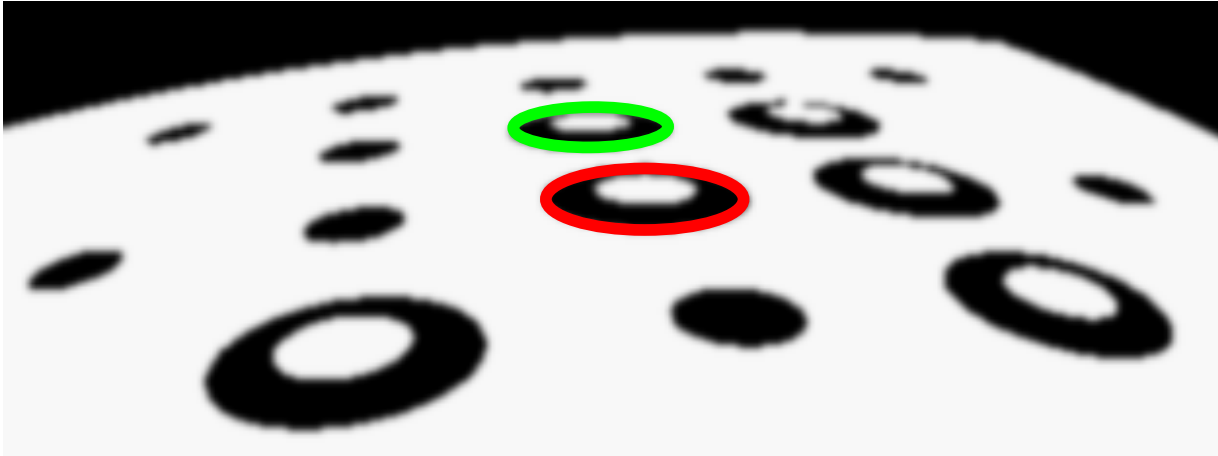
- [9] B. Wang. “LFTag: A Scalable Visual Fiducial System with Low Spatial Frequency”. In: *2020 2nd International Conference on Advances in Computer Technology, Information Science and Communications (CTISC)*. 2020, pp. 140–147.
- [10] *AprilTag website*. URL: <https://april.eecs.umich.edu/software/apriltag> (visited on 05/16/2022).
- [11] *Researchgate*. URL: https://www.researchgate.net/figure/Circular-marker-for-Augmented-Reality_fig1_259752709 (visited on 05/21/2022).
- [12] L. Kneip, H. Li, and Y. Seo. “Upnp: An optimal $O(n)$ solution to the absolute pose problem with universal applicability”. In: *European Conference on Computer Vision*. Springer. 2014, pp. 127–142.
- [13] L. Kneip, D. Scaramuzza, and R. Siegwart. “A novel parametrization of the perspective-three-point problem for a direct computation of absolute camera position and orientation”. In: *CVPR 2011*. IEEE. 2011, pp. 2969–2976.
- [14] B. C. Russell, A. Torralba, K. P. Murphy, and W. T. Freeman. “LabelMe: a database and web-based tool for image annotation”. In: *International journal of computer vision* 77.1 (2008), pp. 157–173.
- [15] A. Quattoni and A. Torralba. “Recognizing indoor scenes”. In: *2009 IEEE conference on computer vision and pattern recognition*. IEEE. 2009, pp. 413–420.

- [16] *Pinclipart website*. URL: https://www.pinclipart.com/pindetail/TiTRbw_request-demo-live-demo-clipart-png-download/ (visited on 09/08/2019).

Backup Slides

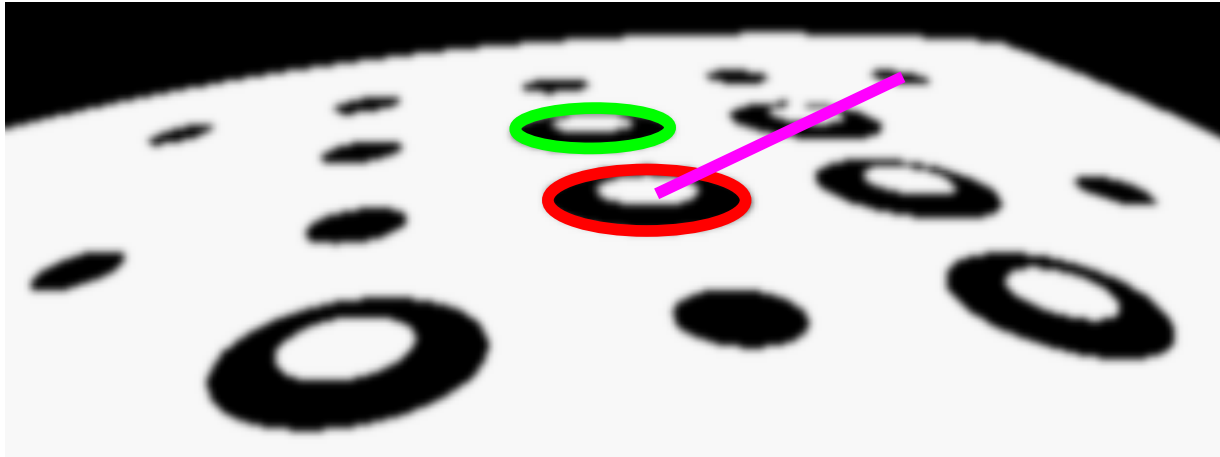
Geometric Heuristic

- find closest neighbor to center ellipse
- perform heuristic filtering based on angle to the closest neighbor



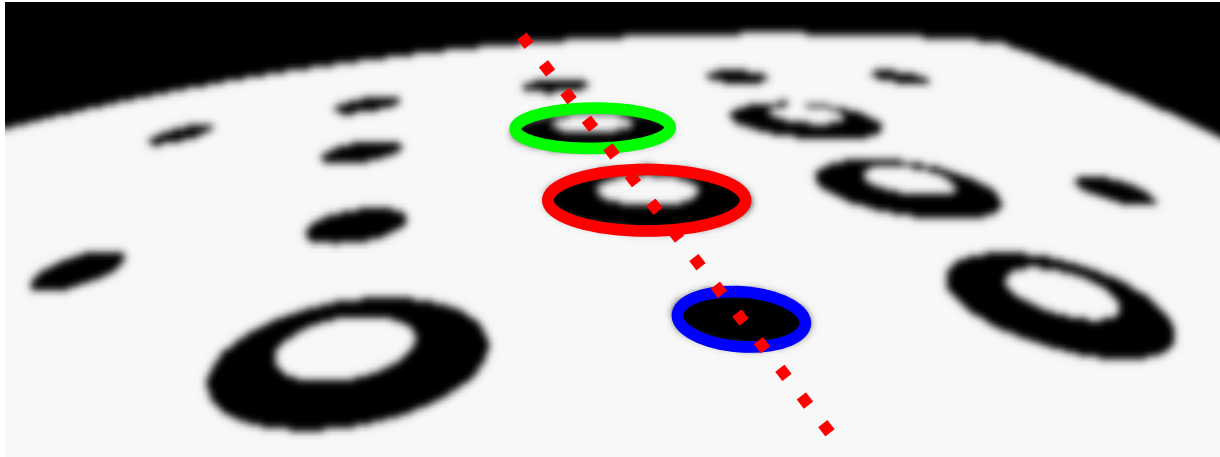
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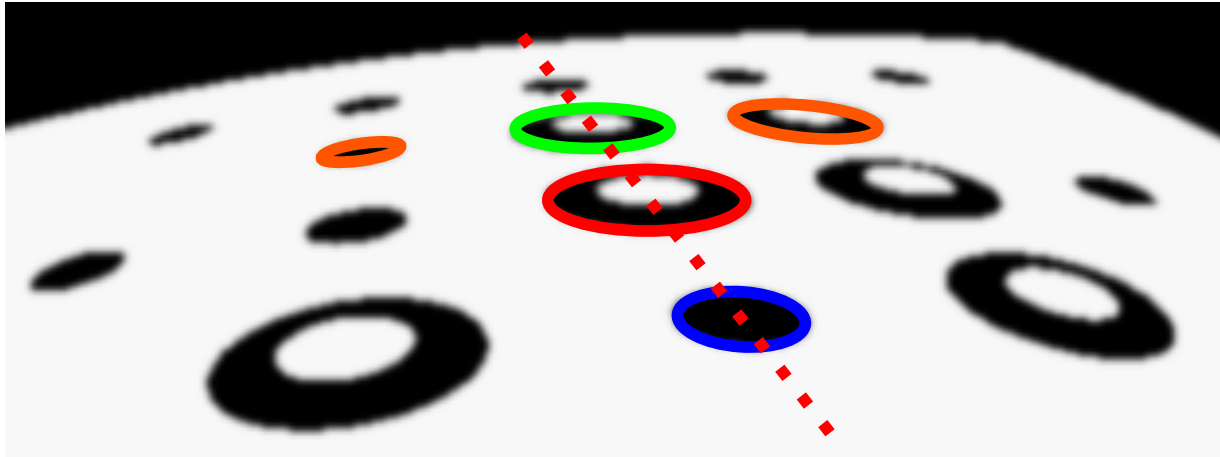
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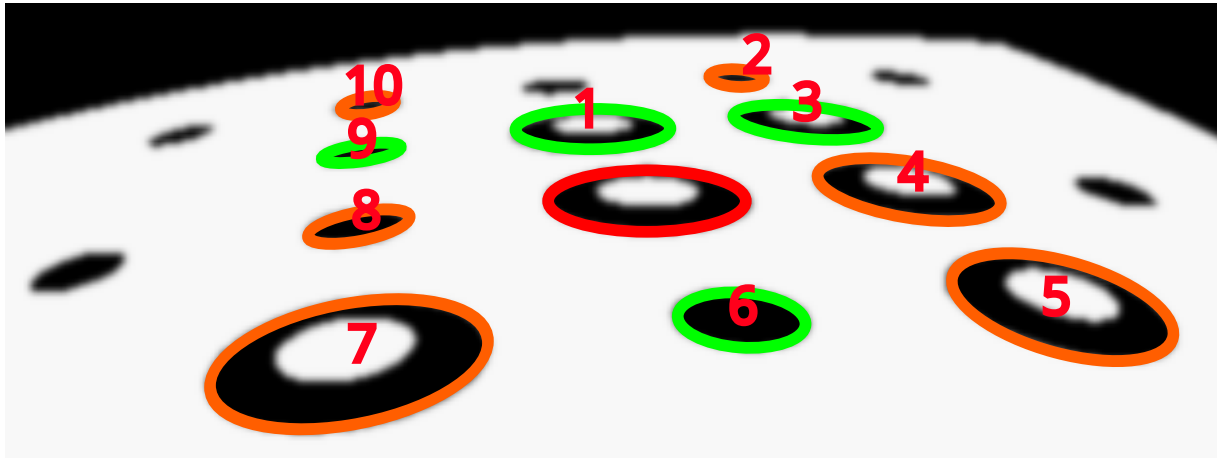
Geometric Heuristic

- find closest neighbor to center ellipse
- perform heuristic filtering based on angle to the closest neighbor



Geometric Heuristic

- brute force search on the remaining neighboring ellipses for best alignment into 3×3 grid



Grid size	Runtime	Number of grids
4×4	2.64s	262,144
5×5	213s	47,807,136
6×6	22h 50m	181,718,080
\vdots	?	≥ 1
19×19	?	≥ 1
20×20	-	0

Number of possible marker grids.