

3DV 2017

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Multiframe Scene Flow with Piecewise Rigid Motion

Vladislav Golyanik, Kihwan Kim, Robert Maier, Matthias Nießner, Didier Stricker and Jan Kautz



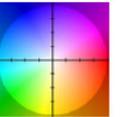
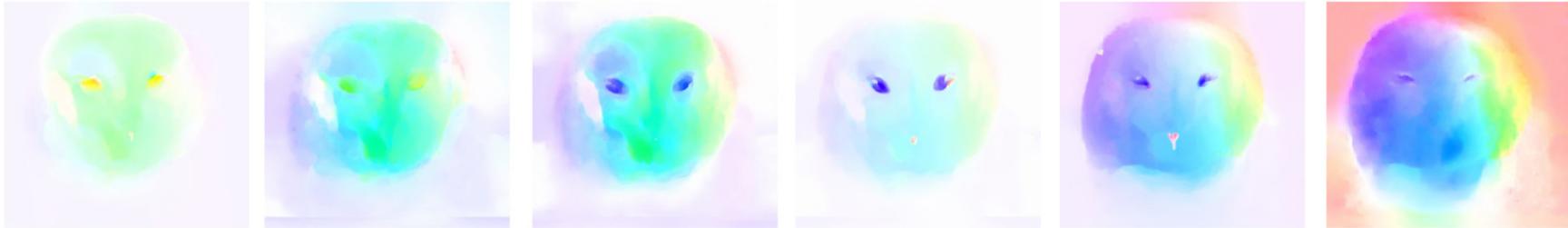
Scene Flow



Scene Flow



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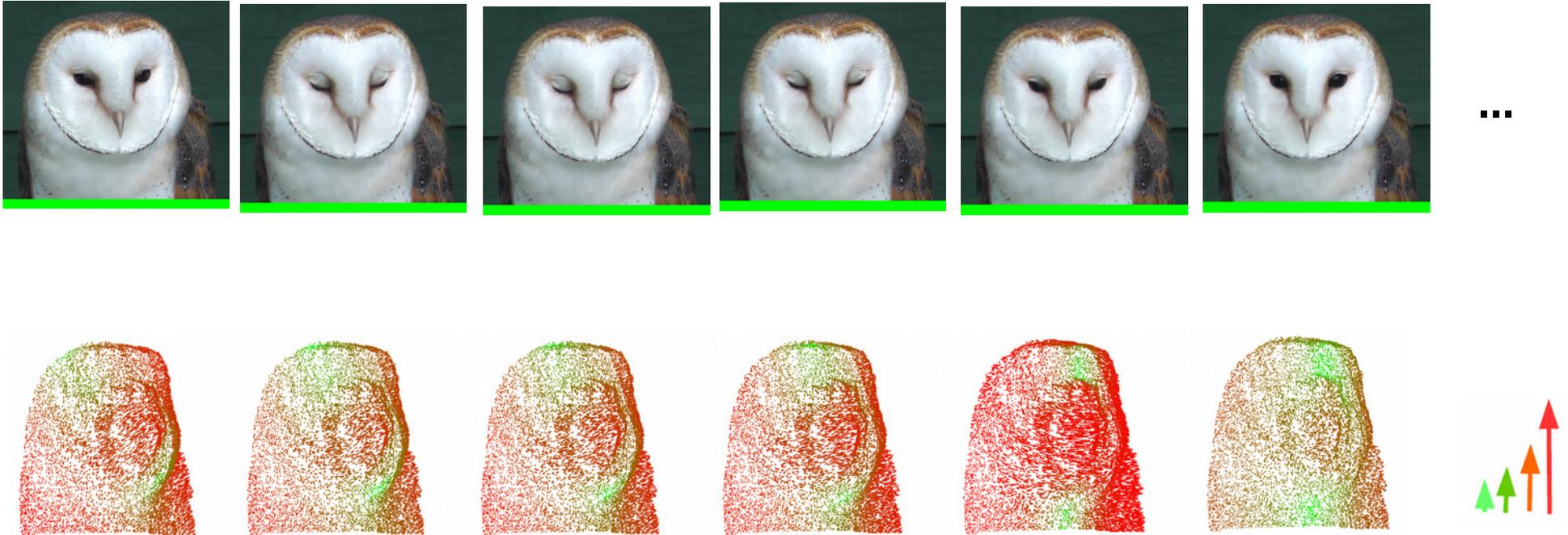
Scene Flow



Scene Flow Estimation:

- input: image sequence (RGB or RGB-D)
- output: 3D displacement field between underlying 3D scene states

Scene Flow



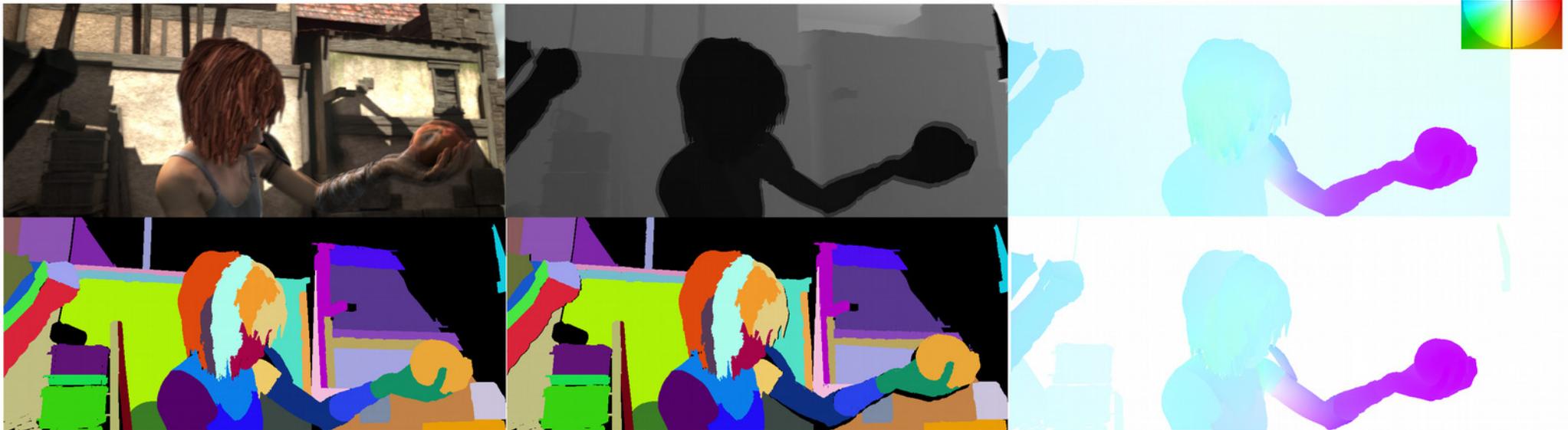
Scene Flow Estimation:

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Overview

input RGB-D frames (overlaid)

ground truth optical flow



oversegmentation of
the reference frame

segmentation transfer
into the current frame

our MSF result
(projected)

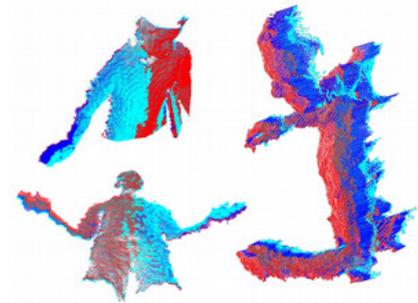
Overview



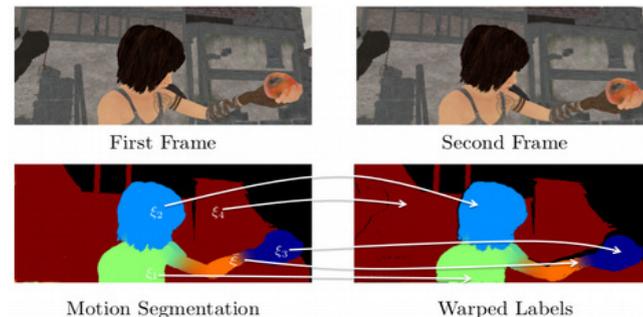
Vogel *et al.* ICCV, 2013.



Quiroga *et al.* ECCV, 2014.



Jaimez *et al.* ICRA, 2015.



Jaimez *et al.* 3DV, 2015.

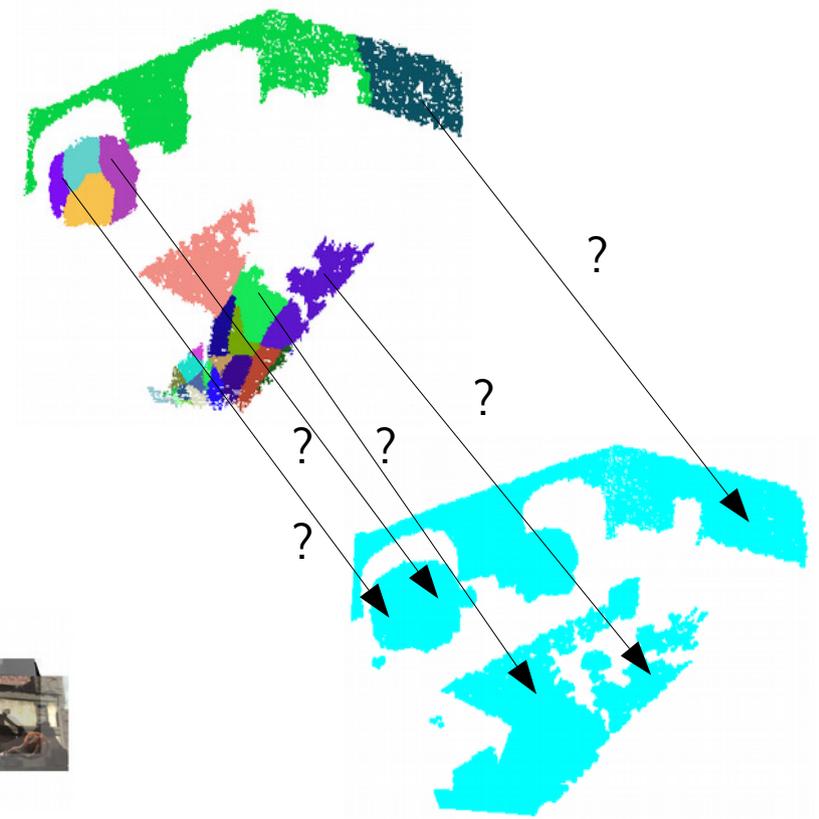
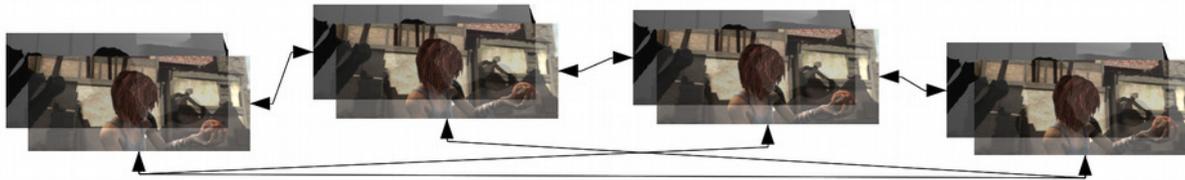
C. Vogel *et al.* Piecewise rigid scene flow. In ICCV, 2013.

J. Quiroga *et al.* Dense semi-rigid scene flow estimation from RGBD images. In ECCV, 2014.

M. Jaimez *et al.* A primal-dual framework for real-time dense rgb-d scene flow. In ICRA, 2015.

M. Jaimez *et al.* Motion cooperation: Smooth piece-wise rigid scene flow from rgb-d images. In 3DV, 2015.

Proposed Approach



Proposed Approach



- **depth channel** is used to obtain oversegmentation of the scene
- segmentation of a scene is kept **fixed**
- a global scene-flow formulation over **multiple frames**

Proposed Approach



- take advantage of **point set registration** (projective point-to-plane ICP term)
- **lifting function** for coherent segment transformations

Proposed Approach

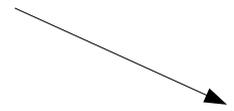
$$\begin{aligned} \mathfrak{E}(\mathbf{T}^1, \mathbf{T}^2, \dots, \mathbf{T}^{|\mathcal{Z}|}, \mathbf{w}) &= \sum_{\zeta \in \mathcal{Z}} \alpha_{\zeta} \mathfrak{E}_{\text{data}}(\mathbf{T}^{\zeta}) + \\ &+ \sum_{\zeta \in \mathcal{Z}} \beta_{\zeta} \mathfrak{E}_{\text{pICP}}(\mathbf{T}^{\zeta}) + \sum_{\zeta \in \mathcal{Z}} \gamma_{\zeta} \mathfrak{E}_{\text{l.reg.}}(\mathbf{T}^{\zeta}, \mathbf{w}) + \\ &+ \eta \mathfrak{E}_{\text{r.opt.}}(\mathbf{w}) + \sum_{\zeta=3}^{|\mathcal{Z}|} \lambda_{\zeta} \mathfrak{E}_{\text{c.}}(\mathbf{T}^{\zeta}). \end{aligned}$$

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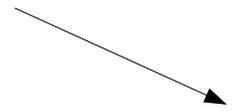
vector of frame-to-frame segment transformations



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vector of frame-to-frame segment transformations

segment-to-segment connectivity weights

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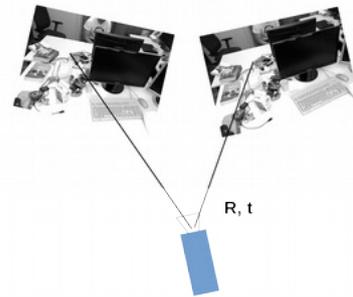
Proposed Approach

vector of frame-to-frame segment transformations

segment-to-segment connectivity weights

brightness constancy

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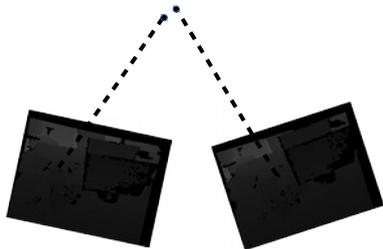
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brightness
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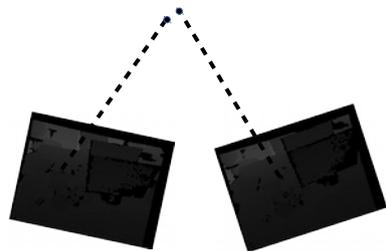
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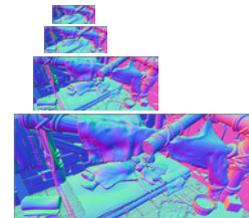
segment-to-segment connectivity weights

brightness constancy

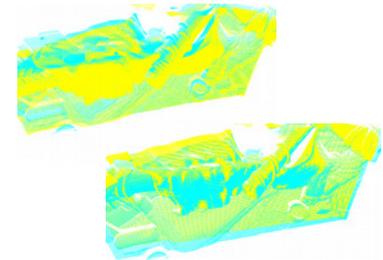
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 \end{aligned}$$



input frames



a pyramid with visualized normals



result of pICP

Proposed Approach

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projective ICP



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lifted segment
pose regularizer

$$+ \eta \mathfrak{E}_{\text{r.opt.}}(\mathbf{w}) + \sum_{\zeta=3}^{|\mathcal{Z}|} \lambda_{\zeta} \mathfrak{E}_{\text{c.}}(\mathbf{T}^{\zeta}).$$

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robust weight
optimizer

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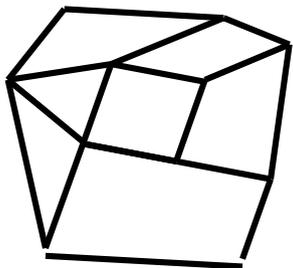
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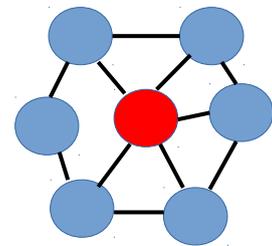


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robust weight optimizer



compute oversegmentation



build a connectivity graph

| | | |
|----|----|----|
| | -1 | |
| -1 | 4 | -1 |
| | -1 | |

Laplace

Proposed Approach

vector of frame-to-frame segment transformations

segment-to-segment connectivity weights

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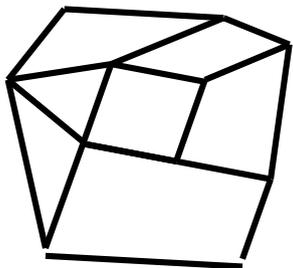


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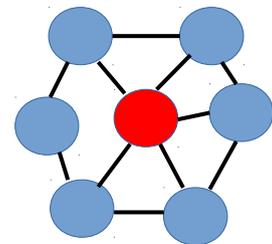
lifted segment pose regularizer

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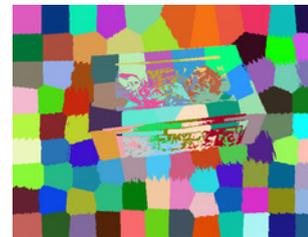
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Laplace



oversegmentation



segment connectivity

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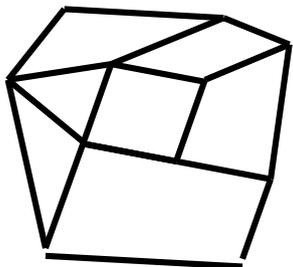


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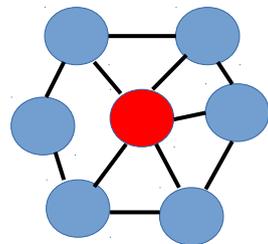
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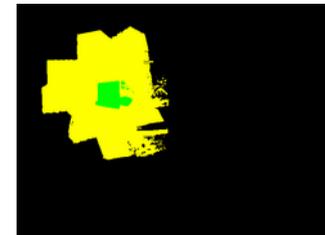
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Laplace



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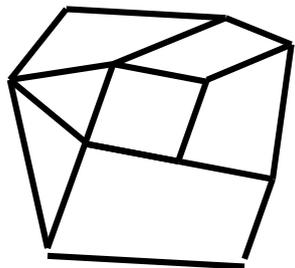
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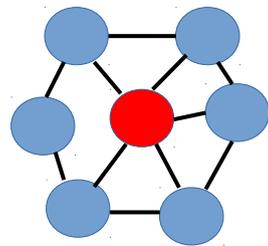
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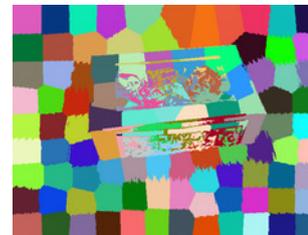
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robust weight optimizer

lifting function $\mathcal{F}(\cdot, \mathbf{w}) = \sum (w_i^2(\cdot) + (1 - w_i^2))$

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robust weight
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multiframe pose
concatenation

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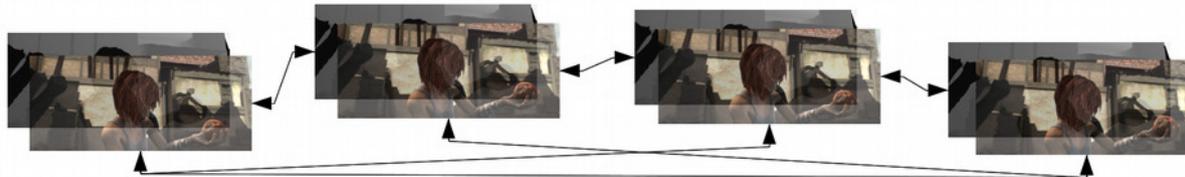
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robust weight optimizer

multiframe pose concatenation



optimization over multiple frames

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robust weight optimizer

multiframe pose concatenation

Huber norm:

$$\|a^2\|_{\epsilon} = \begin{cases} \frac{1}{2}a^2, & \text{for } |a| \leq \epsilon \\ \epsilon(|a| - \frac{1}{2}\epsilon), & \text{otherwise,} \end{cases}$$

Results

In the experimental evaluation we use:

- MPI SINTEL [1]
- virtual KITTI [2]
- Bonn multibody data set [3]
- own RGB-D recordings

... and compare the following methods:

- Primal-Dual Flow [4]
- Semi-Rigid Scene Flow [5]
- Multi-Frame Optical Flow [6]
- tv-l1 optical flow [7]

[1] D. J. Butler *et al.* A naturalistic open source movie for optical flow evaluation. In ECCV, 2012.

[2] A. Gaidon *et al.* Virtual worlds as proxy for multi-object tracking analysis. In CVPR, 2016.

[3] J. Stueckler and S. Behnke. Efficient dense rigid-body motion segmentation and estimation in rgb-d video. IJCV, 2015.

[4] M. Jaimez *et al.* A primal-dual framework for real-time dense rgb-d scene flow. In ICRA, 2015.

[5] J. Quiroga *et al.* Dense semi-rigid scene flow estimation from RGBD images. In ECCV, 2014.

[6] B. Taetz *et al.* Occlusion-aware video registration for highly non-rigid objects. In WACV, 2016.

[7] C. Zach *et al.* A duality based approach for realtime tv-l1 optical flow. In GCPR, 2007.

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End Point Error is defined as $\|(u - u_{GT}), (v - v_{GT})\|$

$(u, v)^T$ is a projected flow vector

$(u_{GT}, v_{GT})^T$ is a ground truth vector

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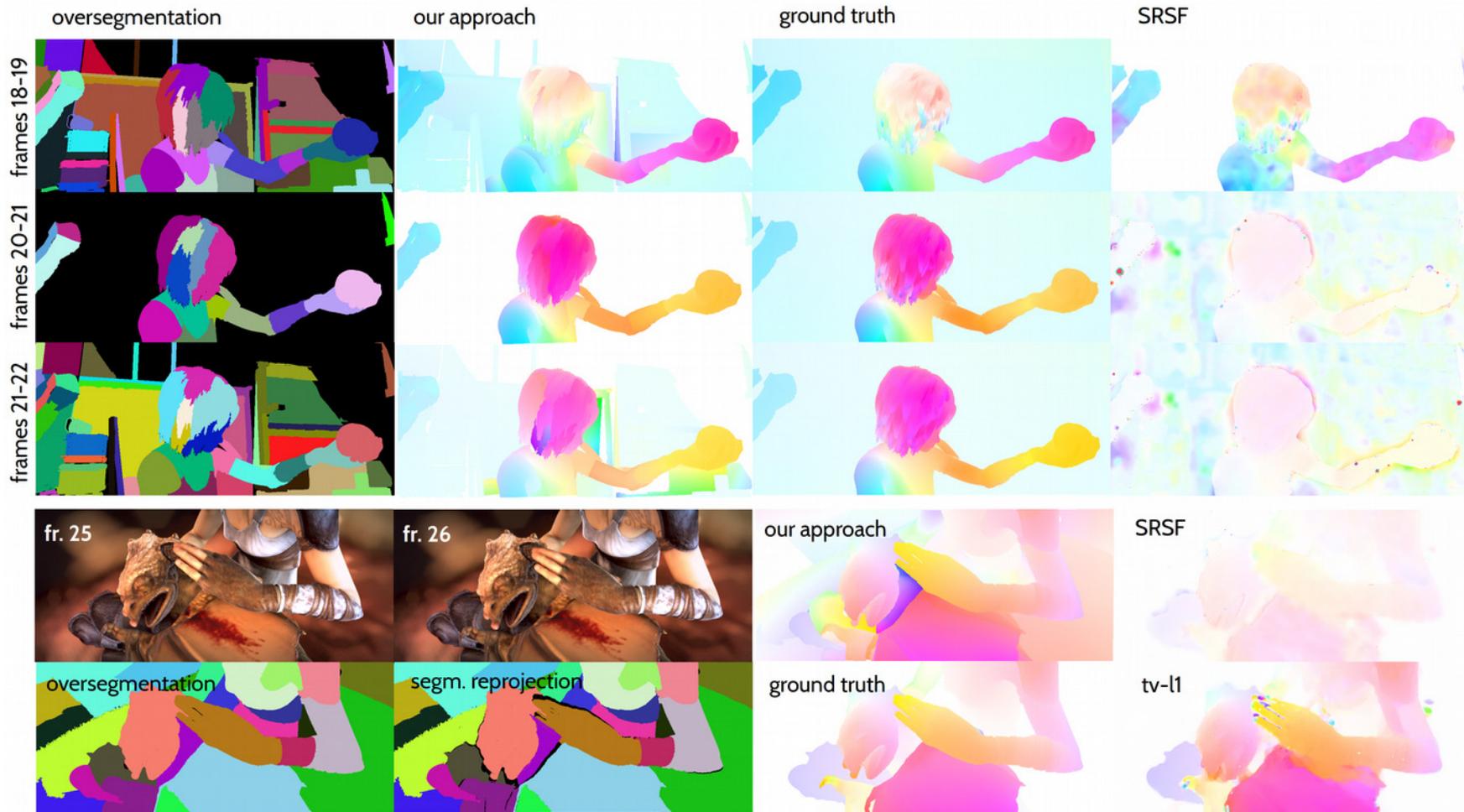
[4] M. Jaimez *et al.* A primal-dual framework for real-time dense rgb-d scene flow. In ICRA, 2015.

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Results



| | <i>alley1</i> | <i>bandage1</i> | <i>sleeping2, rigid</i> |
|------------|-----------------|-----------------|-------------------------|
| SRSF [5] | 2.46122/2.40833 | 2.47801/2.46389 | 1.13584 |
| MSF | 0.740127 | 1.69865 | 0.307526 |

...

Results

We use RGBD input sequences for scene flow estimation



Input RGB



Input Depth



Ground truth optical flow



Projected scene flow (ours)

Average AEPE = 0.963731 (depth range = 0 to inf)

Conclusions and Future Work



We propose a new multiframe RGB-D scene flow approach

Main novelties:

- segmentation is obtained on the depth channel and kept fixed
- projective ICP term
- lifted segment pose regularizer

Next: combine MSF with semantic segmentation, test other energy terms

Thank you for your attention!

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