

# Dense Localization and Mapping

**Jürgen Sturm**

Joint work with Frank Steinbrücker, Jakob Engel,  
Christian Kerl, and Daniel Cremers

# Introduction

- **(RGB-D) Cameras are rich sensors** that provide intensities, color, depth at video frame rates
- Lightweight and cheap
- **Many useful applications** in robotics:  
Localization, mapping, navigation, obstacle avoidance



2



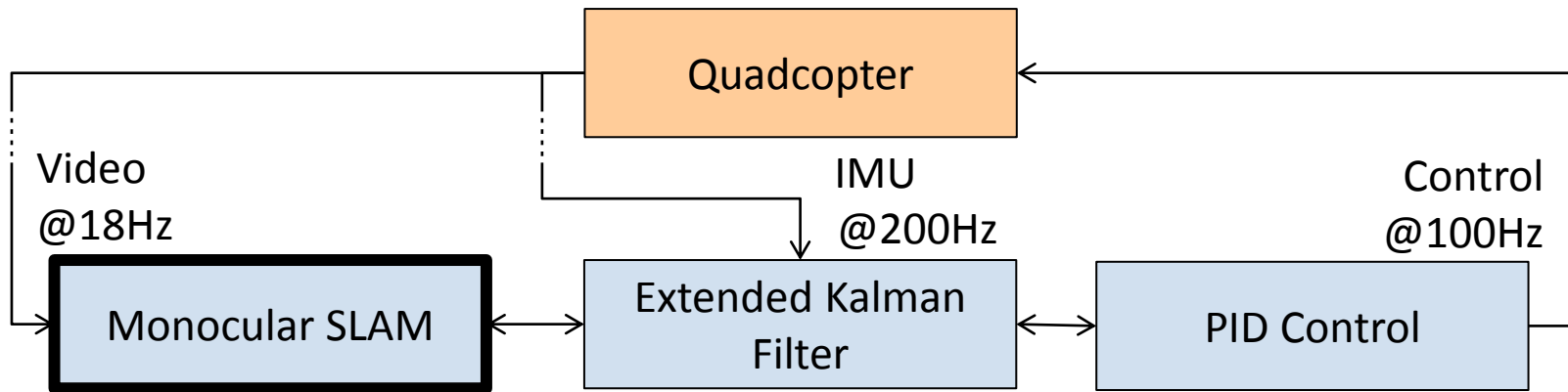
# Feature-based Visual Navigation

[Engel, Sturm, Cremers, IROS '12]

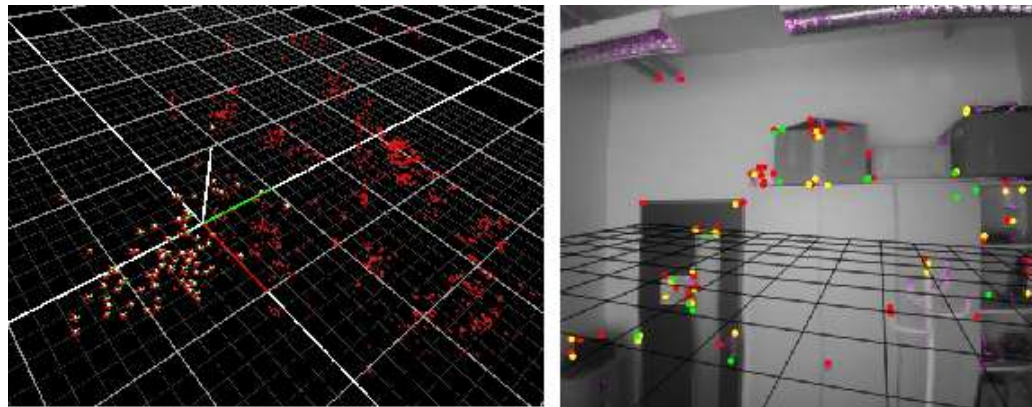
# Feature-based Visual Navigation

[Engel, Sturm, Cremers, IROS '12]

## ■ Architecture



## ■ Based on PTAM [Klein and Murray, ISMAR '07]



# Motivation

- Video feed from quadrocopter



# Motivation

- What PTAM actually sees



# Motivation

- **Problem:** Most approaches only use a small fraction of the available data
    - Keypoint detection
    - Visual features
  - **Question:** How can we use most/all information to maximize the performance?
- ➔ In this talk: Dense methods for localization and mapping

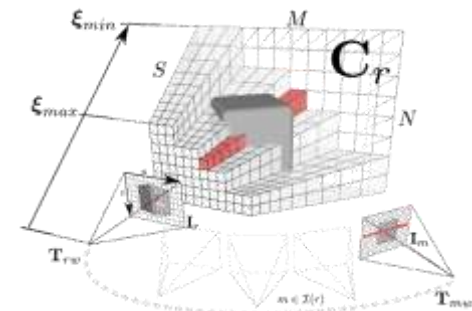
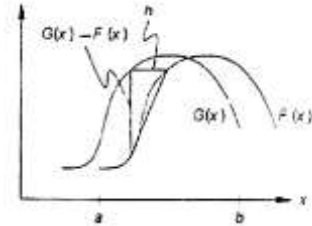
# Outline of the Talk

- Part 1: Dense tracking
- Part 2: Dense reconstruction
- Part 3: Evaluation and benchmarking



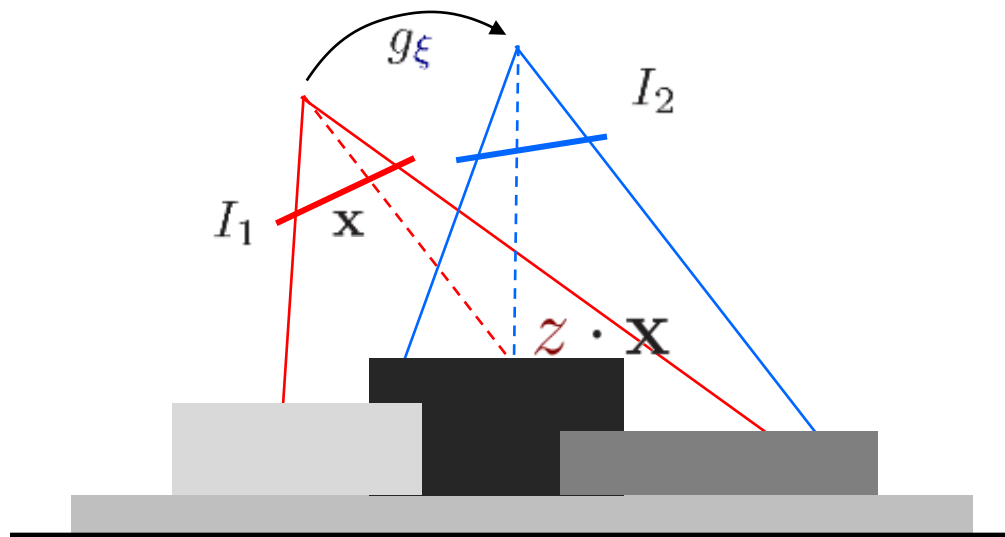
# Related Work on Dense Tracking

- Lucas and Kanade (IJCAI'81)
- Lovegrove et al. (IV'11)
- Newcombe et al. (ICCV'11)
- Comport/Tykkälä et al. (ICCV'11)



# Dense Tracking

- How can we exploit ALL data of the image?
- Idea



- Photo-consistency constraint

$$I_1(\mathbf{x}) = I_2(\pi(g_{\xi}(z \cdot \mathbf{x}))) \text{ for all pixels } \mathbf{x}$$

# How to deal with noise?

- Photo-consistency constraint will not perfectly hold
  - Sensor noise
  - Pose error
  - Reflections, specular surfaces
  - Dynamic objects (e.g., walking people)

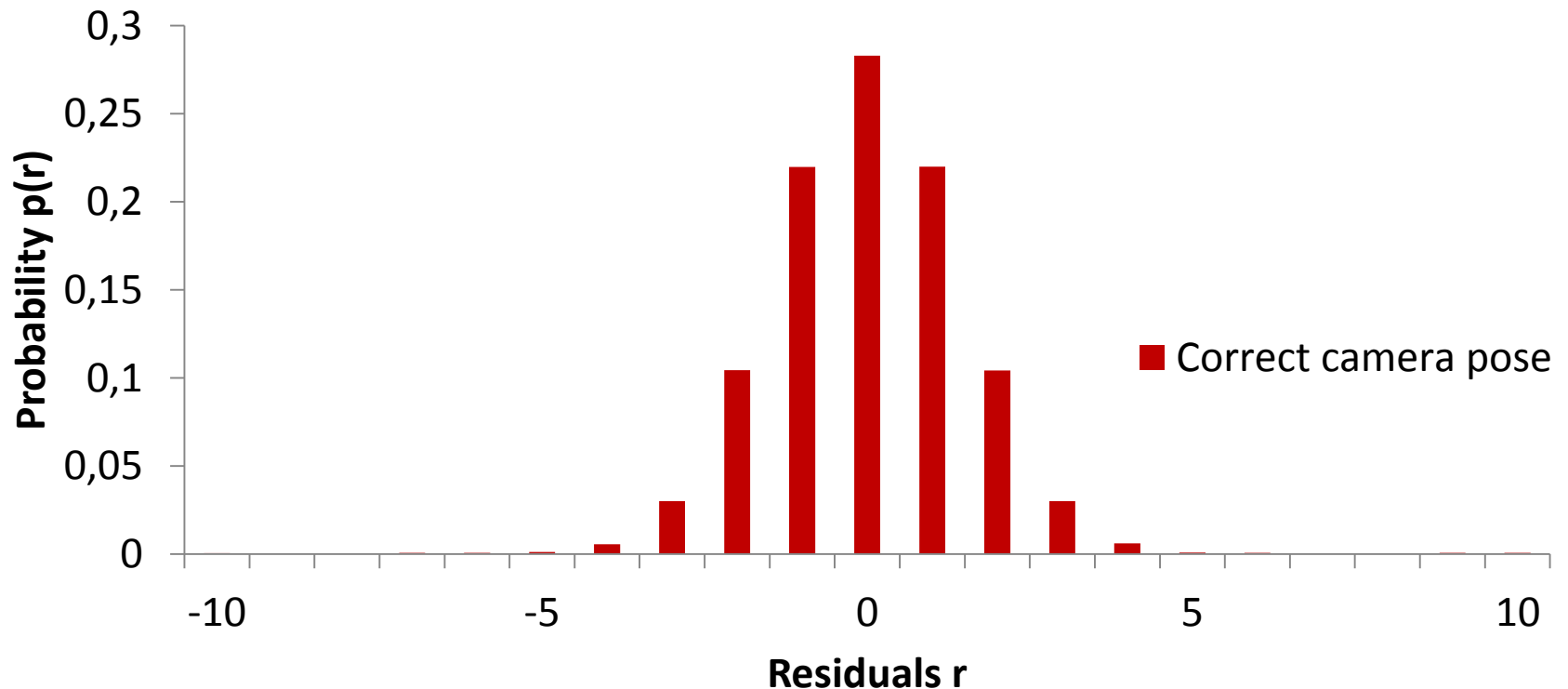
- Residuals will be non-zero

$$r = I_1(\mathbf{x}) - I_2(\pi(g_\xi(z \cdot \mathbf{x})))$$

- Residual distribution  $p(r)$

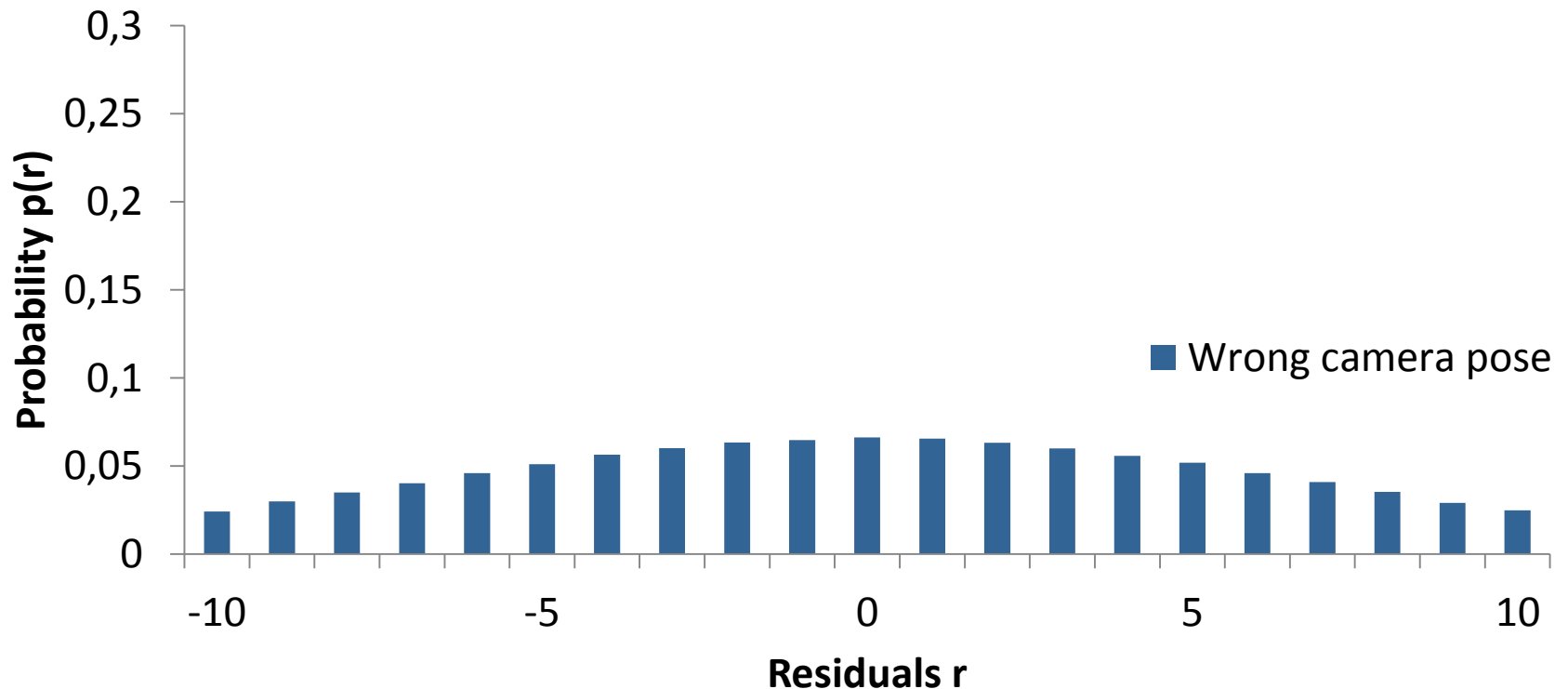
# Residual Distribution

- Zero-mean, peaked distribution
- Example: Correct camera pose



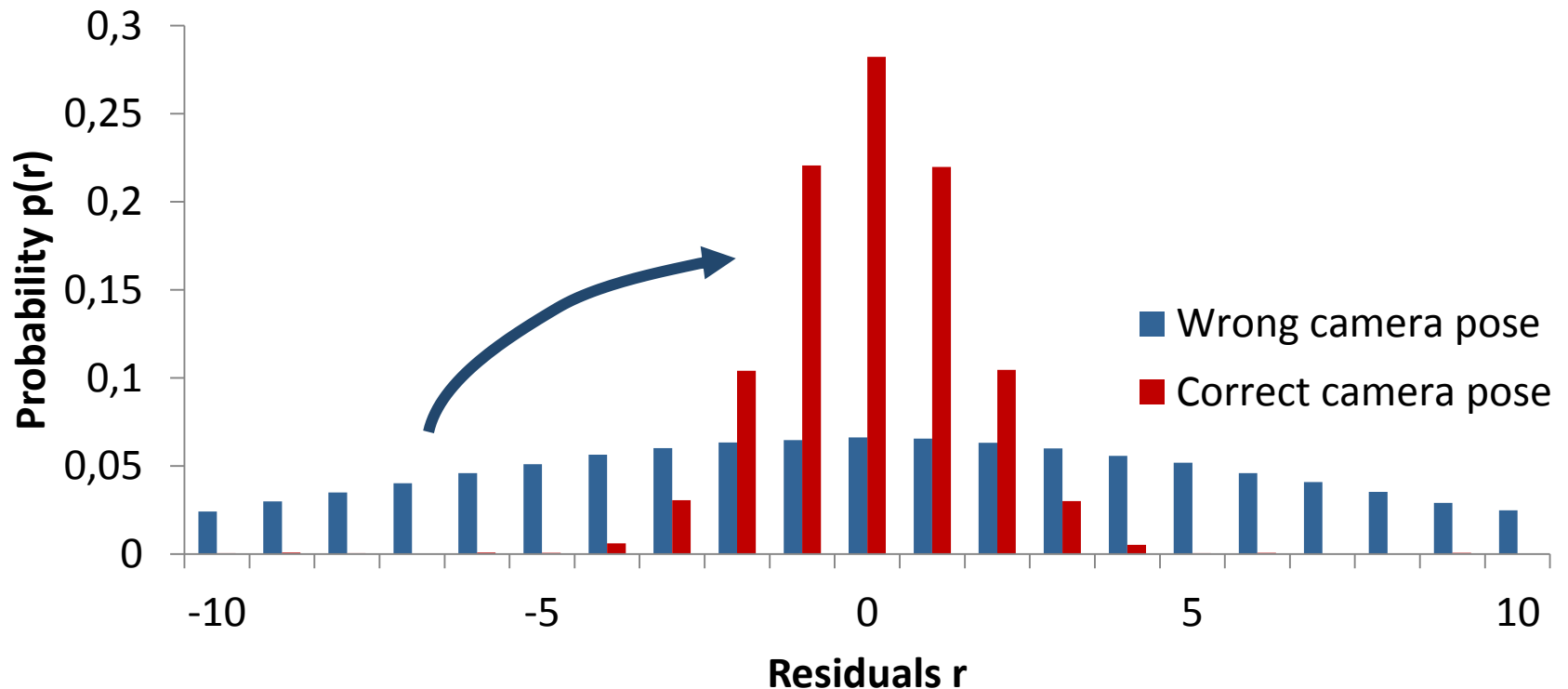
# Residual Distribution

- Zero-mean, peaked distribution
- Example: Wrong camera pose

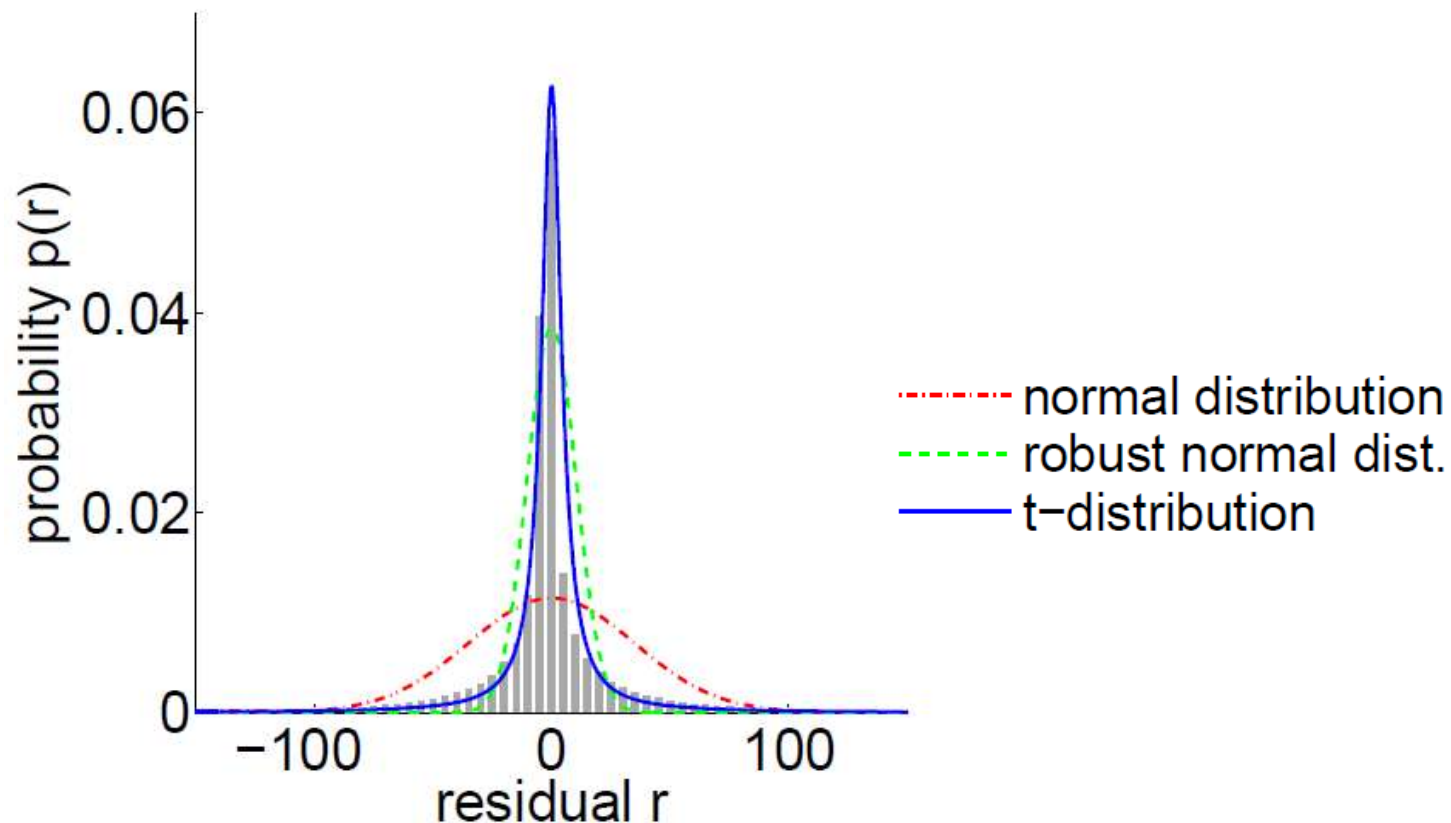


# Residual Distribution

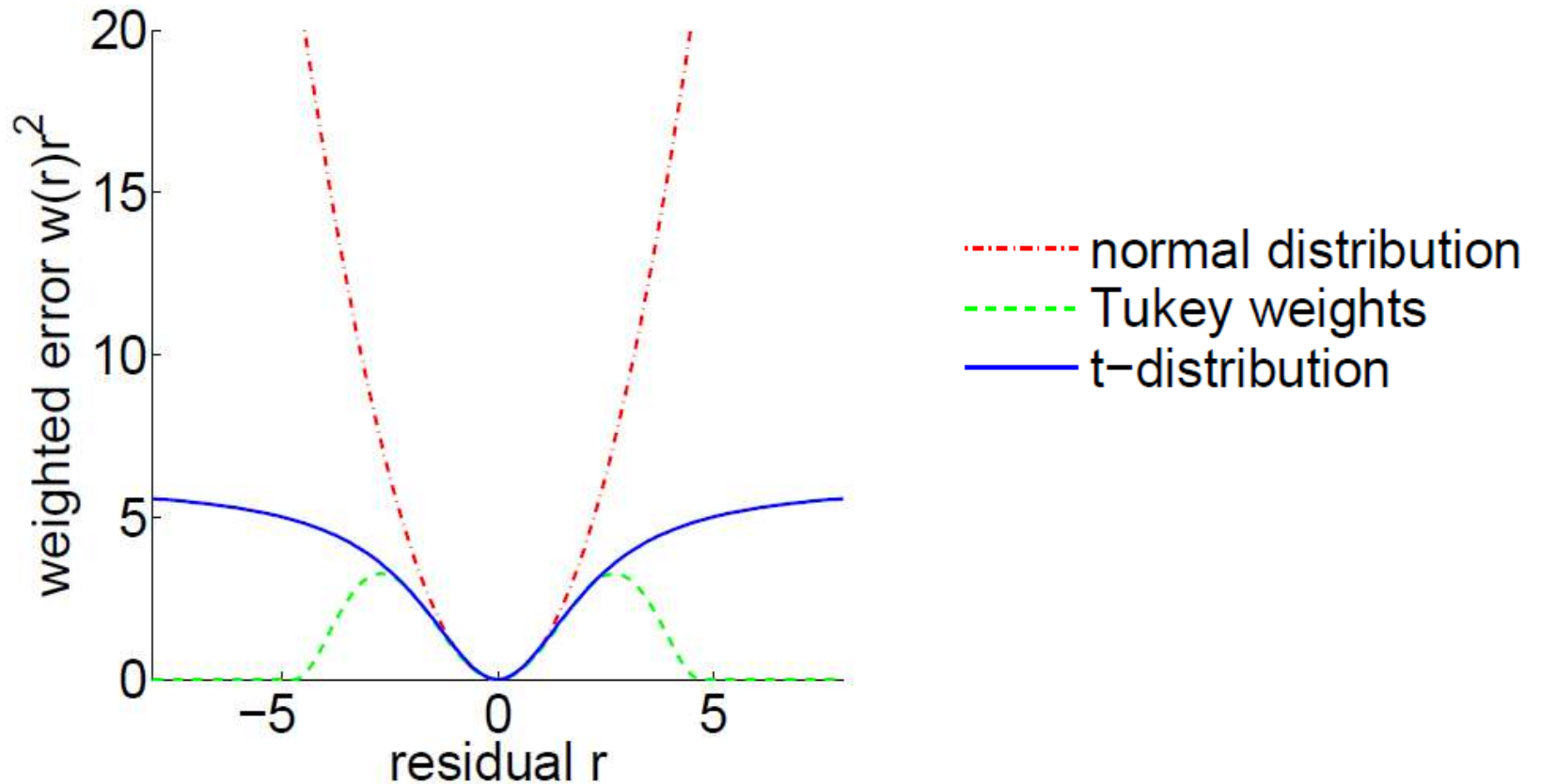
- **Goal:** Find the camera pose that maximizes the observation likelihood



# What is a Good Model for the Residual Distribution?



# Weighted Error





# Example Weights

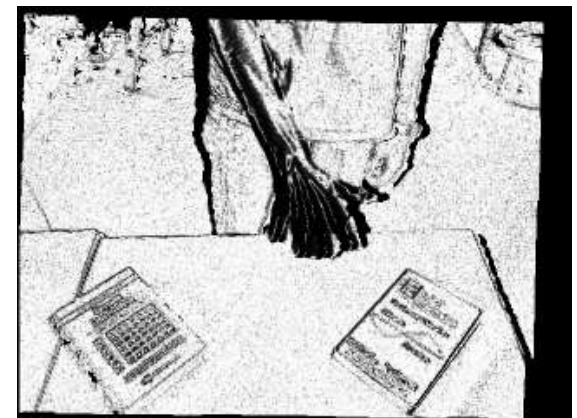
- Robust sensor model allows to down-weight outliers (dynamic objects, motion blur, reflections, ...)



Scene



Residuals



Weights

# Motion Estimation

- **Goal:** Find the camera pose that maximizes the observation likelihood

$$\xi^* = \arg \max_{\xi} \prod_i p(r_i(\xi))$$

compute over all pixels

- Assume pixel-wise residuals are conditionally independent
- How can we solve this optimization problem?

# Example



First input image



Second input image



Residuals

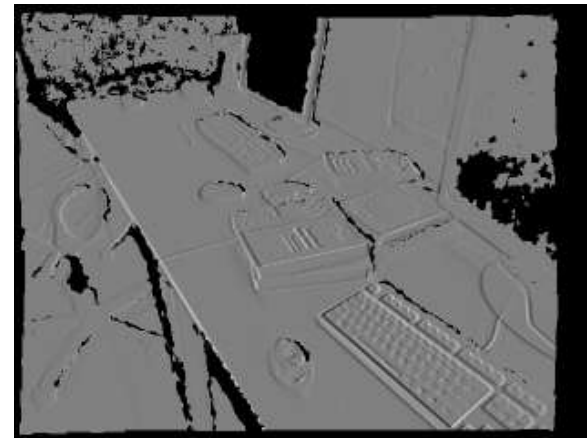


Image Jacobian for  
Camera motion along x axis

# Approach

- Take negative logarithm

$$\xi_{\text{MAP}} = \arg \min_{\xi} \sum_i -\log p(r_i(\xi))$$

- Set derivative to zero

$$\sum_i \frac{\partial \log p(r_i(\xi))}{\partial \xi} = \sum_i \frac{\partial \log p(r_i)}{\partial r_i} \frac{\partial r_i(\xi)}{\partial \xi} \stackrel{!}{=} 0$$

# Approach (cont.d)

- This can be rewritten as a weighted least squares problem

$$\xi^* = \arg \min_{\xi} \sum_i w(r_i) (r_i(\xi))^2$$

with weights  $w(r_i) = \frac{\partial \log p(r_i)}{\partial r_i} \frac{1}{r_i}$

- $r_i(\xi)$  is non-linear in  $\xi$
- Need to linearize, solve, and iterate

# Iteratively Reweighted Least Squares

Problem:  $\xi^* = \arg \min_{\xi} \sum_i w(r_i) (r_i(\xi))^2$

Algorithm:

1. Compute weights  $w(r_i) = \frac{\partial \log p(r_i)}{\partial r_i} \frac{1}{r_i}$

2. Linearize in the camera motion  $\xi$

$$r_{\text{lin}}(\xi) = r(0) + J\Delta\xi$$

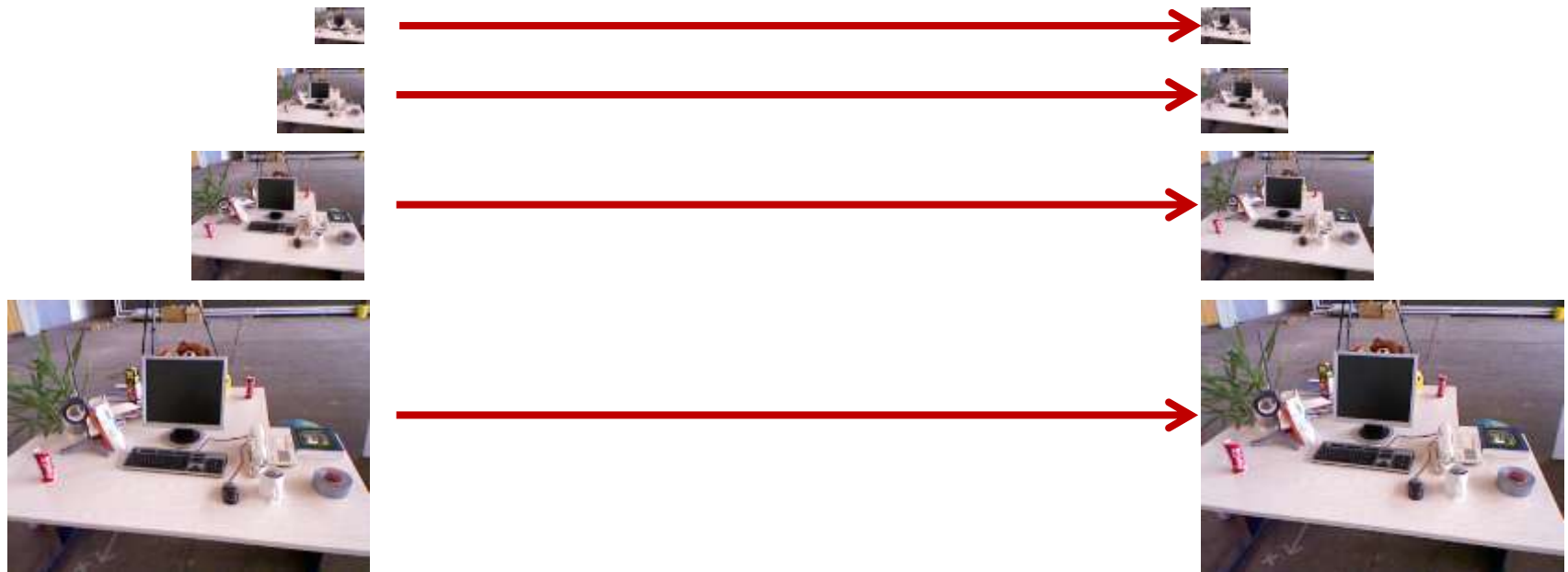
3. Build and solve normal equations

$$J^T W J \Delta\xi = -J^T W \mathbf{r}(0)$$

4. Repeat until convergence

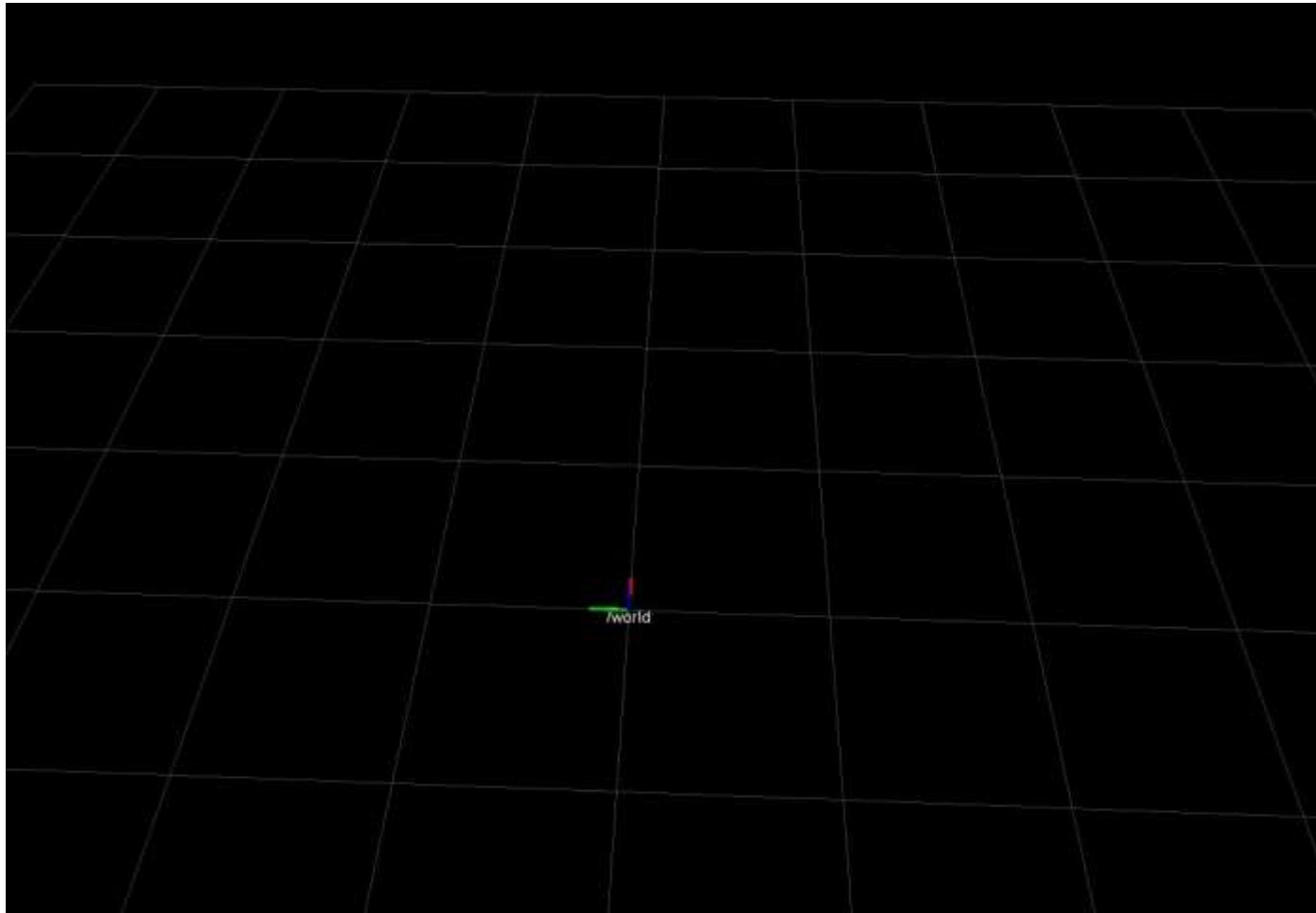
# Coarse-to-Fine

- Linearization only holds for small motions
- Coarse-to-fine scheme
- Image pyramids



# Dense Tracking: Results

[Steinbrücker et al., ICCV LDRMC'11]



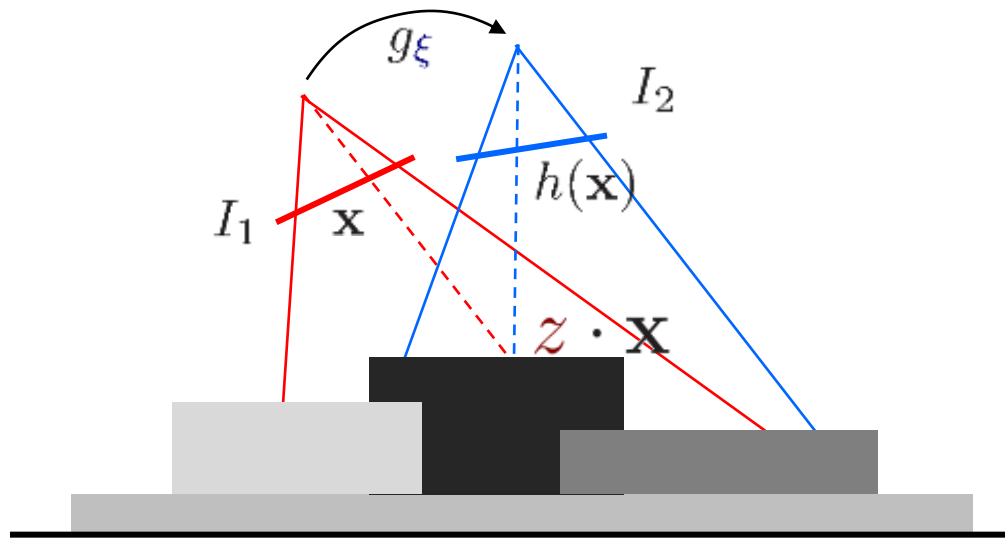


# Summary: Dense tracking

- Pro
  - Super fast, highly accurate
  - Low memory consumption
- Con
  - Accumulates drift over time, sometimes diverges
- Next steps
  - Apply this method on the quadrocopter

# Dense Reconstruction

- Can we use the same principle for 3D reconstruction?



- Photo-consistency constraint

$$I_1(\mathbf{x}) = I_2(\pi(g_\xi(z \cdot \mathbf{x}))) \text{ for all pixels } \mathbf{x}$$

# Dense Reconstruction

- Dense tracking [Steinbrücker et al., ICCV LDRMC'11]
  - Given intensity images and **depth maps**
  - Estimate **camera pose**

$$\min_{\xi} \int_{\Omega} |I_1(\mathbf{x}) - I_2(\pi(g_{\xi}(z \cdot \mathbf{x})))|^2 d\mathbf{x}$$

- Dense reconstruction [Stühmer et al., DAGM'10]
  - Given intensity images and **camera poses**
  - Estimate **depth map**

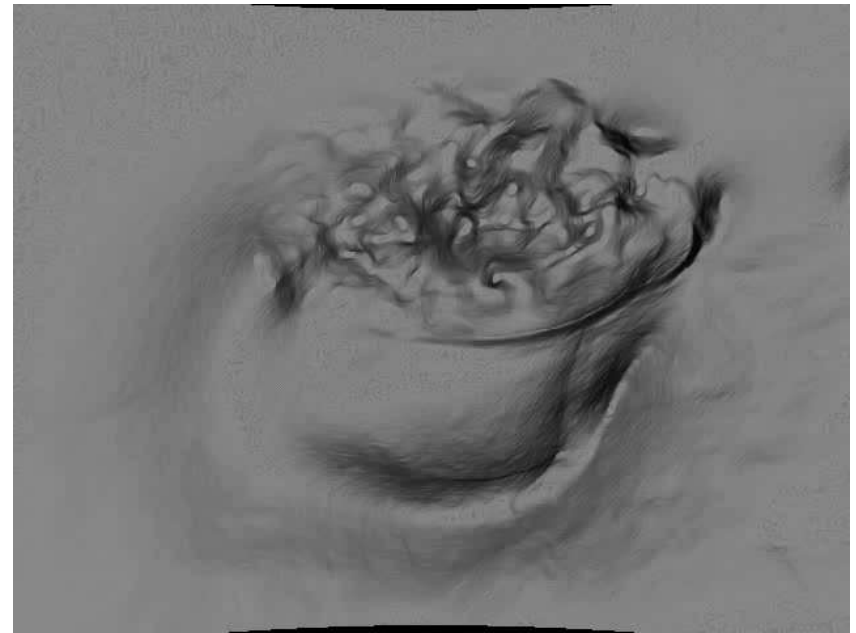
$$\min_z \int_{\Omega} |I_1(\mathbf{x}) - I_2(\pi(g_{\xi}(z \cdot \mathbf{x})))|^2 d\mathbf{x}$$

# Dense Reconstruction: Results

[Stühmer et al., DAGM'10]



Input: Intensity images + pose



Output: Estimated Geometry

# Evaluation and Benchmarking

- How can we evaluate such methods?
- What are good evaluation criteria?
  - Accuracy of the estimated camera trajectory
  - Robustness to dynamic objects, noise, ...
  - Accuracy of the 3D model

# Existing Benchmarks

- Intel dataset: laser + odometry [Haehnel et al., 2004]
- New College dataset: stereo + omni-directional vision + laser + IMU [Smith et al., IJRR'2009]
- KITTI Vision benchmark: stereo [Geiger et al., CVPR'12]
- Our contribution: Dataset for RGB-D evaluation



Intel



New College



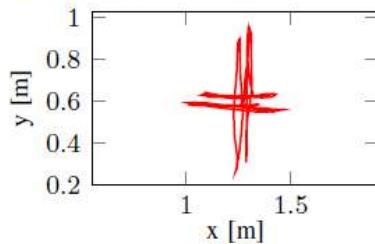
KITTI



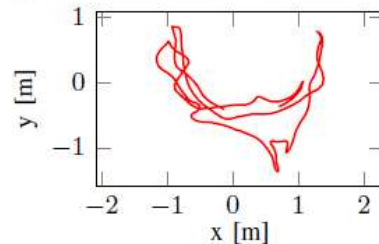
RGB-D

# Recorded Scenes

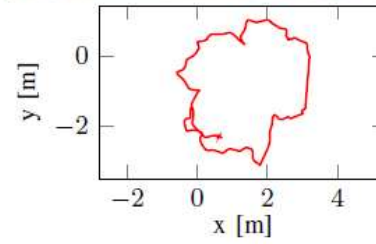
- Different environments (office, industrial hall, ...)
- Large variations in camera speed, camera motion, illumination, number of features, dynamic objects, ...
- Handheld and robot-mounted sensor



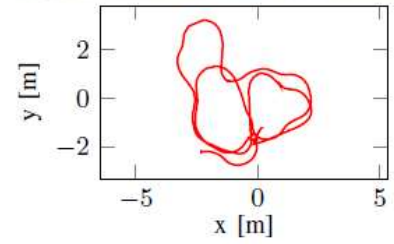
(a) fr1/xyz



(b) fr1/room



(c) fr2/desk



(d) fr2/slam

# Dataset Acquisition

- Motion capture system
  - Camera pose (100 Hz)
- Microsoft Kinect (later: Asus Xtion Pro Live)
  - Color images (30 Hz)
  - Depth images (30 Hz)
- External video camera (for documentation)



# Motion Capture System

- 9 high-speed cameras mounted in room
- Cameras have active illumination and pre-process image (thresholding)
- Cameras track positions of retro-reflective markers



# Calibration

Calibration of the overall system is not trivial:

1. Intrinsic calibration (Mocap + Kinect)
2. Extrinsic calibration (Kinect vs. Mocap)
3. Time synchronization (Kinect vs. Mocap)



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## RGB-D SLAM Dataset and Benchmark

Contact: Jürgen Sturm

We provide a large dataset containing RGB-D data and ground-truth data with the goal to establish a novel benchmark for the evaluation of visual odometry and visual SLAM systems. Our dataset contains the color and depth images of a Microsoft Kinect sensor along the ground-truth trajectory of the sensor. The data was recorded at full frame rate (30 Hz) and sensor resolution (640×480). The ground-truth trajectory was obtained from a high-accuracy motion-capture system with eight high-speed tracking cameras (100 Hz). Further, we provide the accelerometer data from the Kinect. Finally, we propose an evaluation criterion for measuring the quality of the estimated camera trajectory of visual SLAM systems.



### Quick Links

[Download page](#)[File formats](#)[Camera parameters](#)[Useful tools and scripts](#)

### How can I use the RGB-D Benchmark to evaluate my SLAM system?

1. Download one or more of the RGB-D benchmark sequences ([file formats](#), [useful tools](#))
2. Run your favorite visual odometry/visual SLAM algorithm (for example, [RGB-D SLAM](#))
3. Save the estimated camera trajectory to a file ([file formats](#), [example trajectory](#))
4. Evaluate your algorithm by comparing the estimated trajectory with the ground truth trajectory. We provide an [automated evaluation tool](#) to help you with the evaluation. There is also an [online version](#) of the tool.

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## Dataset Download

We recommend that you use the '**xyz**' series for your first experiments. The motion is relatively small, and only a small volume on an office desk is covered. Once this works, you might want to try the '**desk**' dataset, which covers four tables and contains several loop closures.

We are happy to share our data with other researchers. Please refer to the [respective publication](#) when using this data.

Remarks:

- The file formats are described [here](#).
- The intrinsic camera parameters are [here](#).
- We provide a set of [useful tools](#) for working with the dataset.
- The `_validation` sequences do not contain ground truth. They can only be evaluated using the [online tool](#).

Sequence name	Duration	Length	Download	
<b>Category: Testing and Debugging</b>				
freiburg1_xyz	30.09s	7.112m	tgz (0.47GB)	<a href="#">more info</a>
freiburg1_rpy	27.67s	1.664m	tgz (0.42GB)	<a href="#">more info</a>
freiburg2_xyz	122.74s	7.029m	tgz (2.39GB)	<a href="#">more info</a>

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## freiburg1\_xyz: RGB movie



Download this movie as [avi](#)  
 Related movies: [RGB movie](#) and, [depth movie](#), [external camera view](#)

freiburg1_xyz	30.09s	7.112m	🌐tgz (0.47GB)	<a href="#">more info</a>
freiburg1_rpy	27.67s	1.664m	🌐tgz (0.42GB)	<a href="#">more info</a>
freiburg2_xyz	122.74s	7.029m	🌐tgz (2.39GB)	<a href="#">more info</a>

Download

... is relatively small, and only a  
 the 'desk' dataset, which covers

...ive publication when using this

...ed using the online tool.

ad

# File Formats

- In total: 69 sequences (33 training, 36 testing)
- One TGZ archive per sequence, containing
  - Color and depth images (PNG)
  - List of color images (timestamp filename)
  - List of depth images (timestamp filename)
  - List of camera poses (timestamp tx ty tz qx qy qz qw)

# What Is a Good Evaluation Metric?

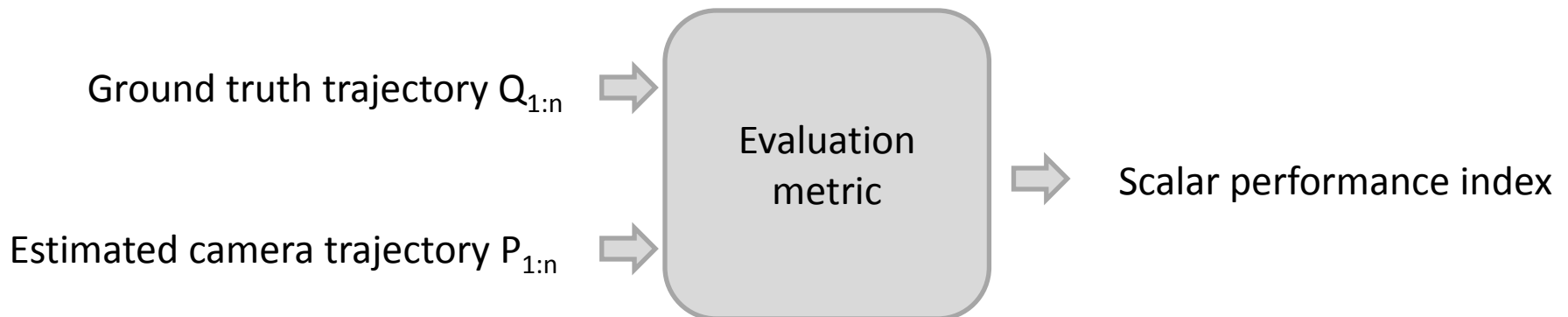
- Visual odometry system outputs
  - Camera trajectory (accumulated)
- Visual SLAM system outputs
  - Camera trajectory
  - 3D map
- Ground truth
  - Camera trajectory

# What Is a Good Evaluation Metric?

- Trajectory comparison
  - Ground truth trajectory
  - Estimate camera trajectory
- Two evaluation metrics
  - Drift per second
  - Global consistency

$$Q_1, \dots, Q_n \in \text{SE}(3)$$

$$P_1, \dots, P_n \in \text{SE}(3)$$





# Relative Pose Error (RPE)

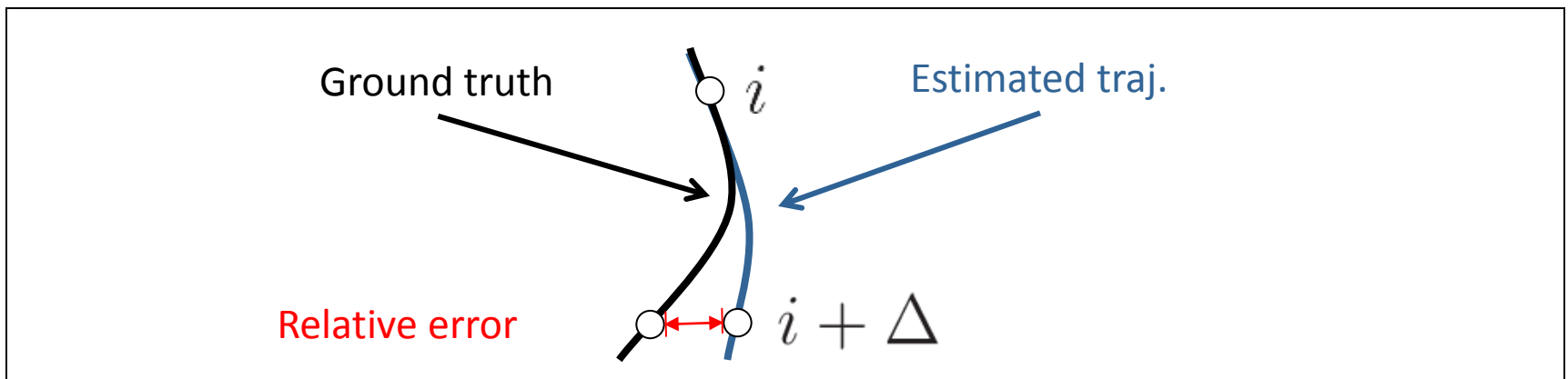
- Measures the (relative) drift between the  $i$ -th frame and the  $(i+\Delta)$ -th frame

$$E_i := \left( Q_i^{-1} Q_{i+\Delta} \right)^{-1} \left( P_i^{-1} P_{i+\Delta} \right)$$

Relative error

True motion

Estimated motion



# Relative Pose Error (RPE)

How to choose the time delta  $\Delta$ ?

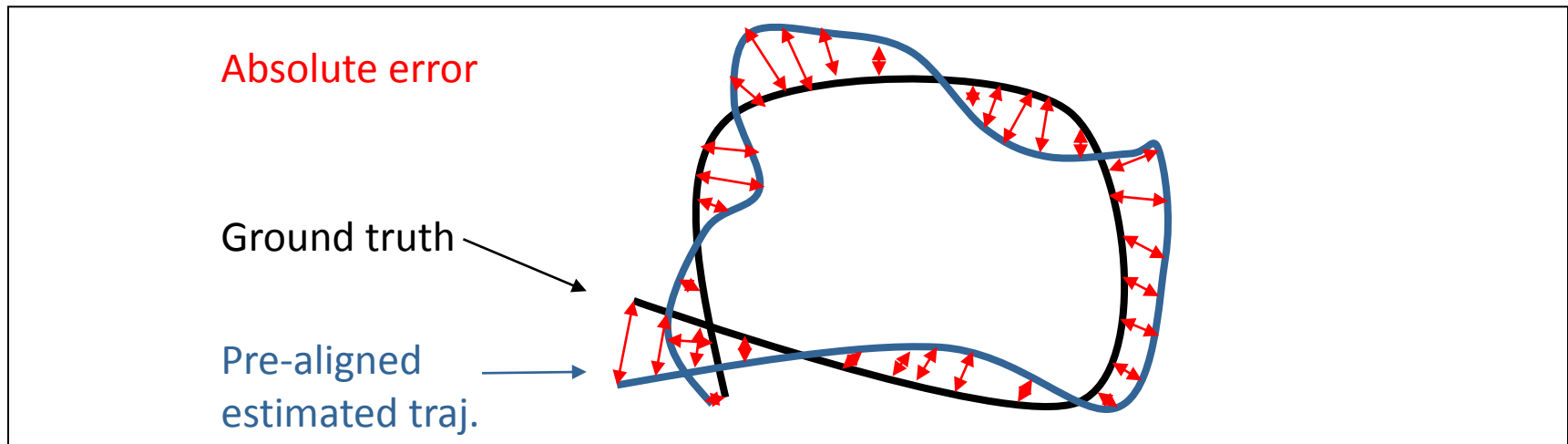
- For odometry methods:
  - $\Delta=1$ : Drift per frame
  - $\Delta=30$ : Drift per second
- For SLAM methods:
  - Average over all possible deltas
  - Measures the global consistency

# Absolute Trajectory Error (ATE)

- Alternative method to evaluate SLAM systems
- Requires pre-aligned trajectories

$$E_i := Q_i^{-1} S P_i$$

Absolute error      Groundtruth Alignment Estimated



# Evaluation Tools

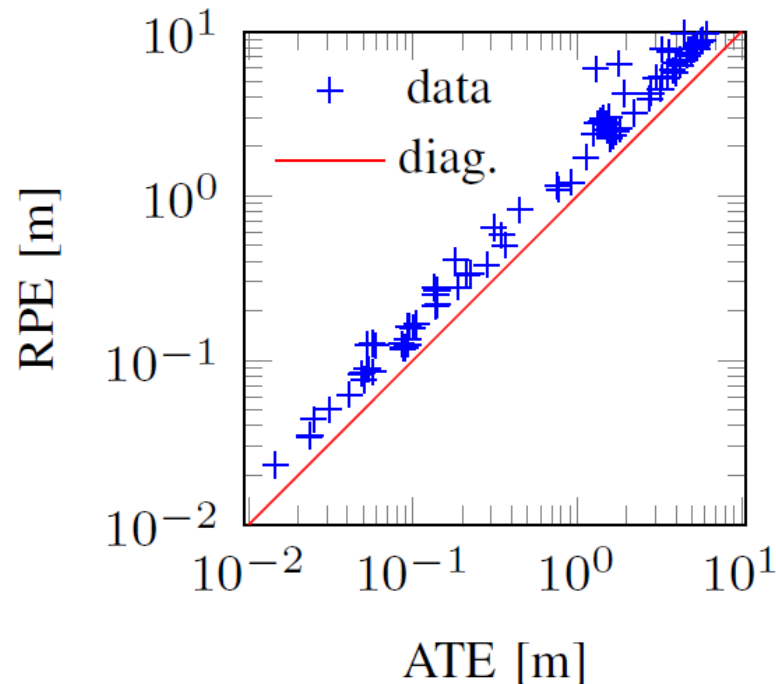
- Average over all time steps

$$\text{RMSE}(E_{1:n}) := \left( \frac{1}{m} \sum_{i=1}^m \| \text{trans}(E_i) \|^2 \right)^{1/2}$$

- Evaluation scripts for both evaluation metrics available (Python)
- Output: RMSE, median, mean
- Plot to png/pdf (optional)

# Comparison of RPE and ATE

- RPE and ATE are strongly related
- RPE considers additionally rotational errors
- $RPE \geq ATE$



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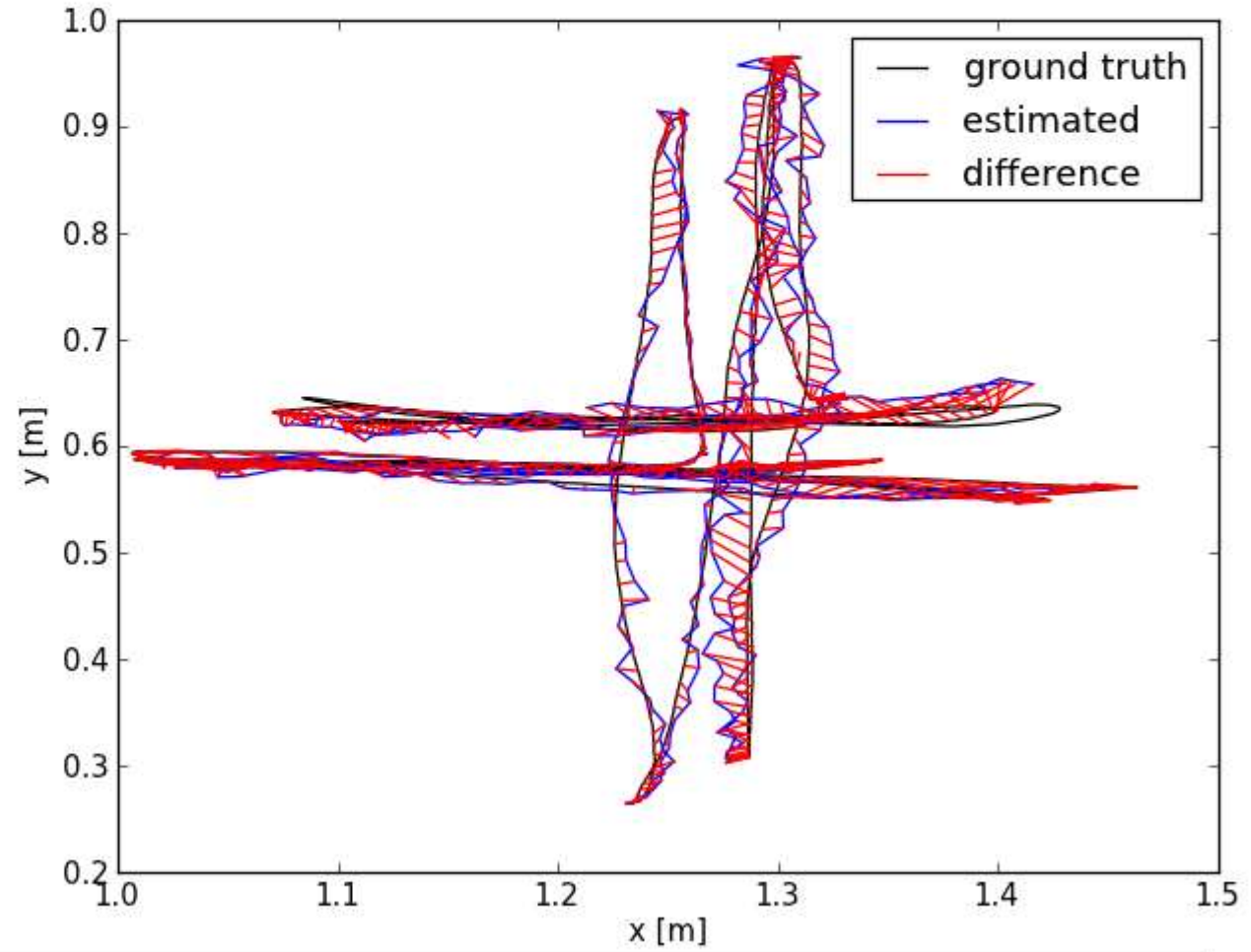
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## Submission form for automatic evaluation of RGB-D SLAM results

Groundtruth trajectory	freiburg1/xyz <input type="button" value="v"/>
Estimated trajectory	<input type="button" value="Datei auswählen"/> Keine ausgewählt
Evaluation options	Offset: <input type="text" value="0.00"/> seconds (add to stamps of estimated traj.) Scale: <input type="text" value="1.00"/> (scale estimated traj. by this factor)
Evaluation mode	<input checked="" type="radio"/> absolute trajectory error (recommended for the evaluation of visual SLAM methods) <input type="radio"/> relative pose error for pose pairs with a distance of <input type="text" value="1"/> <input type="button" value="second(s) v"/> (recommended for the evaluation of visual odometry methods) <input type="radio"/> relative pose error for all pairs (downsampled to <input type="text" value="10000"/> pairs)

*Runs the evaluation script on your data and displays the result. No data will be permanently saved on our servers. Alternatively, you can also download the [evaluation script](#) and perform the evaluation offline. Additional information about the [evaluation options](#) and the [file formats](#) is available. We also provide an [example trajectory](#) for freiburg1/xyz by [RGBD-SLAM](#) as well as instructions how to [reproduce](#) these trajectories.*

```
compared_pose_pairs 786 pairs  
absolute_translational_error.rmse 0.013473 m  
absolute_translational_error.mean 0.012029 m  
absolute_translational_error.median 0.011176 m  
absolute_translational_error.std 0.006068 m  
absolute_translational_error.min 0.000939 m  
absolute_translational_error.max 0.034727 m
```



# Summary – TUM RGB-D Benchmark

- Dataset for the evaluation of RGB-D SLAM systems
- Ground-truth camera poses
- Evaluation metrics + tools available
- Since August 2011:
  - >17.000 visitors
  - >4.500 online trajectory evaluations
  - >15 published research papers using the dataset
- Next steps:
  - Possibility to upload own trajectories/publications
  - Results page and automated ranking



# Conclusion

- Dense methods bear a large potential
  - Dense camera tracking
  - Dense 3D reconstruction
  - Open question: Estimate both at the same time?
- Benchmarks stimulate the comparison of alternative approaches
- Please contact us if you are interested in a collaboration!