Face recognition with wave kernel signatures using a depth camera

Matthäus Brandl

Computer Vision Group Department of Informatics Technische Universität München

September, 14th 2012

Introduction - Problem Definition

Face Recognition:

- identify a given face
- using a database of previously trained faces



Applications of Face Recognition:

- access control
- surveillance
- identification

Applications of Face Recognition:

- access control
- surveillance
- identification



Figure: Example of identification: easy tagging in iPhoto

Why use point images?

sensors became affordable

- sensors became affordable
- independent of illumination variations

- sensors became affordable
- independent of illumination variations
- higher security

- sensors became affordable
- independent of illumination variations
- higher security
- additional information

- sensors became affordable
- independent of illumination variations
- higher security
- additional information
- possibly higher recognition rates

Why use point images?

- sensors became affordable
- independent of illumination variations
- higher security
- additional information
- possibly higher recognition rates

Disadvantages:

• more sensitive to facial expression variations

Why use point images?

- sensors became affordable
- independent of illumination variations
- higher security
- additional information
- possibly higher recognition rates

Disadvantages:

- more sensitive to facial expression variations
- not available in many day-to-day situations

Motivation: just covered

Motivation: just covered

Approach:

- data acquirement
- face detection
- face normalization
- face recognition

Motivation: just covered

Approach:

- data acquirement
- face detection
- face normalization
- face recognition
 - calculation of the geometry descriptor
 - determination of points of interest
 - signature extraction at points of interest
 - \Rightarrow concise face description

Motivation: just covered

Approach:

- data acquirement
- face detection
- face normalization
- face recognition
 - calculation of the geometry descriptor
 - determination of points of interest
 - signature extraction at points of interest
 - \Rightarrow concise face description

Results

Motivation: just covered

Approach:

- data acquirement
- face detection
- face normalization
- face recognition
 - calculation of the geometry descriptor
 - determination of points of interest
 - signature extraction at points of interest
 - \Rightarrow concise face description

Results

Conclusion

Input:

- point image of a face
- face database

Input:

- point image of a face
- face database

Output:

Face Enrollment:

• database with added face

Input:

- point image of a face
- face database

Output:

Face Enrollment:

• database with added face

Face Recognition:

• identification of the face

Input:

- point image of a face
- face database

Output:

Face Enrollment:

• database with added face

Challenges:

- expression variations
- pose variations
- occlusions

Face Recognition:

identification of the face

Overview of the Approach



Figure: Data flow of our recognition approach

Data Acquisition - Overview





Data Acquisition - The Kinect depth camera



Data Acquisition - The Kinect depth camera



Working principle:

- disparity approach
- structured light is projected into environment
- depth is inferred from speckle deviation

Data Acquisition - The Kinect depth camera



Working principle:

- disparity approach
- structured light is projected into environment
- depth is inferred from speckle deviation



- array of width w and height h
- $\bullet\,$ each array element is a point in \mathbb{R}^3

- array of width w and height h
- $\bullet\,$ each array element is a point in \mathbb{R}^3
- all points are given in the same coordinate system

- array of width w and height h
- \bullet each array element is a point in \mathbb{R}^3
- all points are given in the same coordinate system
- not acquirable points are marked with a NaN vector

- array of width w and height h
- \bullet each array element is a point in \mathbb{R}^3
- all points are given in the same coordinate system
- not acquirable points are marked with a NaN vector

$$\Rightarrow \mathcal{I}_{P} \in \left(\mathbb{R}^{3} \cup \left(\perp \perp \perp\right)^{T}\right)^{w \times h}$$

Point Images - Examples





Face Detection - Overview



Face Detection - Background Removal



Figure: Segmented torso

Face Detection - Nose Detection

Nose Detection:

- nose tip candiates: locally convex
- Inner eye corner candidates: locally concave

Face Detection - Nose Detection

Nose Detection:

- nose tip candiates: locally convex
- Inner eye corner candidates: locally concave
- geometric candidate filtering scheme

Face Detection - Nose Detection

Nose Detection:

- nose tip candiates: locally convex
- Inner eye corner candidates: locally concave
- geometric candidate filtering scheme
- verification of remaining candidates using a model face
Face Detection - Nose Detection

Nose Detection:

- nose tip candiates: locally convex
- Inner eye corner candidates: locally concave
- geometric candidate filtering scheme
- verification of remaining candidates using a model face
- Schoose nose tip candidate with least error

Face Detection - Nose Detection

Nose Detection:

- nose tip candiates: locally convex
- Inner eye corner candidates: locally concave
- geometric candidate filtering scheme
- verification of remaining candidates using a model face
- Schoose nose tip candidate with least error
- unless it exceeds a threshold

Face Normalization - Overview



Face Normalization

Face Clipping:

• clip all points farther from the nose tip than a threshold

Pose Correction:

Smoothing:

Face Normalization

Face Clipping:

Pose Correction:

- translate nose tip to a defined position
- determine pose using the nose tip and the inner eye corners
- rotate the face into a defined configuration

Smoothing:

Face Normalization

Face Clipping:

Pose Correction:

Smoothing:

• apply a Binomial filter to smoothen the depth values

Face Recognition - Overview



Face Recognition - Geometry Descriptor



Basic idea:

- quantum particle on a surface \mathcal{X}
- Iocation is unknown
- approximate energy E is measured at time t = 0

Basic idea:

- quantum particle on a surface ${\mathcal X}$
- Iocation is unknown
- approximate energy E is measured at time t = 0

 \Rightarrow energy probability distribution $f_E^2(x, t)$

Energy probability distribution:

• governed by wave function $\psi(x, t)$

Energy probability distribution:

• governed by wave function $\psi(x, t)$

Wave function:

• solution to the Schrödinger equation $\frac{\partial \psi}{\partial t}(x, t) = i\Delta \psi(x, t)$, where Δ is the Laplace-Beltrami operator of surface \mathcal{X}

The Laplace-Beltrami operator can be decomposed into:

- eigenfunctions ϕ_k
- "eigenenergies" E_k

The Laplace-Beltrami operator can be decomposed into:

- eigenfunctions ϕ_k
- "eigenenergies" E_k

Using them the wave function can be given as:

$$\psi_{E}(x,t) = \sum_{k=0}^{\infty} \exp(iE_{k}t) \phi_{k}(x) f_{E}(E_{k})$$

The WKS is introduced as:

WKS
$$(E, x) = \lim_{T \to \infty} \frac{1}{T} \int_0^T |\psi_E(x, t)|^2 dt$$

WKS(E, x) is

- over time average probability
- to measure the quantum particle
- with initial energy E
- at point $x \in \mathcal{X}$ on the surface

Definition (Wave Kernel Signature)

The WKS for a point $x \in \mathcal{X}$ and initial energy E is given as

WKS
$$(E, x) := \sum_{k=0}^{\infty} \phi_k (x)^2 f_E (E_k)^2$$

where f_E is the energy probability distribution for the initial energy E.

Wave Kernel Signature - Example



Finite approximation L of Laplace-Beltrami operator Δ is needed

Finite approximation L of Laplace-Beltrami operator Δ is needed

Idea:

- convert point image into a graph
- use weighted Graph Laplacian as approximation

Finite approximation L of Laplace-Beltrami operator Δ is needed

Idea:

- convert point image into a graph
- use weighted Graph Laplacian as approximation

Pro:

- easy to understand
- straightforward to implement

Finite approximation L of Laplace-Beltrami operator Δ is needed

Idea:

- convert point image into a graph
- use weighted Graph Laplacian as approximation

Pro:

- easy to understand
- straightforward to implement

Contra:

• does not converge to Δ for increasingly finer discretizations

Implementation - Conversion into a Graph

create a graph vertex for every element of the point image

Implementation - Conversion into a Graph

- create a graph vertex for every element of the point image
- add edges between each vertex and the vertices of its 8-connected-neighborhood



Implementation - Conversion into a Graph

- create a graph vertex for every element of the point image
- add edges between each vertex and the vertices of its 8-connected-neighborhood
- add edge weights depending on the vertex distances

$$w_{ij} = \exp\left(-rac{\|v_i - v_j\|^2}{t}
ight)$$

Implementation - Weighted Graph Laplacian

Definition (Adjacency Matrix)
$$A(i,j) = \begin{cases} w_{ij} = \exp\left(-\frac{\|v_i - v_j\|^2}{t}\right), & if \{v_i, v_j\} \in E\\ 0, & else \end{cases}$$

Implementation - Weighted Graph Laplacian

Definition (Adjacency Matrix) $A(i,j) = \begin{cases} w_{ij} = \exp\left(-\frac{\|v_i - v_j\|^2}{t}\right), & \text{if } \{v_i, v_j\} \in E\\ 0, & else \end{cases}$ Definition (Degree Matrix)

$$D(i,j) = \begin{cases} \sum_{k=1}^{n} A(i,k), & \text{if } i = j \\ 0, & \text{else} \end{cases}$$

Implementation - Weighted Graph Laplacian

Definition (Adjacency Matrix) $A(i,j) = \begin{cases} w_{ij} = \exp\left(-\frac{\|v_i - v_j\|^2}{t}\right), & \text{if } \{v_i, v_j\} \in E\\ 0, & else \end{cases}$

Definition (Degree Matrix)

$$D(i,j) = \begin{cases} \sum_{k=1}^{n} A(i,k), & \text{if } i = j \\ 0, & \text{else} \end{cases}$$

Definition (Graph Laplacian)

$$L = D - A$$

Laplacian Eigenfunctions



Figure: Corresponding eigenfunctions of the 8 least non-zero eigenenergies

Wave Kernel Signature - Examples



Figure: Signature distance of several points

Face Recognition - Face Graph



Face Graph - Model



Imatch vertices to a new face using ICP

- Imatch vertices to a new face using ICP
- Ø determine nearest neighbor of every model graph vertex

- Imatch vertices to a new face using ICP
- Ø determine nearest neighbor of every model graph vertex
- I make them the corresponding vertices of the new graph

- Imatch vertices to a new face using ICP
- Ø determine nearest neighbor of every model graph vertex
- Imake them the corresponding vertices of the new graph
- Onnect the new vertices as the model graph vertices

- Imatch vertices to a new face using ICP
- Ø determine nearest neighbor of every model graph vertex
- Imake them the corresponding vertices of the new graph
- connect the new vertices as the model graph vertices
- Imanual graph correction


 ${\small \textcircled{0}} \quad \text{extract the WKS at every graph vertex}$

 \Rightarrow concise face description

34 / 39

extract the WKS at every graph vertex ⇒ concise face description

enrollment: store the signatures in a database

● extract the WKS at every graph vertex
 ⇒ concise face description

• recognition: compare the signatures with those in the database

- extract the WKS at every graph vertex
 ⇒ concise face description
- recognition: compare the signatures with those in the database
- select the entry with the least signature distance

$$d_{\mathsf{WKS}}(x,x')^{2} = \int_{e_{min}}^{e_{max}} (\mathsf{WKS}(x,e) - \mathsf{WKS}(x',e))^{2} de$$

Face Recognition - Experimental Setup

- we recorded point images of 54 persons, a total of 2061 images
- one image per person used for training
- three images per person used for testing
 - \Rightarrow total of 157 recognition runs

Face Recognition - Experimental Results

Rank 1 recognition rate:	94	out of	157	59.9%
Rank 3 recognition rate:	114	out of	157	72.6%
Rank 6 recognition rate:	130	out of	157	82.8%

Table: Overall recognition rates

Face Recognition - Experimental Results

Rank 1 recognition rate:	94	out of	157	59.9%
Rank 3 recognition rate:	114	out of	157	72.6%
Rank 6 recognition rate:	130	out of	157	82.8%

Table: Overall recognition rates

Compilation of the graph Laplacian:		seconds	30.0%
Eigendecomposition of the graph Laplacian:	6.19	seconds	66.6%
Calculation of the WKS:	0.24	seconds	1.0%
Transformation into the SIWKS:	0.15	seconds	1.6%
Recognition:	0.07	seconds	0.8%
Total	9.29	seconds	

Table: Run-times

- recognition rate of 59.9%
- by a factor of 30 above the expected value of random choice (=1.9%)

- recognition rate of 59.9%
- by a factor of 30 above the expected value of random choice (=1.9%)
- neutral and non-neutral expressions are recognized with equal rates
 ⇒ WKS is well suited to handle expression variations

- recognition rate of 59.9%
- by a factor of 30 above the expected value of random choice (=1.9%)
- neutral and non-neutral expressions are recognized with equal rates
 ⇒ WKS is well suited to handle expression variations
- method is stable under mild occlusions and mild pose variations

- recognition rate of 59.9%
- by a factor of 30 above the expected value of random choice (=1.9%)
- neutral and non-neutral expressions are recognized with equal rates
 ⇒ WKS is well suited to handle expression variations
- method is stable under mild occlusions and mild pose variations
- scales very good with database size theoretical runtime for 1000 DB entries is 1.4 seconds

Conclusions - Future Work

Possible Future Work:

• replace graph Laplacian with Point Cloud Data Laplacian

Conclusions - Future Work

Possible Future Work:

- replace graph Laplacian with Point Cloud Data Laplacian
- improve model graph matching

Possible Future Work:

- replace graph Laplacian with *Point Cloud Data Laplacian*
- improve model graph matching
- weighted signature distance

Questions?

Thank you for your attention

Any questions?