



## Part II: Practical Exercises

This exercise is to be solved **during the tutorial**.

1. Download the package `mvg_exerciseSheet_02.zip` and use `openOFF.m` to load the 3D model `model.off`.
2. (a) Write a function that rotates the model around its center (i.e. the mean of its vertices) for given rotation angles  $\alpha$ ,  $\beta$  and  $\gamma$  around the  $x$ -,  $y$ - and  $z$ -axis. Use homogeneous coordinates and describe the overall transformation by a single matrix. The rotation matrices around the respective axes are as follows:

$$\begin{array}{ccc} \text{rotation matrix (x-axis)} & \text{rotation matrix (y-axis)} & \text{rotation matrix (z-axis)} \\ \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{pmatrix} & \begin{pmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{pmatrix} & \begin{pmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{pmatrix} \end{array}$$

- (b) Rotate the model first 5 degrees around the  $x$ -axis and then 25 degrees around the  $z$ -axis. Now start again by doing the same rotation around the  $z$ -axis first followed by the  $x$ -axis rotation. What do you observe?
  - (c) Perform a translation in addition to the rotation. Find a suitable matrix from  $SE(3)$  for this purpose and add it to your function from 2. Translate the model by the vector  $(0.5 \ 0.2 \ 0.1)^\top$ .
3. (a) Write a function which takes a vector  $w \in \mathbb{R}^3$  as input and returns its corresponding element  $R = e^{\hat{w}} \in SO(3) \subset \mathbb{R}^{3 \times 3}$  from the Lie group. Hence, the function will be a concatenation of the hat operator  $\hat{\cdot}: \mathbb{R}^3 \rightarrow so(3)$  and the exponential mapping.
  - (b) Implement another function which performs the corresponding inverse transformation and test the two functions on some examples.
  - (c) Implement similar functions which calculate the transformation for twists. I.e. from  $\xi \in \mathbb{R}^6$  to  $e^{\hat{\xi}} \in SE(3) \subset \mathbb{R}^{4 \times 4}$  and the other way around.
  - (d) How can you use Matlab's built-in functions `expm` and `logm` to achieve the same functionality (your solutions to (a)-(c) should *not* use these functions)?

### Matlab-Tutorials:

<http://www.math.utah.edu/lab/ms/matlab/matlab.html>

<http://www.math.ufl.edu/help/matlab-tutorial/>