

Note that MAP inference can be efficiently done by making use of *Max-sum* algorithm.





Optimization
Lagrange multiplies !

$$m_m \in (-\infty, m_m) = (-\infty$$

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sum over q_i . This convolution can be efficiently calculated in $\mathcal{O}(|\mathcal{V}|)$ time (instead of $\mathcal{O}(|\mathcal{V}|^2)$). IN2329 - Probabilistic Graphical Models in Computer Vision 9. Human pose estimation & Mean field approximation - 31

Source: Chen et al... Semantic Image Segmentation with Deep Convolutional Nets and Fully Connected CRFs. ICLR, 2015.

Summary *

Mean field approximation: instead of an *intractable* distribution $p(\mathbf{y} | \mathbf{x})$, we consider an *approximate distribution* $q(\mathbf{y})$, which minimizes the KL divergence.

In case of *naïve mean field approximation* $q(\mathbf{y})$ is defined as

$$q(\mathbf{y}) = \prod_{i \in \mathcal{V}} q_i(y_i) \; ,$$

which is tractable.

A local optimal solution can be obtained by applying the update equation:

$$q_i^*(y_i) = \frac{1}{Z_i(\mathbf{x}_F)} \exp\left(-\sum_{\substack{F \in \mathcal{M}(i) \ \mathbf{y}'_F \in \mathcal{Y}_F, \\ y'_i = y_i}} \sum_{\substack{j \in N(F) \setminus \{i\} \\ y'_i = y_i}} \left(\prod_{j \in N(F) \setminus \{i\}} q_j(y_j)\right) E_F(\mathbf{y}_F; \mathbf{x}_F)\right).$$

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Literature *

Human pose estimation

1.1

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Mean field approximation

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Next lecture *



In the next lecture we will learn about

- Sampling of a distribution $(p(\mathbf{y} \mid \mathbf{x}))$ via *Gibbs sampling*.
- Parameter learning Consider an energy function for a parameter vector $\mathbf{w} = [w_1, w_2]^T$:

$$E(\mathbf{y}; \mathbf{x}, \mathbf{w}) = w_1 \sum_{i \in \mathcal{V}} E_i(y_i; x_i) + w_2 \sum_{(i,j) \in \mathcal{E}} E_{ij}(y_i, y_j)$$

We aim to estimate optimal parameter vector \mathbf{w} consisting of (positive) weighting factors (like $w_1, w_2 \in \mathbb{R}^+$) for $E(\mathbf{y}; \mathbf{x}, \mathbf{w})$.