Probabilistic Graphical Models in Computer Vision

Lecture: Dr. Tao Wu Exercises: Yuesong Shen, Zhenzhang Ye

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Weekly Exercises 2

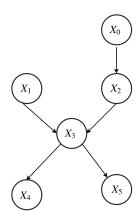
Room: 02.09.023 Wednesday, 22.05.2019, 12:15 - 14:00

Bayesian Network

(12+6 Points)

Exercise 1 (4 Points). Given two Bernoulli random variable X and Y, (i.e. check Tao's slides). Show that if X=0 is independent to Y=0, we have X and Y are independent.

Exercise 2 (4 Points). Given following Bayesian network:



- 1. Give the factorization of $p(x_0, x_1, x_2, x_3, x_4, x_5)$.
- 2. Assume the observation is $\{X_4\}$, give reachable nodes of $\{X_0\}$ via active trail.
- 3. Assume the observation is $\{X_0\}$, give reachable nodes of $\{X_2\}$ via active trail.

Exercise 3 (4 Points). Given three boolean random variables X, Y and Z (i.e. each can only be true or false), is it possible to find a perfect map for following distribution:

$$p(x, y, z) = \begin{cases} \frac{1}{12} & x \oplus y \oplus z = \text{false} \\ \frac{1}{6} & x \oplus y \oplus z = \text{true} \end{cases}$$
 (1)

where \oplus is the XOR function. Explain why or draw the corresponding perct map.

Exercise 4 (6 Points). For a directed graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$, assume that the max indegree is 2 (*i.e.* any node has maximum 2 parents). Given an observation set Z and a random variable Y, figure out an algorithm to find the reachable nodes of Y via active trail in this graph.

Hint: First of all, assume there is no v-structure in the graph, what should we do? Then include the v-structure, what kind of preprocessing do we have to do?

Programming (Due:27.05)

(12Points)

Exercise 5. In this programming exericse, you are asked to implement an algorithm to find reachable nodes via active trail in a directed graph. See the ipython file for more details.