



Multiple View Geometry: Exercise Sheet 9

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Wednesdays 16:15–18:15 at Hörsaal 2, "Interims I"
(5620.01.102), and on RBG Live

Exercise: July 2nd, 2025

This exercise partly builds upon the theory part of last week's exercise. Check the solutions of Sheet 8 in case there is something you do not understand.

1. Robust Least Squares

In order to make the solution of the Direct Image Alignment from Sheet 8 more robust to outliers, one can replace the square in the energy

$$E(\xi) = \sum_i r_i(\xi)^2$$

by a robust loss function ρ :

$$E_\rho(\xi) = \sum_i \rho(r_i(\xi)).$$

(a) What situations can you think of where a robust loss function might be needed?

The minimizer of E_ρ also minimizes the weighted least squares problem

$$E_w(\xi) = \sum_i w(r_i) r_i(\xi)^2$$

with weights defined by $w(t) := \rho'(t)/t$.

(b) One example for a robust loss function is the Huber loss function ρ_δ :

$$\rho_\delta(t) = \begin{cases} \frac{t^2}{2} & |t| \leq \delta \\ \delta|t| - \frac{\delta^2}{2} & \text{else} \end{cases}$$

Write down the weight function for the Huber loss.

2. Optimization Techniques

Define \mathbf{r} as the vector containing the residuals and J as the matrix containing gradients of all residuals at $\xi = \mathbf{0}$:

$$\mathbf{r}_i = r_i(\mathbf{0}) , \quad J^{(i)} = \left. \frac{\partial r_i(\xi)}{\partial \xi} \right|_{\xi=\mathbf{0}} .$$

Furthermore, let W be the diagonal matrix with weights $w(r_i(\mathbf{0}))$ on the diagonal. Write down the update step $\Delta\xi$ for each of the following minimization methods:

- (a) Gradient descent, normal least squares,
- (b) Gradient descent, weighted least squares,
- (c) Gauss-Newton, normal least squares,
- (d) Gauss-Newton, weighted least squares,
- (e) Levenberg-Marquardt, normal least squares, and
- (f) Levenberg-Marquardt, weighted least squares.