



Multiple View Geometry: Solution Sheet 7

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Wednesdays 16:15–18:15 at Hörsaal 2, "Interims I"
(5620.01.102), and on [RBG Live](#)

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$$1. \exists \lambda \in \mathbb{R} : [R', T'] = \lambda [R, T] H = \lambda [R, T] \begin{bmatrix} I & 0 \\ v^\top & v_4 \end{bmatrix} = \lambda [R + Tv^\top, Tv_4]$$

$$\begin{aligned} E' &= \hat{T}' R' \\ &= (\widehat{\lambda v_4 \hat{T}}) \cdot (\lambda (R + Tv^\top)) \\ &= \lambda^2 v_4 \hat{T} (R + Tv^\top) \\ &= \lambda^2 v_4 \hat{T} R + \lambda^2 v_4 \underbrace{\hat{T} T}_{=0} v^\top \\ &= \lambda^2 v_4 \hat{T} R \\ &= \lambda^2 v_4 E \quad \text{with } \lambda^2 v_4 \in \mathbb{R} \end{aligned}$$

$$\Rightarrow E' \sim E$$

2. (a) l is in the coimage of L , and therefore l is a normal vector to the plane that is determined by the camera position and L .

$$\begin{aligned} \Rightarrow l^\top x_1 &= 0 \\ l^\top x_2 &= 0. \end{aligned}$$

$$\Rightarrow l \sim x_1 \times x_2 = \hat{x}_1 x_2.$$

l_1 and l_2 are normal vectors to the planes through camera position and L_1, L_2 respectively.

$$\begin{aligned} \Rightarrow l_1^\top x &= 0 \\ l_2^\top x &= 0 \end{aligned}$$

$$\Rightarrow x \sim l_1 \times l_2 = \hat{l}_1 l_2.$$

- (b) i. $l_1 \sim \hat{x}u$:
 x is in the preimage of L_1 . $\Rightarrow l_1^\top x = 0$.
 $\exists$ point $u \neq p$ in L_1 . $\Rightarrow l_1^\top u = 0$
 $\Rightarrow l_1 \sim \hat{x}u$.
 ii. $l_2 \sim \hat{x}v$: analog to i.
 iii. $x_1 \sim \hat{l}r$:
 x_1 is in the preimage of L . $\Rightarrow x_1^\top l = 0$
 $\exists$ a line L' through p_1 with coimage $r \neq l$. $\Rightarrow x_1^\top r = 0$.
 $\Rightarrow x_1 \sim \hat{l}r$.
 iv. $x_2 \sim \hat{l}s$: analog to iii.

$$3. \quad \text{rank} \begin{pmatrix} \hat{x}_1 \Pi_1 \\ \hat{x}_2 \Pi_2 \end{pmatrix} \leq 3$$

$$\Rightarrow \exists X \in \mathbb{R}^4 \setminus \{0\} \text{ with } \begin{pmatrix} \hat{x}_1 \Pi_1 \\ \hat{x}_2 \Pi_2 \end{pmatrix} X = 0.$$

$$\Rightarrow \hat{x}_1 \Pi_1 X = 0 \quad \wedge \quad \hat{x}_2 \Pi_2 X = 0,$$

$$\Rightarrow x_1 \times \Pi_1 X = 0 \quad \wedge \quad x_2 \times \Pi_2 X = 0.$$

$$\Rightarrow x_1 \text{ and } \Pi_1 X \text{ are linearly dependent; and } x_2 \text{ and } \Pi_2 X \text{ are linearly dependent.}$$

$$\Rightarrow \exists \lambda_1, \lambda_2 \in \mathbb{R} \text{ with } \Pi_1 X = \lambda_1 x_1 \quad \wedge \quad \Pi_2 X = \lambda_2 x_2$$

$$\Rightarrow x_1 \text{ and } x_2 \text{ are projections of } X.$$