Image Segmentation I

Image Segmentation

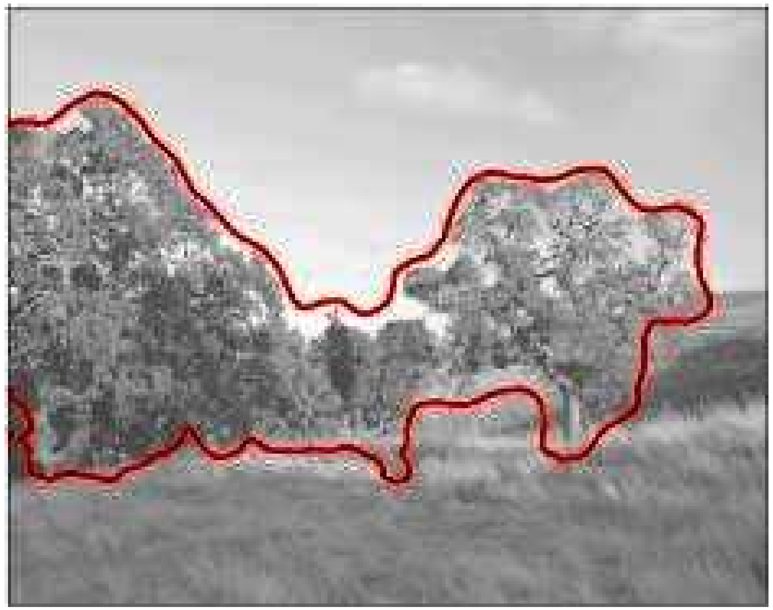
- The goal of image segmentation (Bildsegmentierung) is to partition the image plane into “meaningful” components.
- What is meaningful depends on the application. Typically one may want a segmentation where each region corresponds to a separate object or structure in the scene. As a consequence, image segmentation is tightly coupled with figure-ground discrimination, image interpretation and semantic analysis.
- Image segmentation is the most studied problem in image processing.
- There exist many approaches. They typically differ in:
    - which local properties are used in the process (brightness, color, texture, motion,...).
    - how the partitioning is computed (examples: region merging, region growing, watershed, graph cuts, level sets, convex relaxation techniques,...).

A Difficult Problem

Segmentation: Brightness

D. Mumford, J. Shah ’89, T. Chan, L. Vese, TIP ’01

Segmentation: Texture



M. Heiler, C. Schnörr, IJCV ’05

T. Brox, J. Weickert, ECCV ’04

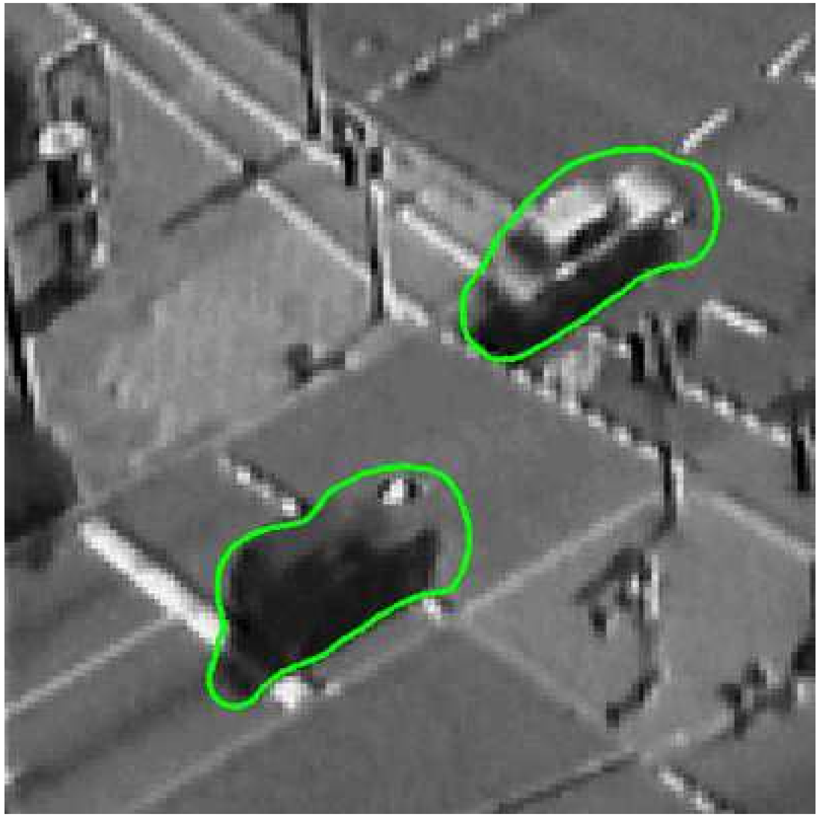
Segmentation: Color

Input | Segmented image | Segmentation

Input | Segmented image | Segmentation

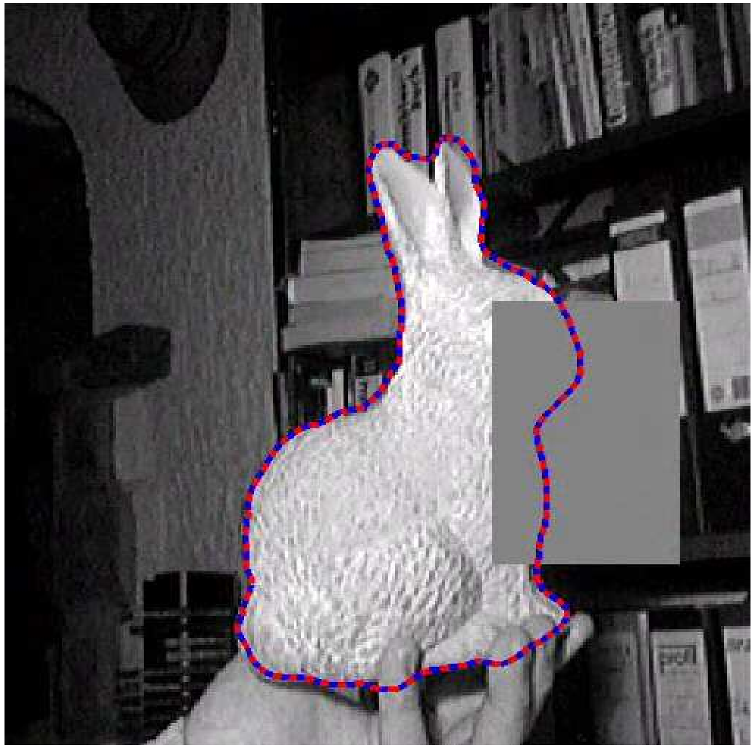
J. Keuchel, C. Schnörr, C. Schellewald, D. Cremers, *Semidefinite Programming*, IEEE PAMI 2003.

Segmentation: Motion

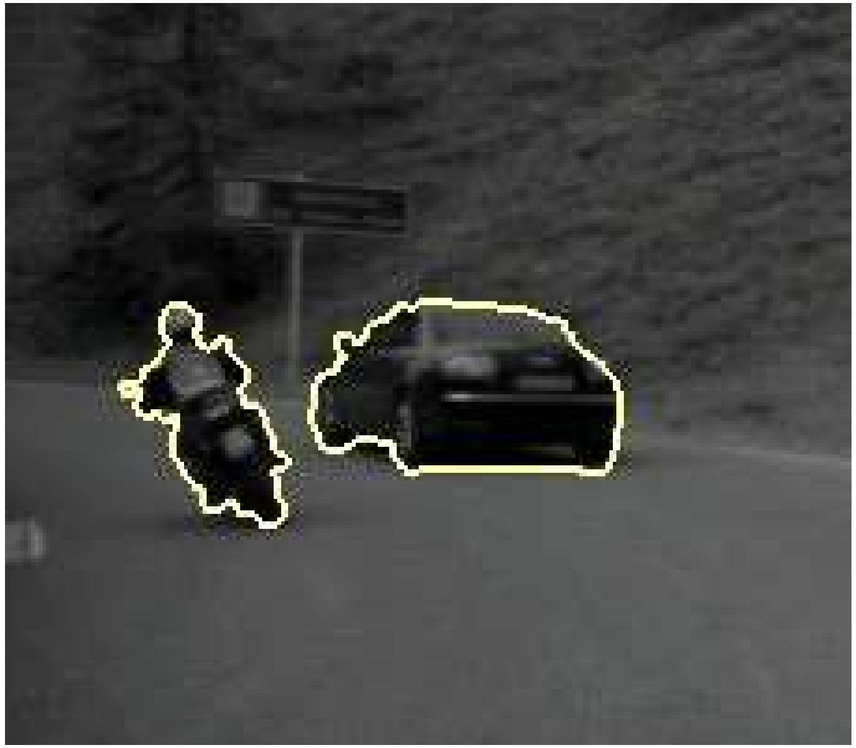


D. Cremers, S. Soatto, *Motion Competition*, IJCV 2005.

Segmentation: Brightness and Shape



Cremers et al., ECCV ’02



Schoenemann, Cremers, PAMI ’09

Basic Concepts in Image Segmentation

- Segmentation methods are generally based on two complementary concepts:
  - Edge-based methods identify contours which approximate discontinuities of the color or texture. Whereas traditional methods heuristically group the output of edge detectors into connected curves, in recent years respective boundaries are computed by energy minimization.
  - Region-based methods identify regions in the image plane for which some criterion is more or less uniform (brightness, color, textures,...). Among these methods are the simple thresholding, region growing, region merging, but also a number of energy minimization methods.
- Although all segmentation methods expoit discontinuities or similarity, they are based on fundamentally different representations of the solution (discrete vs. continuous, explicit vs. implicit) and on fundamentally different numerical solutions (PDEs, maximum-flow algorithms, stochastic sampling,...).

Segmentation in 8 Steps

To compute a segmentation based on edge detector output, researchers have proposed a variety of methods.
For example the following:

1. Identify edges by thresholding the gradient norm,
2. thinnen regions ($\rightarrow$ 1-dim. structures),
3. expand contour pieces ($\rightarrow$ close gaps),
4. identify connected components,
5. eliminate smaller regions,
6. thinnen regions (again),
7. introduce new boundary pixels ($\rightarrow$ close gaps),
8. eliminate smaller regions.

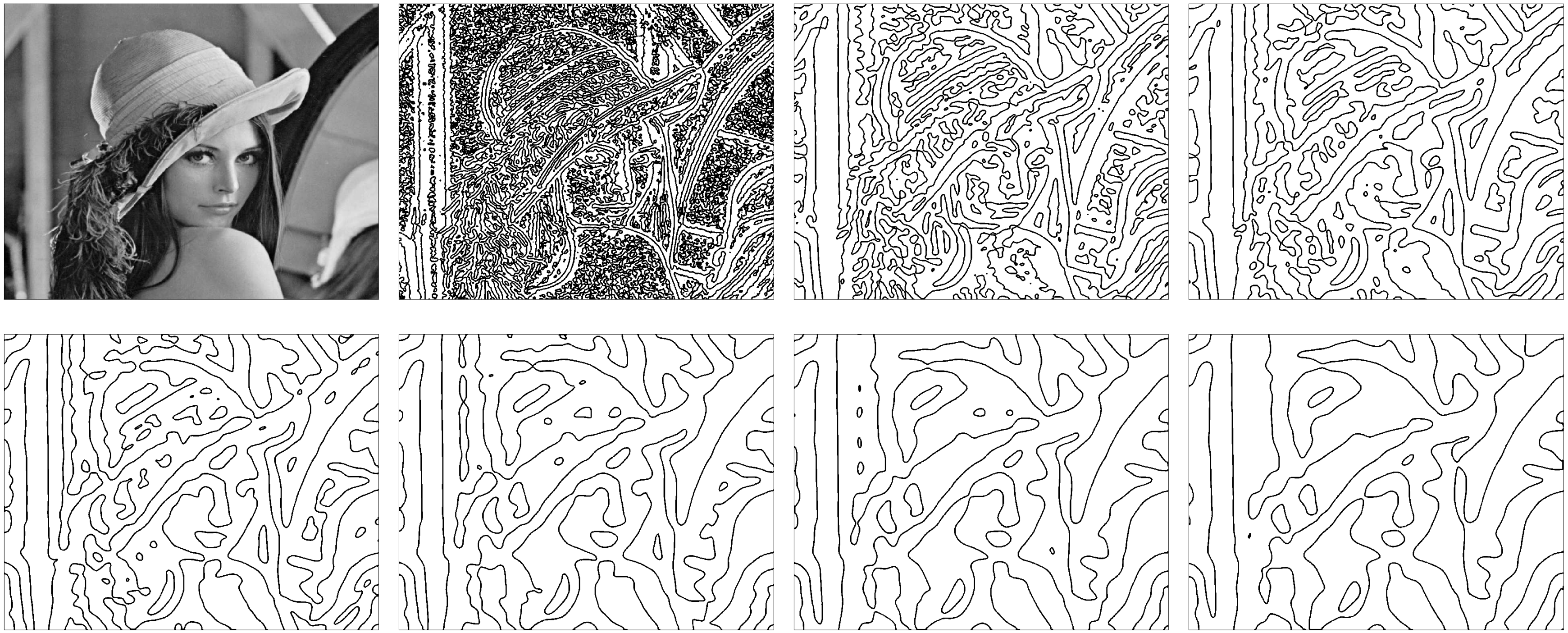
W. A. Perkins, IEEE Trans. on Patt. Anal. and Mach. Intell. 1980

Laplace Zero Crossings

- A simple strategy which automatically generates closed curves is to detect the zero crossings of the Laplacian of an input image $f(x, y)$:

$$\Delta(G_\sigma * f) = 0.$$

where G_σ denotes Gaussian smoothing of width σ.



Laplace zero-crossing for increasing σ (Author: D. Cremers)

Thresholding

- The simplest method to compute segmentations is to threshold the input image $f : \Omega \to \mathbb{R}$:

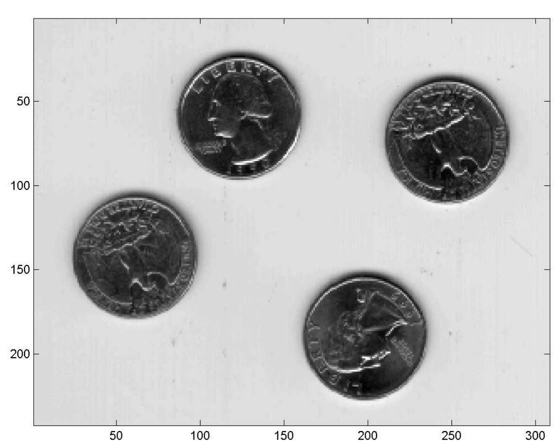
$$g(x) = \begin{cases} 1, & f(x) > \theta \\ 0, & \text{sonst} \end{cases} .$$

- The threshold $\theta \in \mathbb{R}$ must be chosen "appropriately".
- For many images one can automatically determine appropriate thresholds by selecting minima of the smoothed histogram of brightness values.
- N. Otsu proposed to select the threshold such that the brightness variance of object and background are minimized:

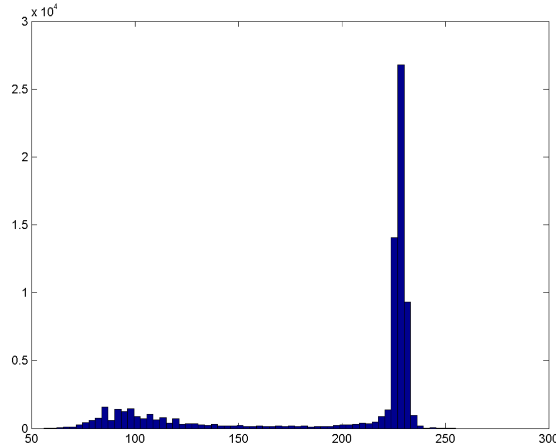
  N. Otsu, *A Threshold Selection Method from Gray-Level Histograms*, IEEE Transactions on Systems, Man, and Cybernetics, vol. 9, no. 1, pp. 62-66, 1979.

  Matlab: `level=graythresh(I);`

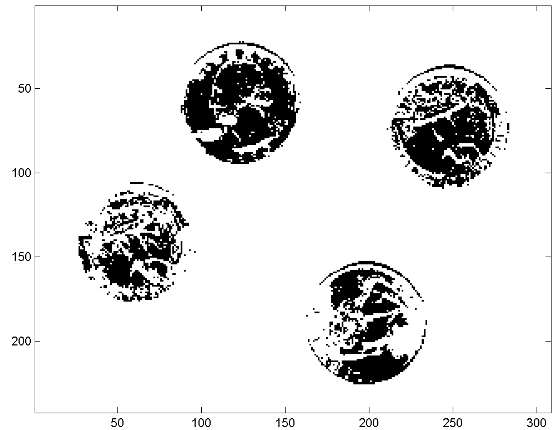
Thresholding



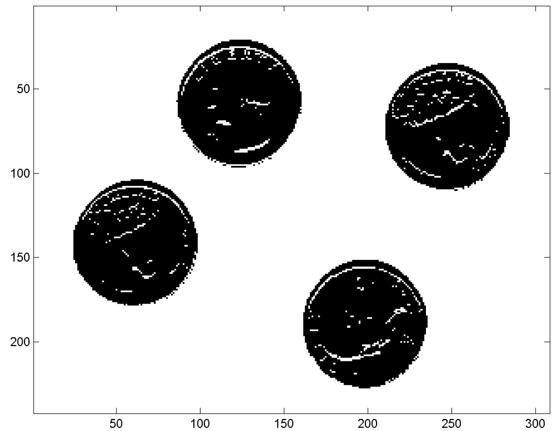
Input image



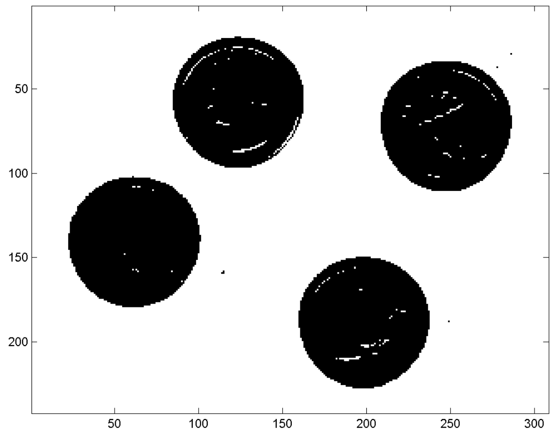
histogram



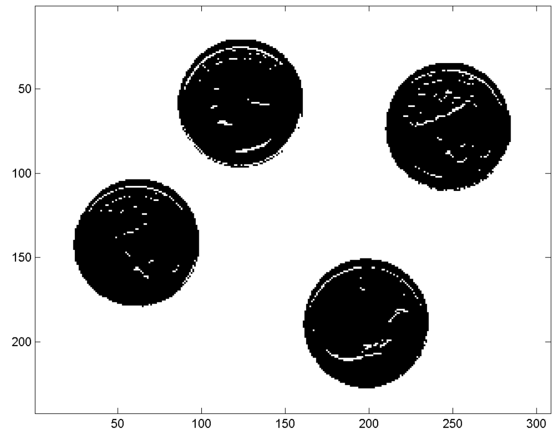
$\theta = 100$



$\theta = 150$



$\theta = 200$



Otsu: $\theta = 165.5$

Author: D. Cremers

Alternative Methods

There exists a number of adaptive thresholding techniques:

- Chose θ as the minimum of the (smoothed) histogram.
- Otsu: θ by minimizing brightness variance.
- Set $\theta = $ average brightness.
- Spatially adaptive: $\theta = $ average brightness in the vicinity.
- Clustering: Determine mean intensity of inside (μ_1) and outside (μ_2):

$$\theta = \frac{\mu_1 + \mu_2}{2}$$

  recompute segmentation and iterate.
- Double thresholding: For two threshold values $\theta_1 < \theta_2$ determine:
  1. all pixels i, for which $f_i > \theta_2$.
  2. all pixels j with $f_j > \theta_1$, which are connected with a pixel i (for which $f_i > \theta_2$).

Thresholding: Advantages and Drawbacks

Advantages:

- Very fast to compute.
- Adaptive variants allow to
  1. adapt to brightness distribution of the image,
  2. take into account brightness variance in the separated regions.

Drawbacks of thresholding:

- Thresholding methods neglect spatial context, for example the information that neighboring pixels are likely to be part of the same region. Instead all pixels are treated independently.
- A systematic (and mathematically more transparent) generalization of adaptive thresholding methods is given by clustering methods.

Segmentation by Color Clustering

- Idea: Compute segementations of an image by combining pixels of “similar” color in a single region.
- Consider the colors of all pixels as samples in the rgb color space $\mathbb{R}^3$ and apply a clustering algorithm.
- There exist many possible clustering algorithms (see for example the Matlab help menue).
- Among the best known methods is k-means clustering. This method determines a given number of k clusters by iteratively assigning data points to the nearest of k cluster centers and subsequently recomputing these cluster centers.
- An extension of this amounts to fitting each cluster with a multivariate Gaussian distribution (i.e. an ellipsoid), thereby allowing adaptive stretching (in color space).

Segmentation with k-means Clustering

Input

Otsu threshold

2 clusters

5 clusters

5 cluster reconstr.

10 cluster reconstr.

Author: D. Cremers

The last two images are obtained by coloring each region with the color of its cluster center (its average color).

Region-based Segmentation

- Region-based segmentation methods are related to thresholding and clustering methods. In addition, they consider (explicitly or implicitly) spatial context.
- The central idea is as follows: Determine a partitioning of the image plane $\Omega \subset \mathbb{R}^2$ into n pairwise disjoint, regions $\{\Omega_1, \dots, \Omega_n\}$:

  (i) $\bigcup_{i=1}^{n} \Omega_i = \Omega$,

  (ii) $\Omega_i \cap \Omega_j = \emptyset$, if $i \neq j$.

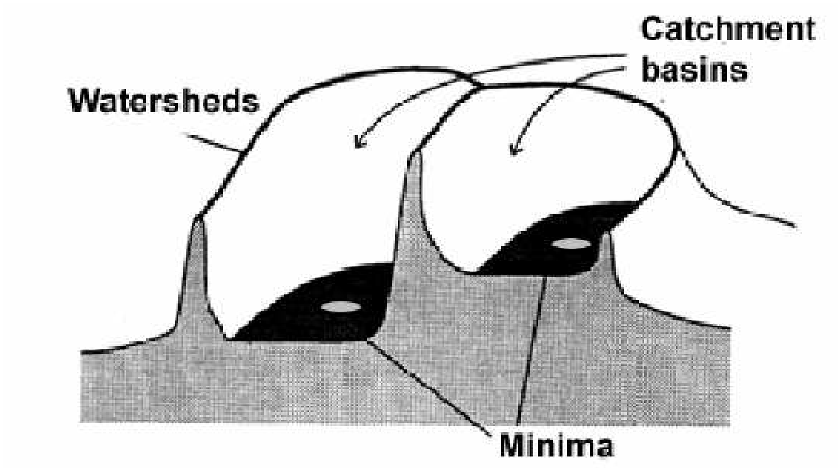
  (iii) $P(\Omega_i) =$ TRUE $\forall i$, $\quad P(\Omega_i \cup \Omega_j) =$ FALSE $\forall i \neq j$.
- In addition, one typically assumes that neighboring pixels are preferably part of the same region (spatial context).
- Condition (iii) states that region Ω_i should be homogeneous with respect to some property P. Two different regions, on the other hand, should not be.

Regiongrowing and Regionmerging

- Two rather old methods for computing region-based segmentations are region growing and region merging.
- Region Growing (Adams & Bischof, PAMI ’94):
  1. Select a seed pixel.
  2. Iteratively include neighboring pixels as long as their color is sufficiently similar.
- Region Merging (Brice, Fennema 1970, Koepfler et al. ’95):
  1. Start with a partitioning for which each pixel is its own region.
  2. Iteratively merge neighboring regions as long as they are sufficiently similar.
- Advantages: interactive, always determines connected regions.
- Drawbacks: Threshold values (“sufficiently similar”) needed, typically lack a systematic optimization criterion.

The Watershed Transform

- An (edge-based) segmentation can be computed using the watershed transform (Wasserscheidentransformation).



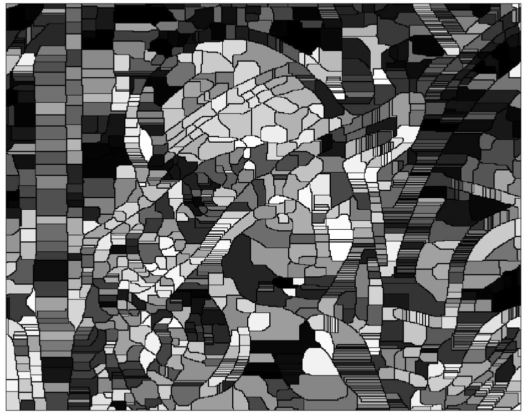
(Bild: P. Soille 1998)

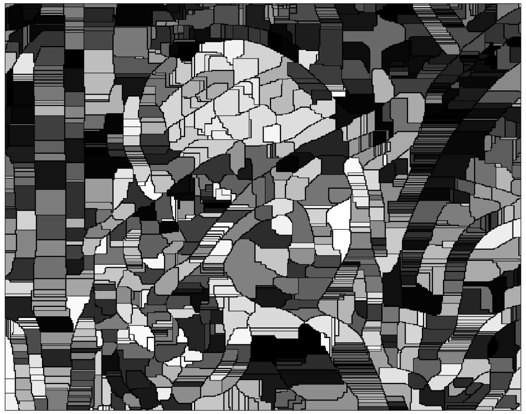
- Intuition:
  - Interpret the gradient of the smoothed image $|\nabla f_\sigma(x)| \equiv |\nabla G_\sigma * f|$ as a height profile.
  - For each point let water drops go down-hill until they fill a bassin (steepest descent).
  - Alll points going to the same bassin form a connected region (linear complexity).

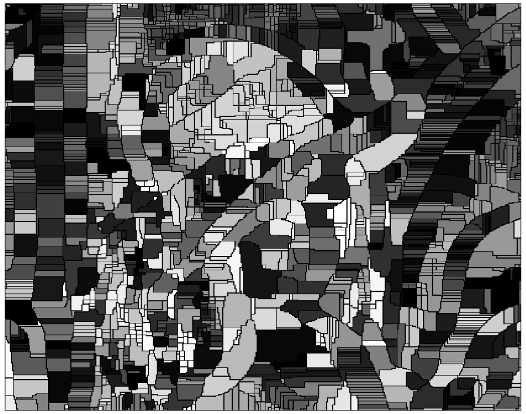
The Watershed Transform


Input


$\sigma = 2.5$


$\sigma = 5$


$\sigma = 7$


$\sigma = 10$


$\sigma = 10$ Reconstr.

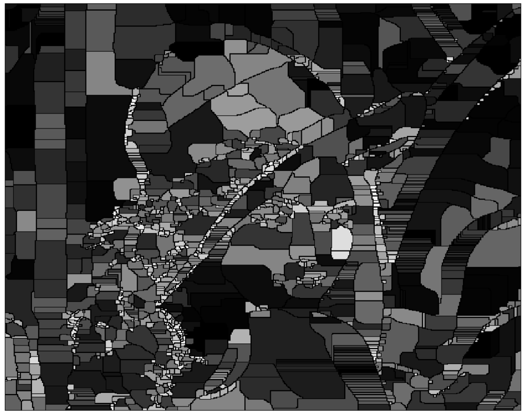
Author: D. Cremers

The last image is obtained by coloring respective regions with their average color value.

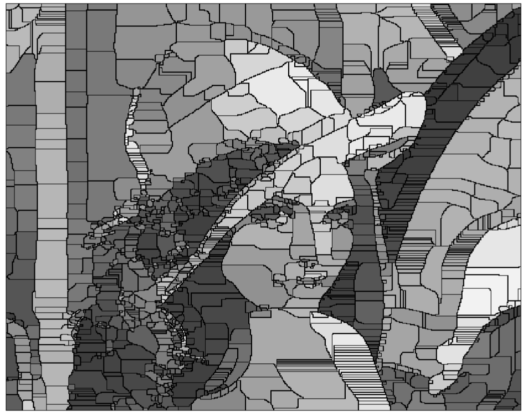
Watershed with Nonlinear Diffusion

One drawback of the watershed transform is that it typically leads to an oversegmentation (too many small regions). On the other hand, a simple presmoothing delocalizes semantically important edge information. A better alternative is nonlinear presmoothing (for example with Perona-Malik diffusion).

Perona-Malik



Watershed



Reconstruktion

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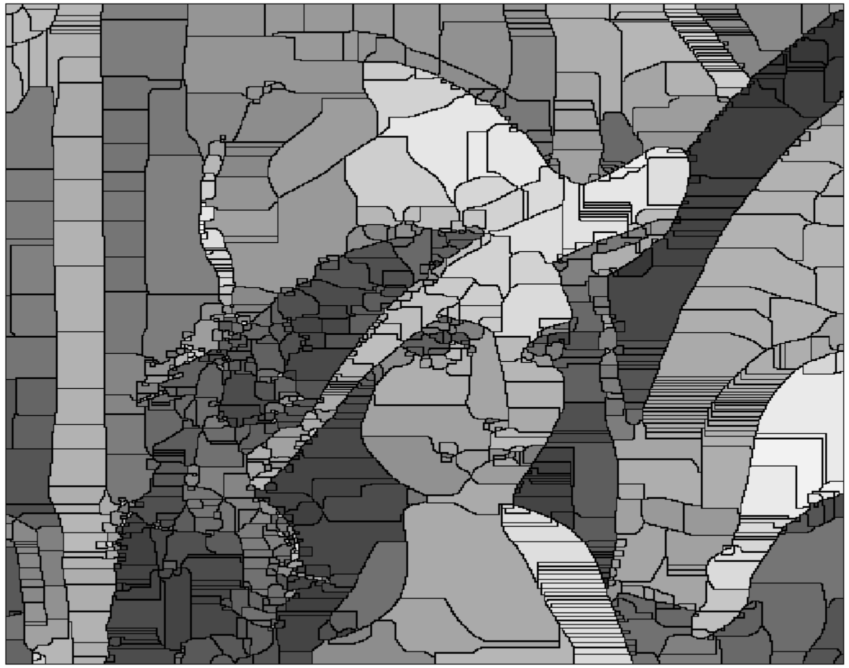
Watershed with Nonlinear Diffusion

Diffused



1104 regionen

Author: D. Cremers

Clustering with Nonlinear Diffusion

Diffused

10 cluster

Author: D. Cremers

Summary

- We have seen a number of edge-based and region-based segmentation methods (Laplace zero-crossings, thresholding, clustering, region growing, region merging, watershed).
- Edge-based methods exploit brightness discontinuities as a criterion of region boundaries. The integration of such edge information to coherent closed curves is an algorithmic challenge.
- Region-based methods exploit color similarity as a criterion for grouping pixels into coherent regions.
- The last methods (region growing, merging, watershed) also integrate some kind of neighborhood information, albeit at in a somewhat heuristic manner.
- All above methods (except for clustering) lack a mathematically transparent optimization criterion. This is where optimization methods and statistical approaches enter the picture.