





$$\begin{aligned} \int_{\mathbb{R}^{N}} \left\{ \begin{array}{c} \text{Code Extension} \\ \text$$

posiform

 $E(x) = \sum_{i=1}^{K} c_i \cdot \prod_{j \in \mathcal{C}_i} x_j,$ 

We refer to  $\Omega$  as the set of variables. The set  $\mathcal{L}=\{x|x\in\Omega\}\sqcup\{\overline{x}|x\in\Omega\}$  is called

 $E(x) = \sum_{i=1}^{K} c_i \cdot \prod_{j \in \mathcal{C}_i} x_j + C_0,$ 

the set of literals. Any pseudo-Boolean function  $E\colon \mathbb{B}\to \mathbb{R}$  can be written as a

where  $c_i \in \mathbb{R}$  and  $C_i \subset \Omega$ . We call  $C_i$  a **clique**. If the multi-linear function only

 Literature \*
 Literature \*

 Pseudo-Boolean Function
 Submodularity
 Lovász Extension
 Multilinear Extension

 Pseudo Boolean Optimization
 Boros and Hammer, Pseudo-Boolean Optimization, 2002, Discrete Applied Mathematics (123), 155–225.

## Submodularity

- Edmonds, Submodular Functions, Matroids, and Certain Polyhedra, 1970, Combinatorial structures and their applications, 69–87.
- Boros and Hammer, *Pseudo-Boolean Optimization*, 2002, Discrete Applied Mathematics (123), 155–225.
- Schrijver, Combinatorial Optimization, Chapters 44-45.

where  $c_i > 0$ ,  $C_0 \in \mathbb{R}$  and  $C_i \subset \mathcal{L}$ . This representation is **not** unique.

 $E: \mathbb{B}^N \to \mathbb{R}$  can be uniquely written as a multi-linear function

contains cliques of size  $|C_i| \leq 2$ , we call it a **quadratic** function.