

Lecture 2 Recap

Nearest Neighbor

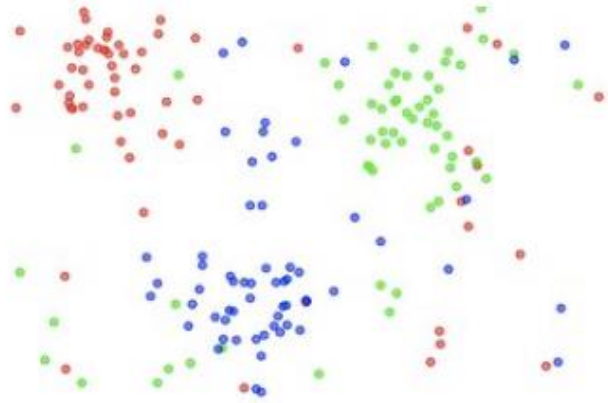
NN classifier = dog



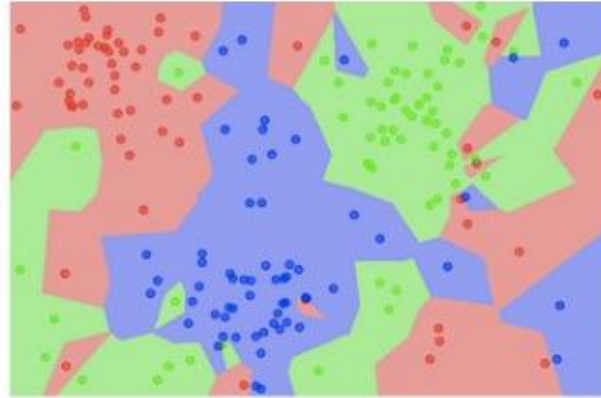
distance

Nearest Neighbor

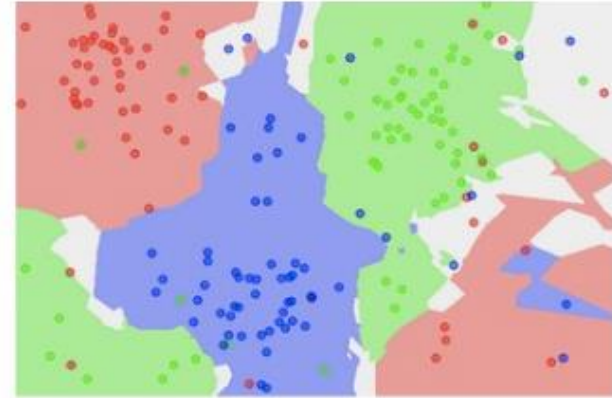
the data



NN classifier



5-NN classifier

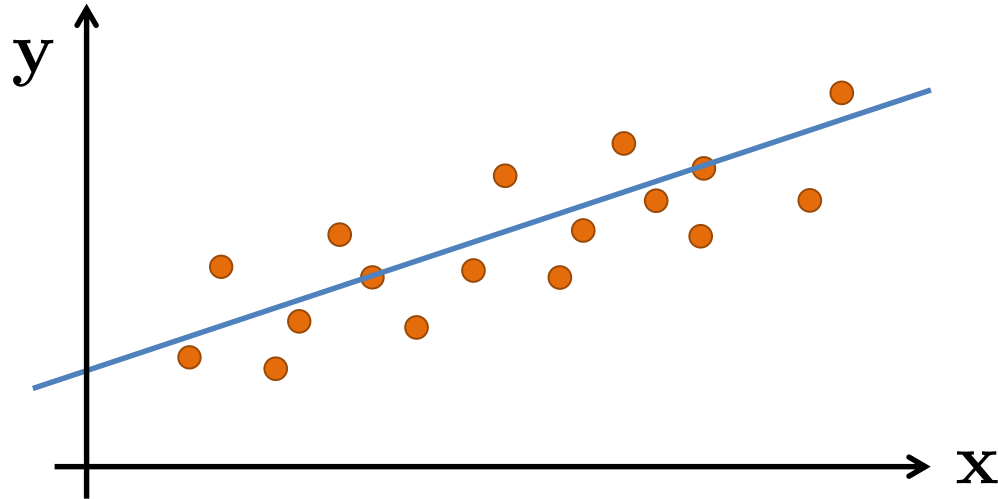


What is the performance on training data for NN classifier?

What classifier is more likely to perform best on test data?

Linear Regression

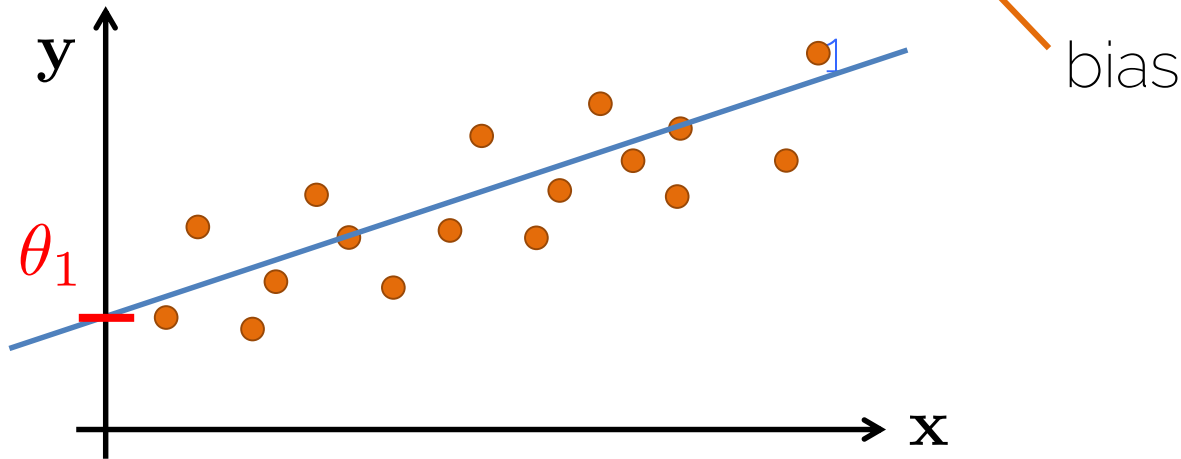
- Supervised learning
- Find a linear model that explains a target \mathbf{y} given the inputs \mathbf{X}



Linear Regression

- A linear model is expressed in the form

$$\hat{y}_i = \sum_{j=1}^d x_{ij}\theta_j = x_{i1}\theta_1 + x_{i2}\theta_2 + \cdots + x_{id}\theta_d$$



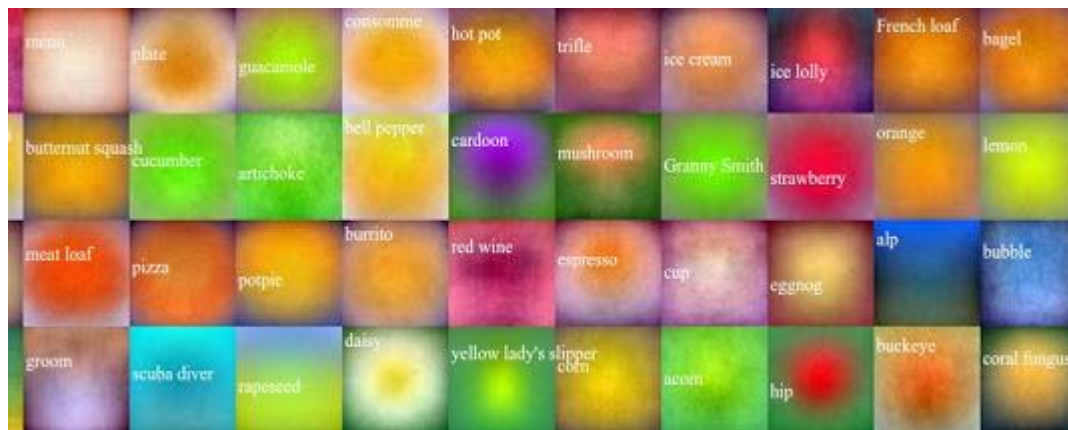
Introduction to Neural Networks

Neural Network

- Linear score function $f = Wx$



On CIFAR-10



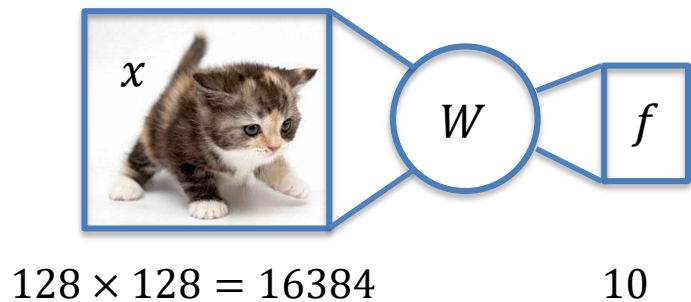
On ImageNet

Neural Network

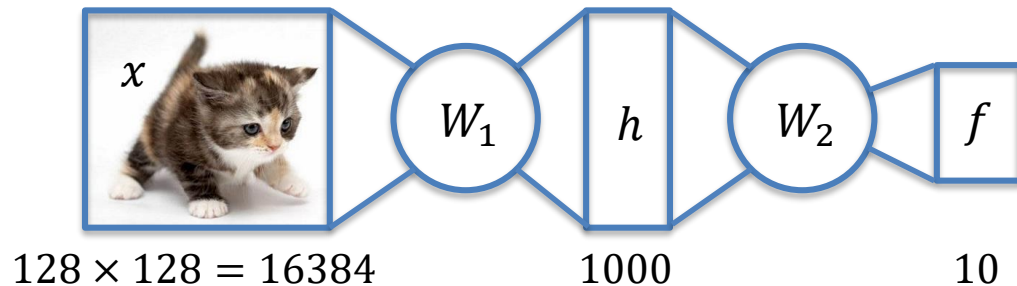
- Linear score function $f = Wx$
- Neural network is a nesting of 'functions'
 - 2-layers: $f = W_2 \max(0, W_1 x)$
 - 3-layers: $f = W_3 \max(0, W_2 \max(0, W_1 x))$
 - 4-layers: $f = W_4 \tanh(W_3, \max(0, W_2 \max(0, W_1 x)))$
 - 5-layers: $f = W_5 \sigma(W_4 \tanh(W_3, \max(0, W_2 \max(0, W_1 x))))$
 - ... up to hundreds of layers

Neural Network

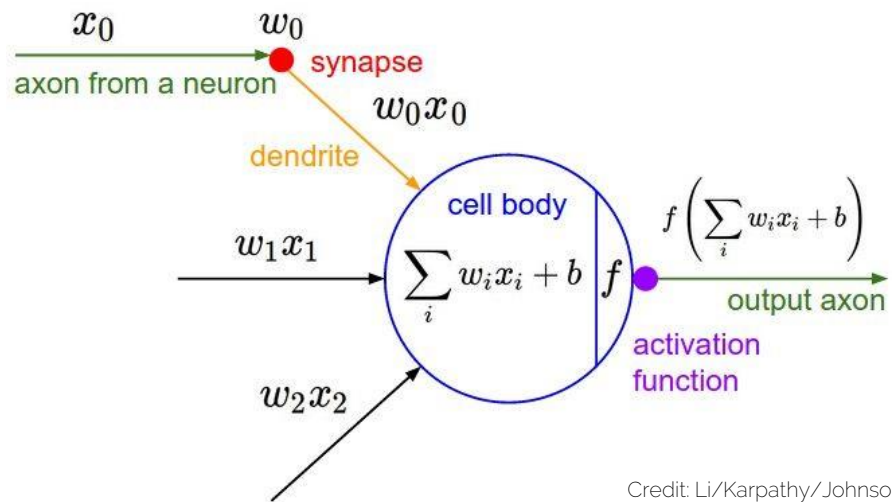
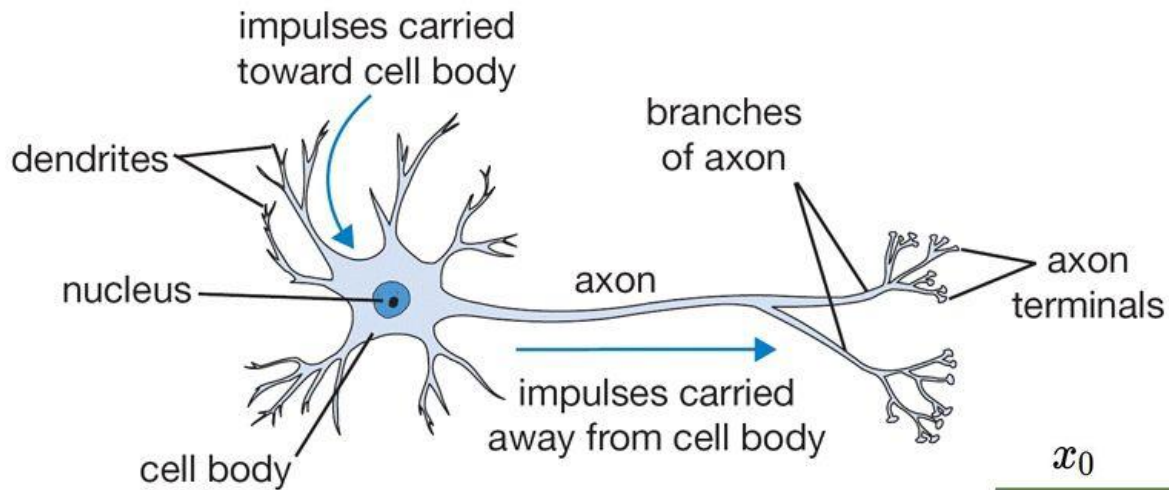
1-layer network: $f = Wx$



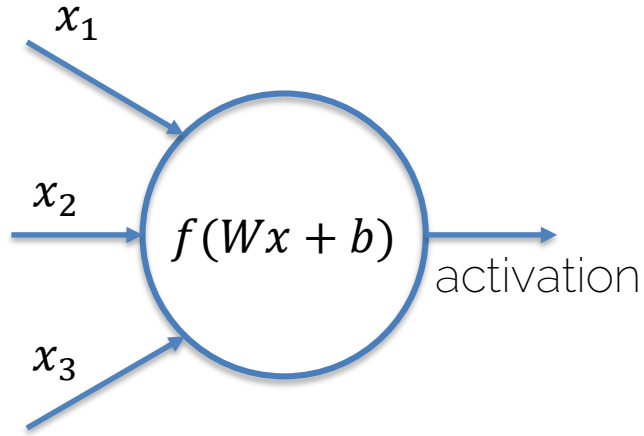
2-layer network: $f = W_2 \max(0, W_1 x)$



Neurons



Neurons

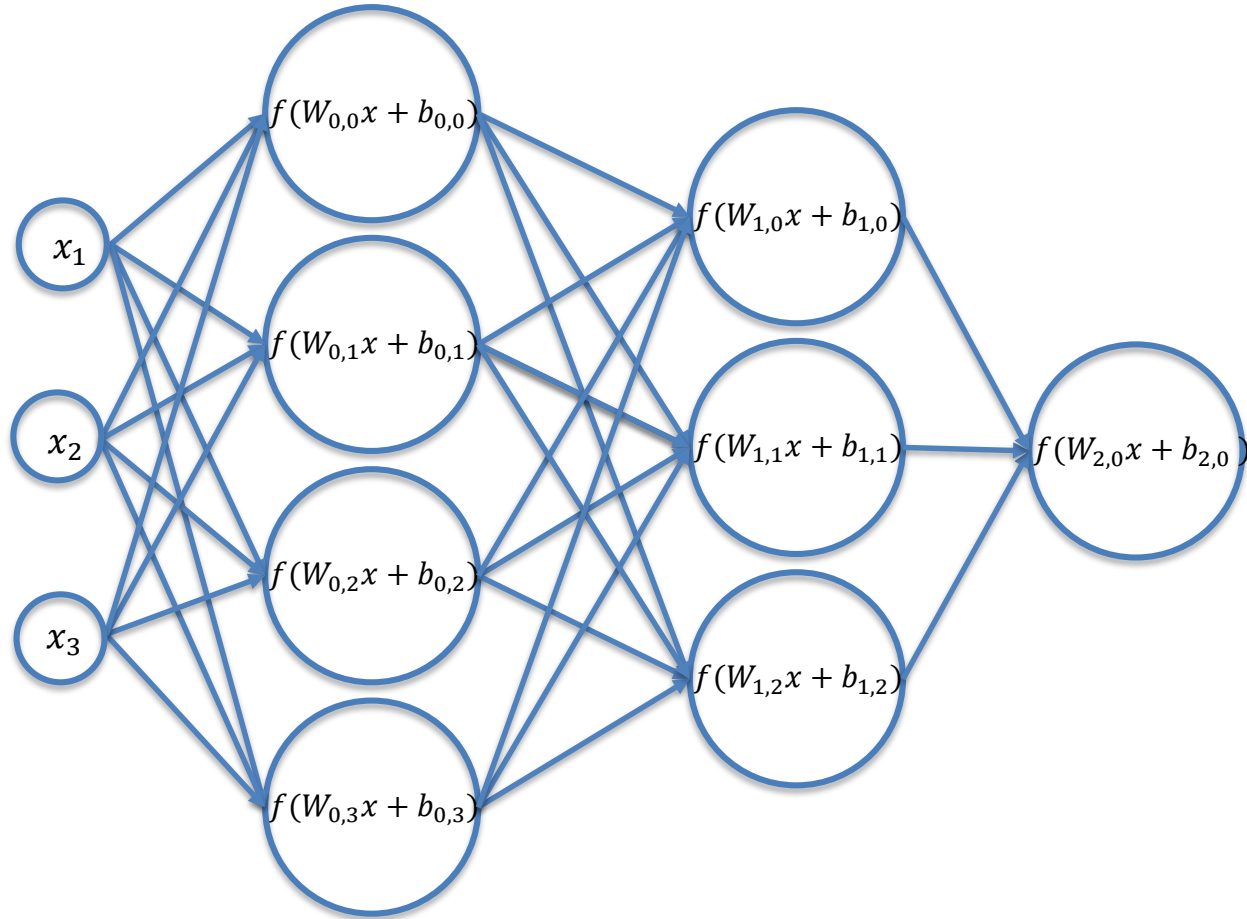


Linear function: $Wx + b$

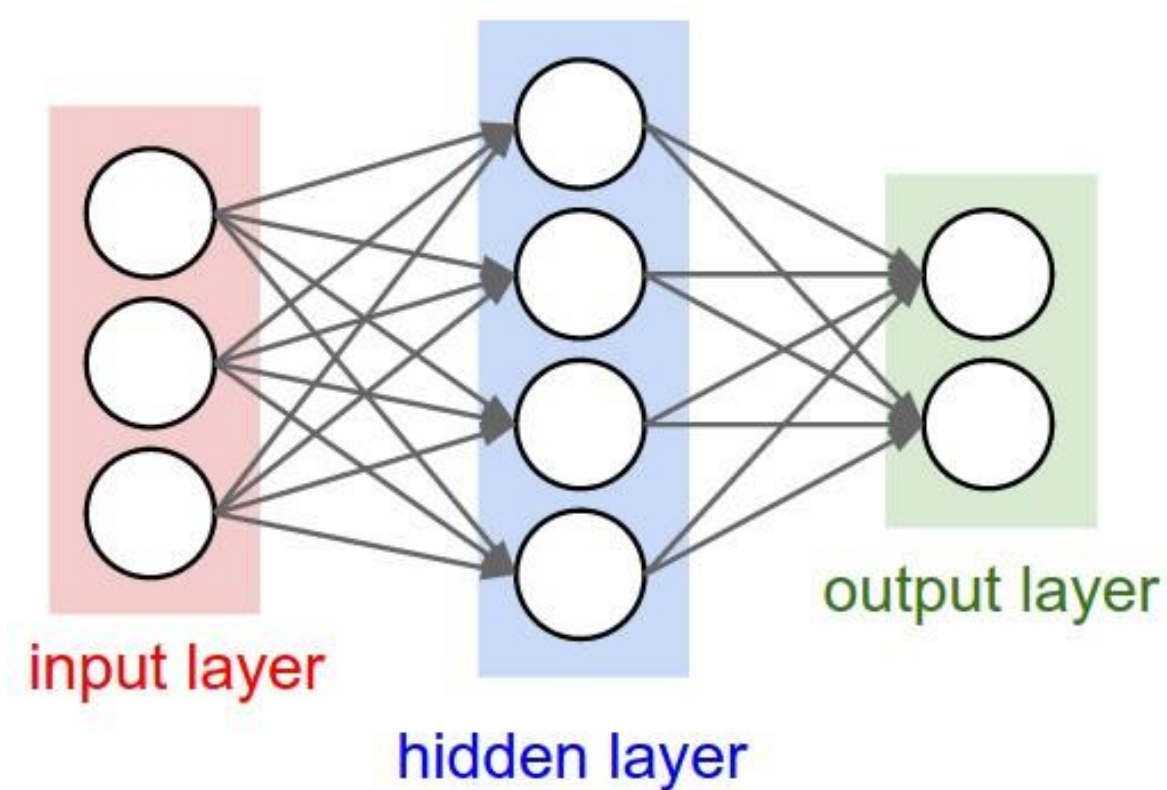
Non-linearity (activation): $f(x)$

Every neuron computes: $f(Wx + b)$

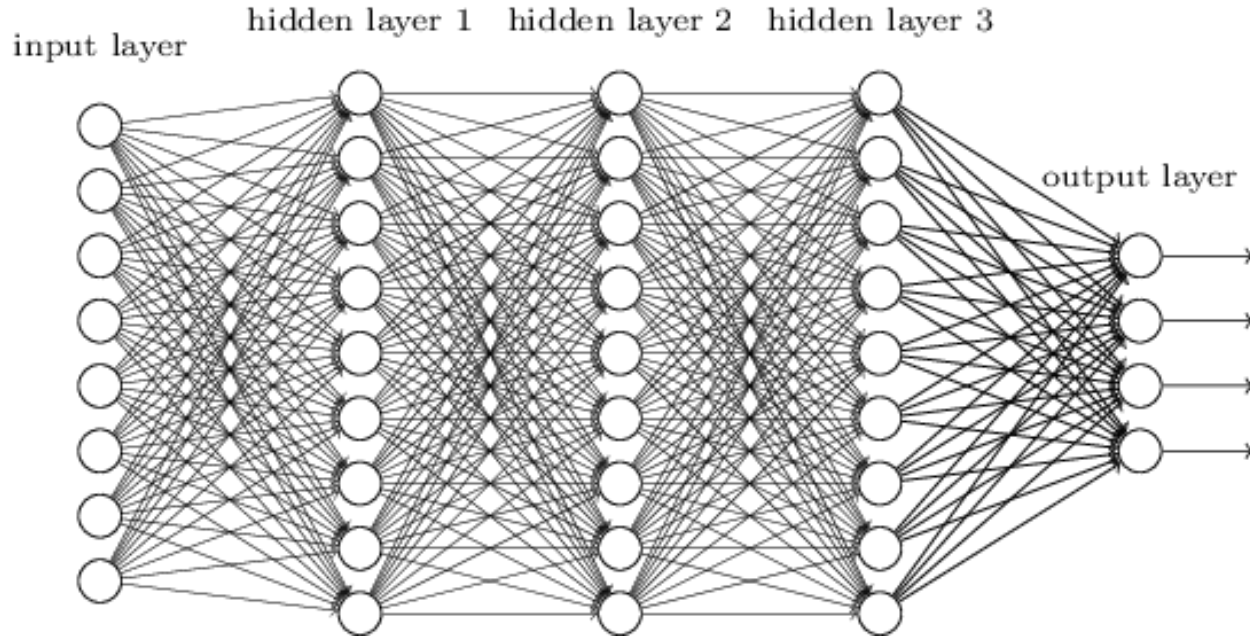
Net of Neurons



Neural Network



Neural Network



Neural Network

$$f = W_3 \cdot (W_2 \cdot (W_1 \cdot x))$$

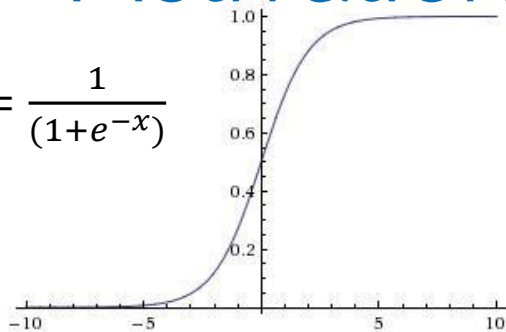
Why activation functions?

Why not just concatenate?

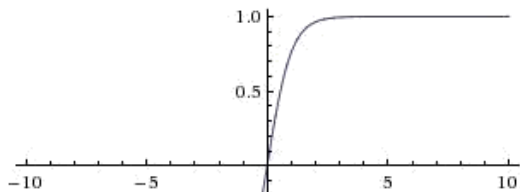
Would be much cheaper to
compute...

Activation Functions

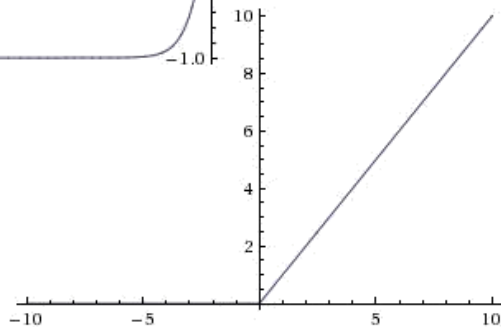
Sigmoid: $\sigma(x) = \frac{1}{1+e^{-x}}$



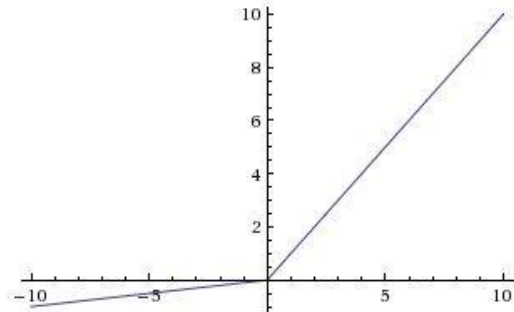
tanh: $\tanh(x)$



ReLU: $\max(0, x)$



Leaky ReLU: $\max(0.1x, x)$



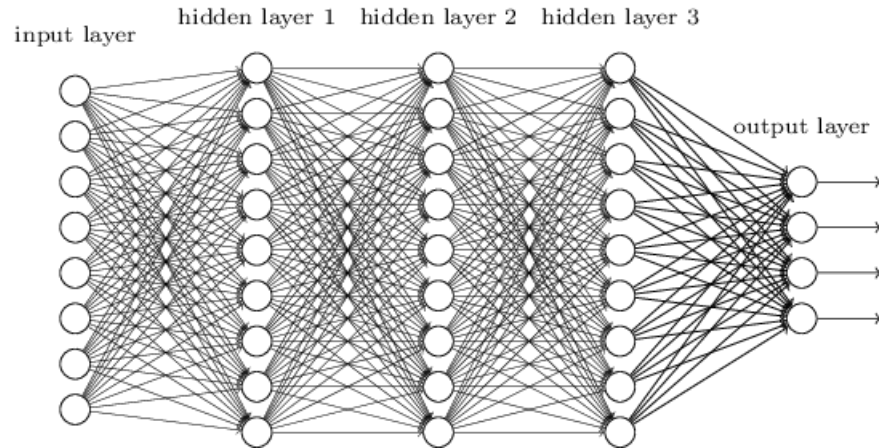
Parametric ReLU: $\max(\alpha x, x)$

Maxout $\max(w_1^T x + b_1, w_2^T x + b_2)$

ELU $f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha(e^x - 1) & \text{if } x \leq 0 \end{cases}$

Neural Network

Why organize a neural network into layers?



Neural Network

- Summary
 - Given a dataset with ground truth training pairs $[x_i; y_i]$,
 - Find optimal weights W using stochastic gradient descent, such that the loss function is minimized
 - Compute gradients with backpropagation (use batch-mode; more later)
 - Iterate many times over training set (SGD; more later)

Artificial Neural Network vs Brain



Artificial neural networks: inspired but not even close to the brain!
It's much more complex than simple linearity + activations
Great for the media and news articles 😊

Artificial Neural Network vs Brain



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GOOGLE · 3 days ago

Google's artificial intelligence computer 'no longer constrained by limits of human knowledge'



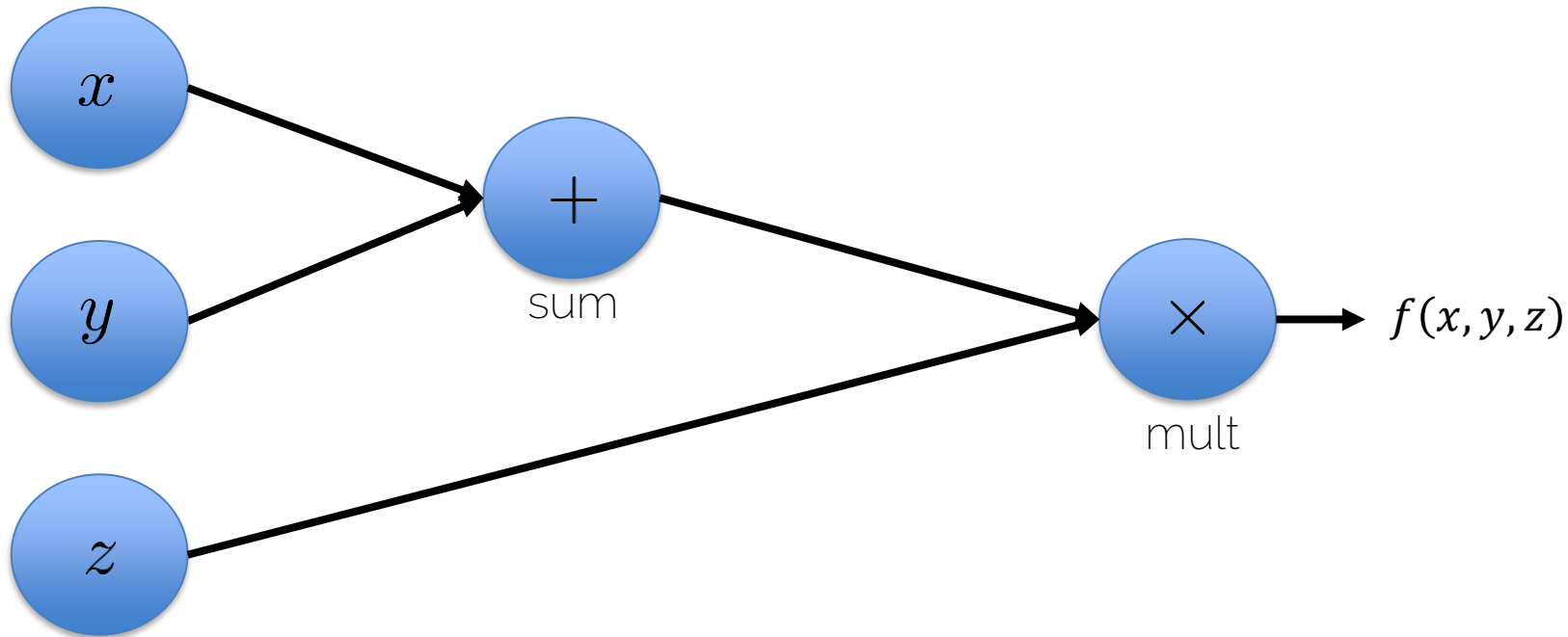
Computational Graphs

Computational Graphs

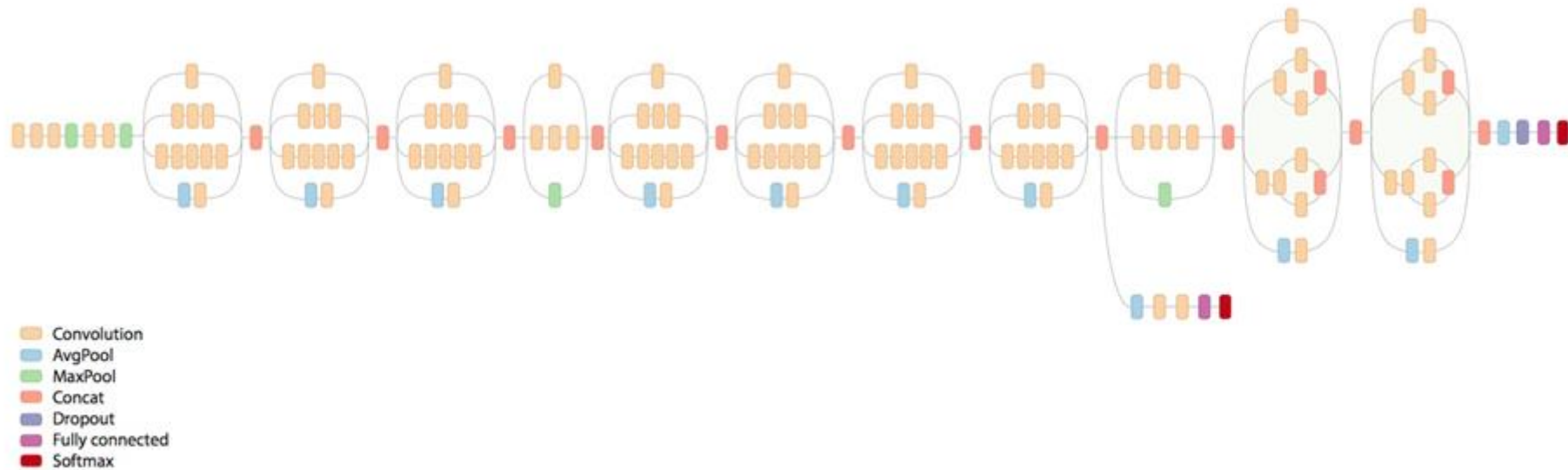
- Neural network is a computational graph
 - It has compute nodes
 - It has edges that connect nodes
 - It is directional
 - It is organized in 'layers'

Computational Graphs

- $f(x, y, z) = (x + y) \cdot z$



Computational Graphs

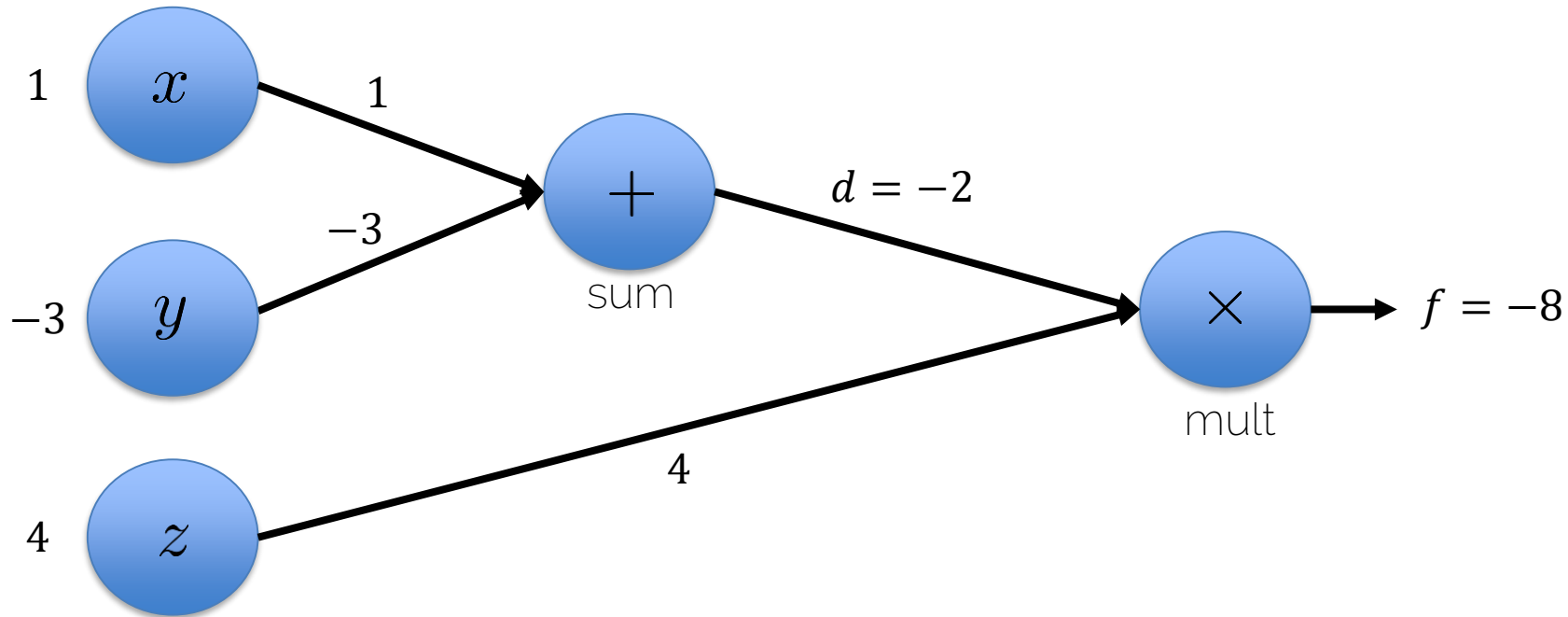


Another view of GoogLeNet's architecture.

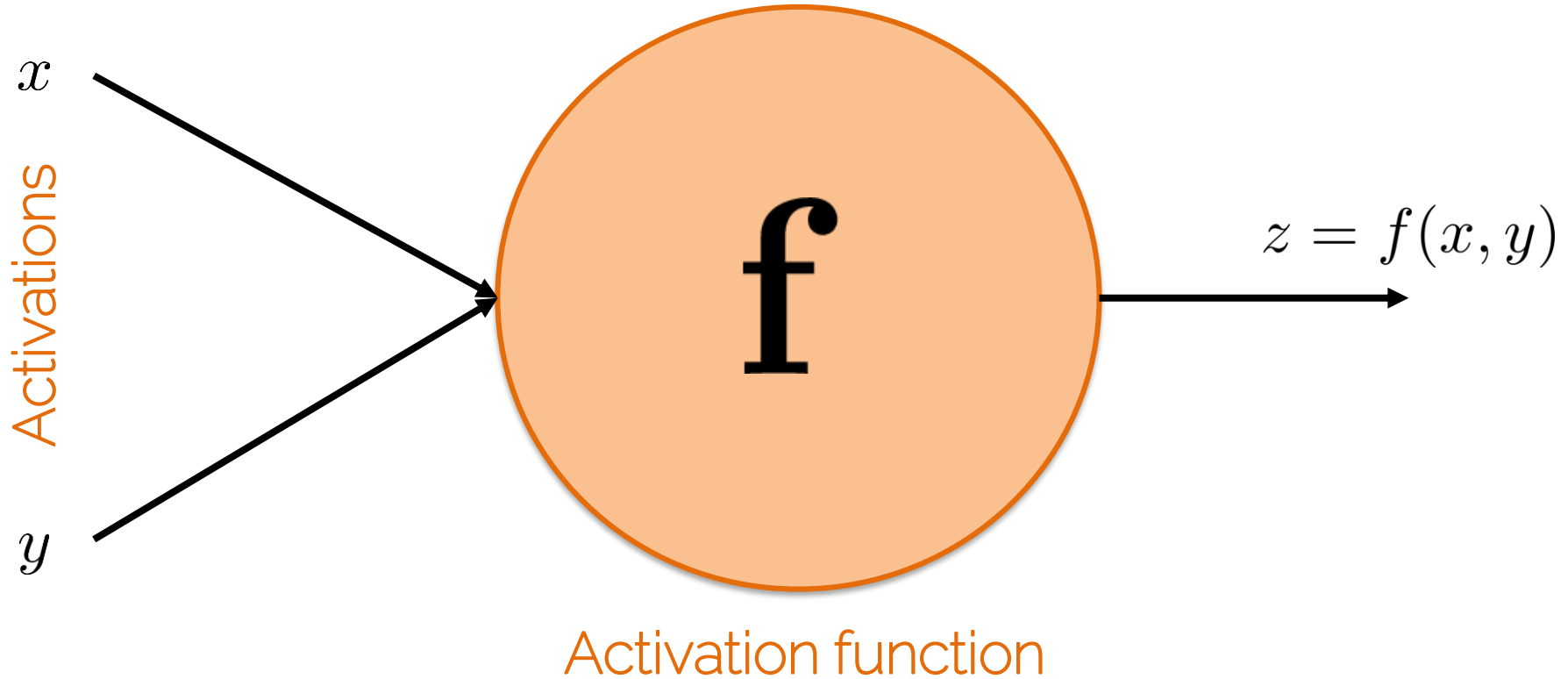
Evaluation: Forward Pass

- $f(x, y, z) = (x + y) \cdot z$

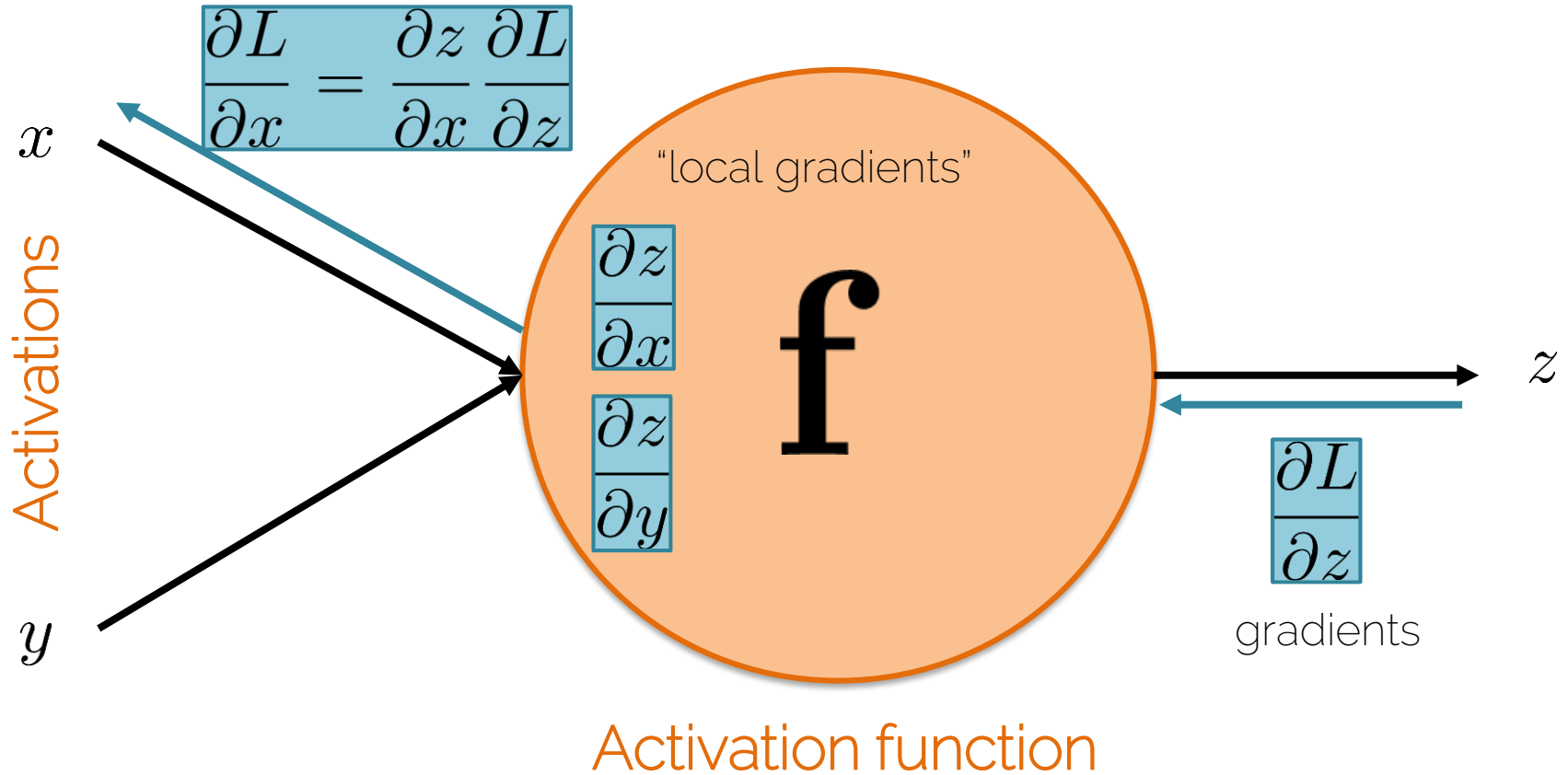
Initialization $x = 1, y = -3, z = 4$



The Flow of Gradients



The Flow of Gradients

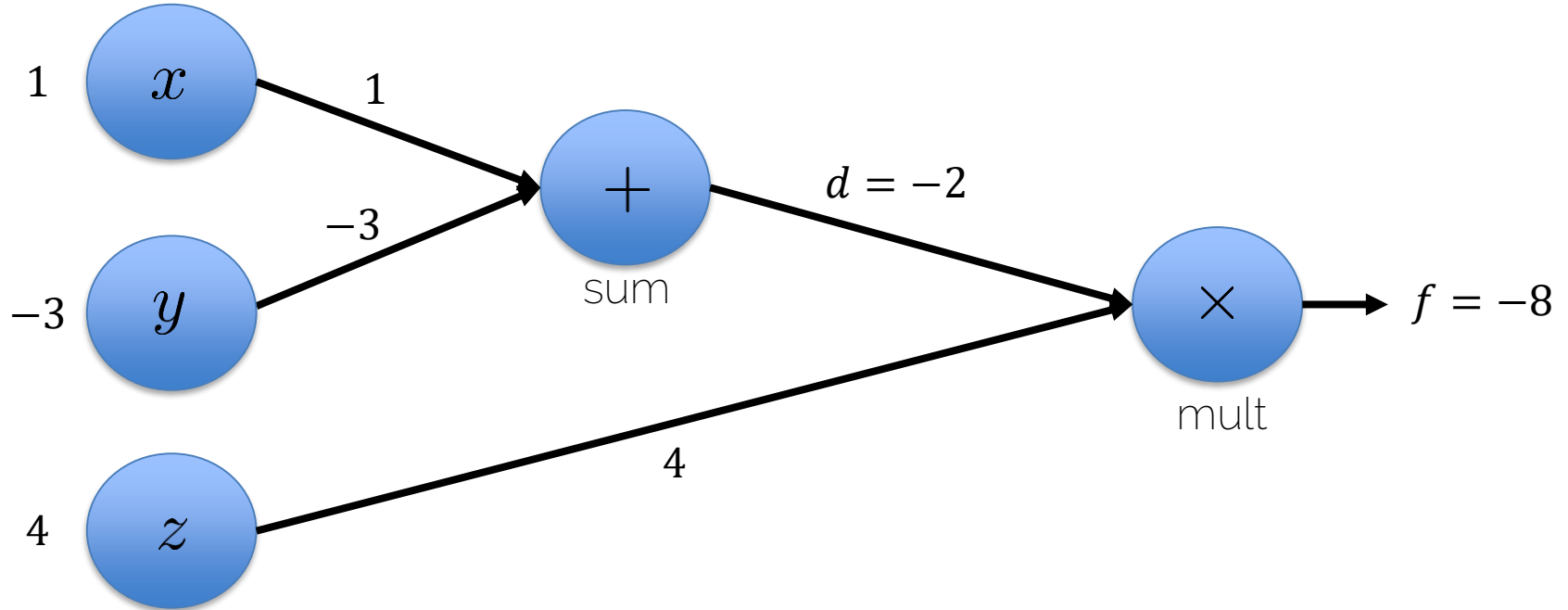


Backpropagation

Backprop: Forward Pass

- $f(x, y, z) = (x + y) \cdot z$

Initialization $x = 1, y = -3, z = 4$



Backprop: Backward Pass

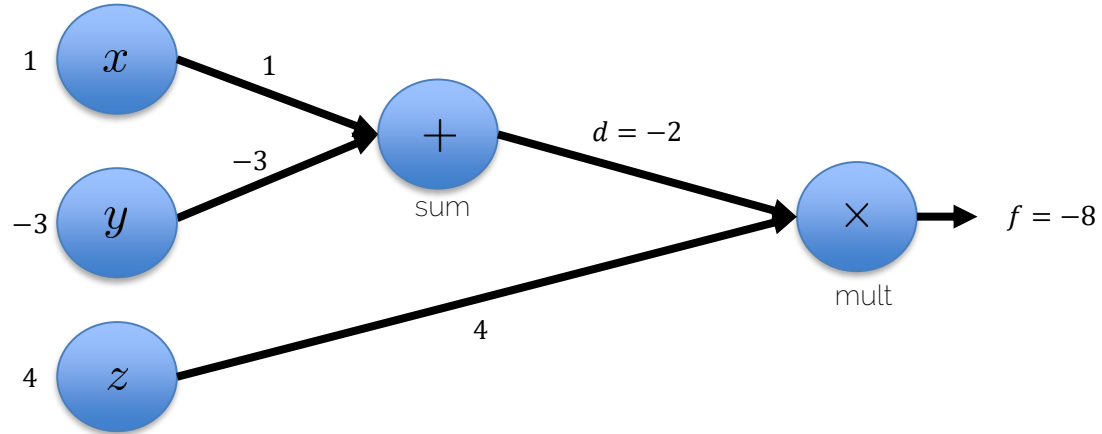
$$f(x, y, z) = (x + y) \cdot z$$

with $x = 1, y = -3, z = 4$

$$d = x + y \quad \frac{\partial d}{\partial x} = 1, \frac{\partial d}{\partial y} = 1$$

$$f = d \cdot z \quad \frac{\partial f}{\partial d} = z, \frac{\partial f}{\partial z} = d$$

What is $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$?



Backprop: Backward Pass

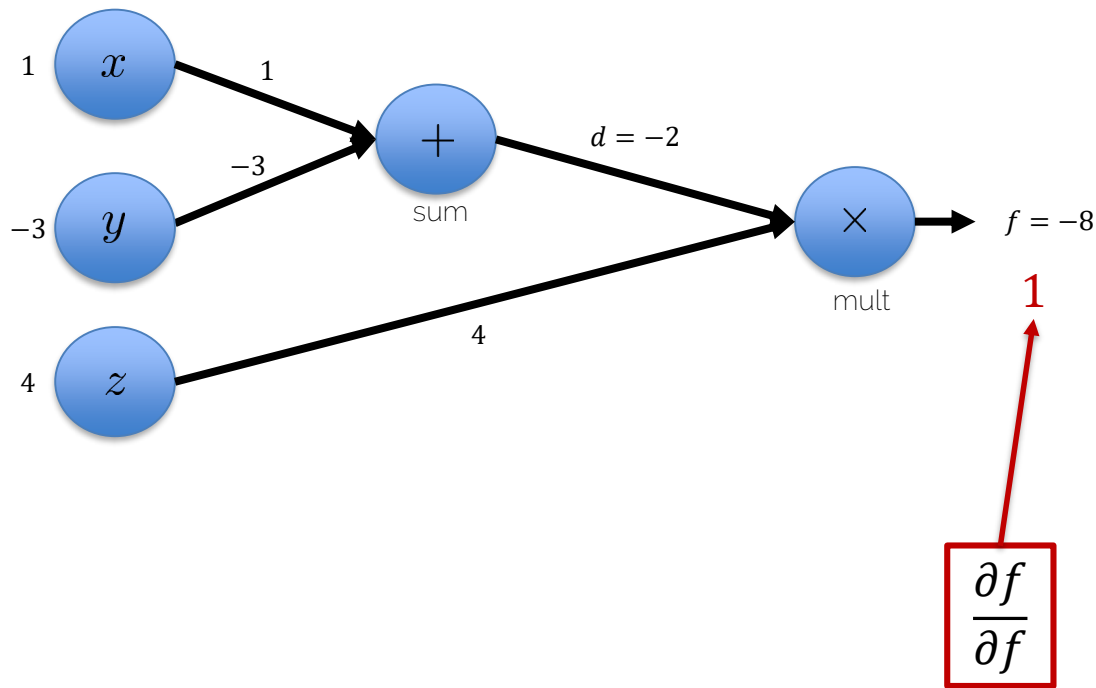
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Backprop: Backward Pass

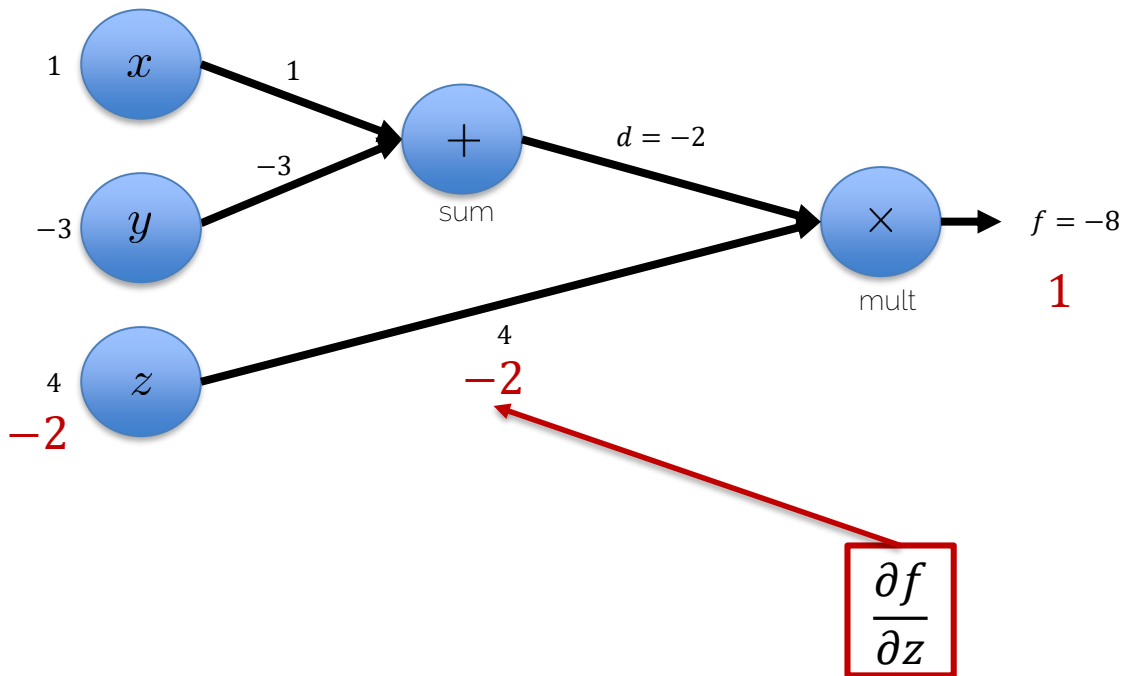
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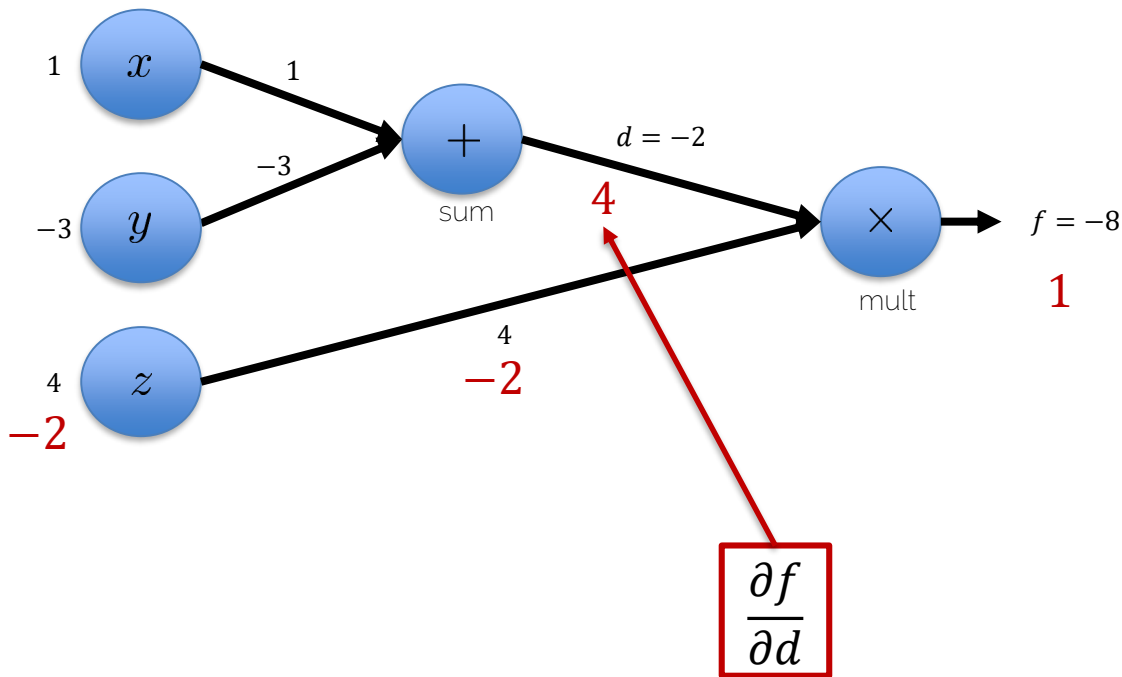
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Backprop: Backward Pass

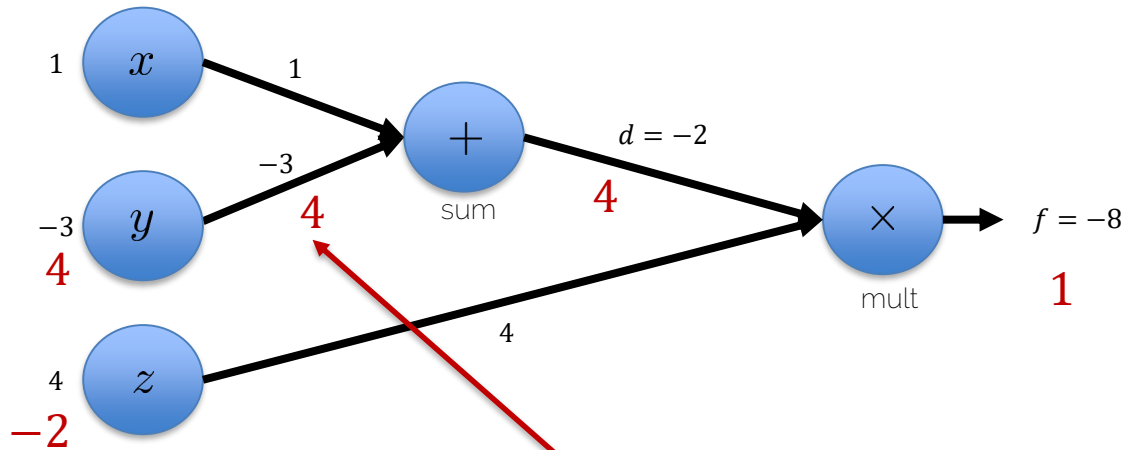
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What is $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$?



Chain Rule:

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial d} \cdot \frac{\partial d}{\partial y}$$

$$\rightarrow \frac{\partial f}{\partial y} = 4 \cdot 1 = 4$$

$$\frac{\partial f}{\partial y}$$

Backprop: Backward Pass

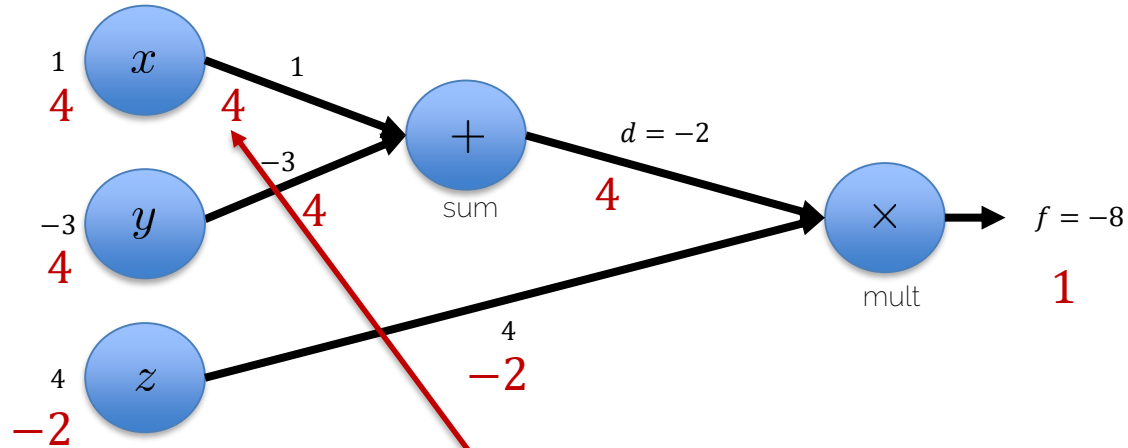
$$f(x, y, z) = (x + y) \cdot z$$

with $x = 1, y = -3, z = 4$

$$d = x + y \quad \boxed{\frac{\partial d}{\partial x} = 1} \quad \frac{\partial d}{\partial y} = 1$$

$$f = d \cdot z \quad \frac{\partial f}{\partial d} = z, \quad \frac{\partial f}{\partial z} = d$$

What is $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$?



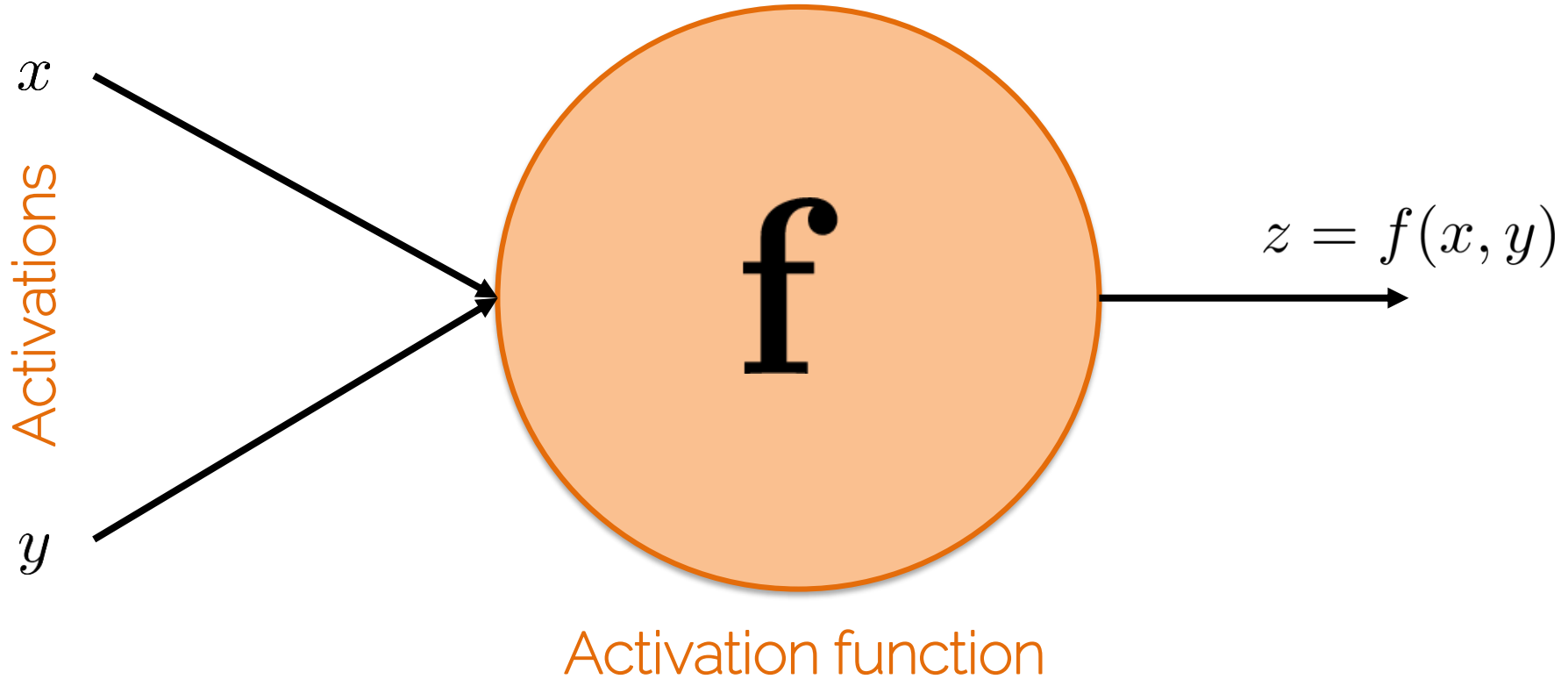
Chain Rule:

$$\boxed{\frac{\partial f}{\partial x} = \frac{\partial f}{\partial d} \cdot \frac{\partial d}{\partial x}}$$

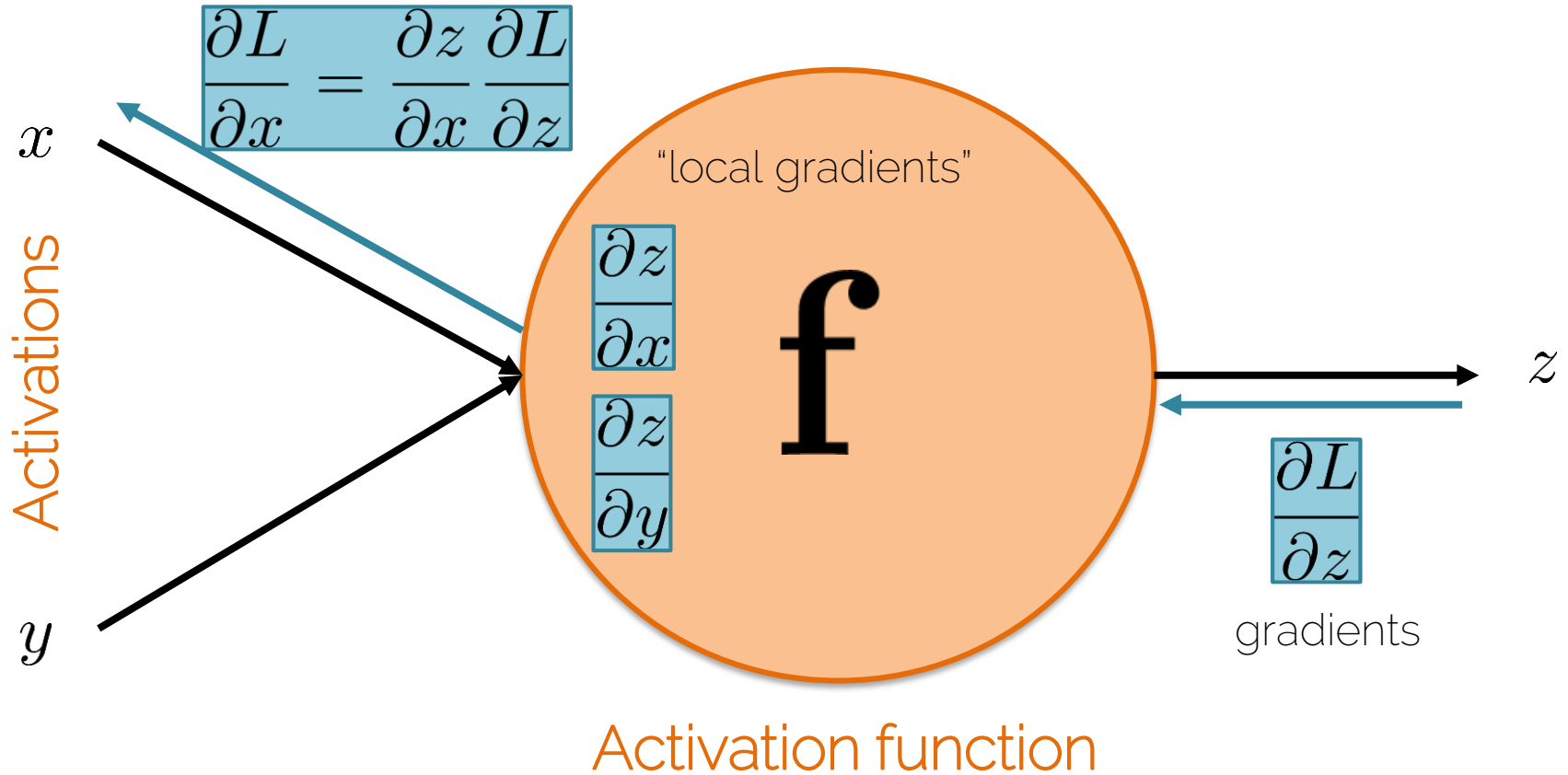
$$\rightarrow \frac{\partial f}{\partial x} = 4 \cdot 1 = -4$$

$$\boxed{\frac{\partial f}{\partial x}}$$

The Flow of Gradients

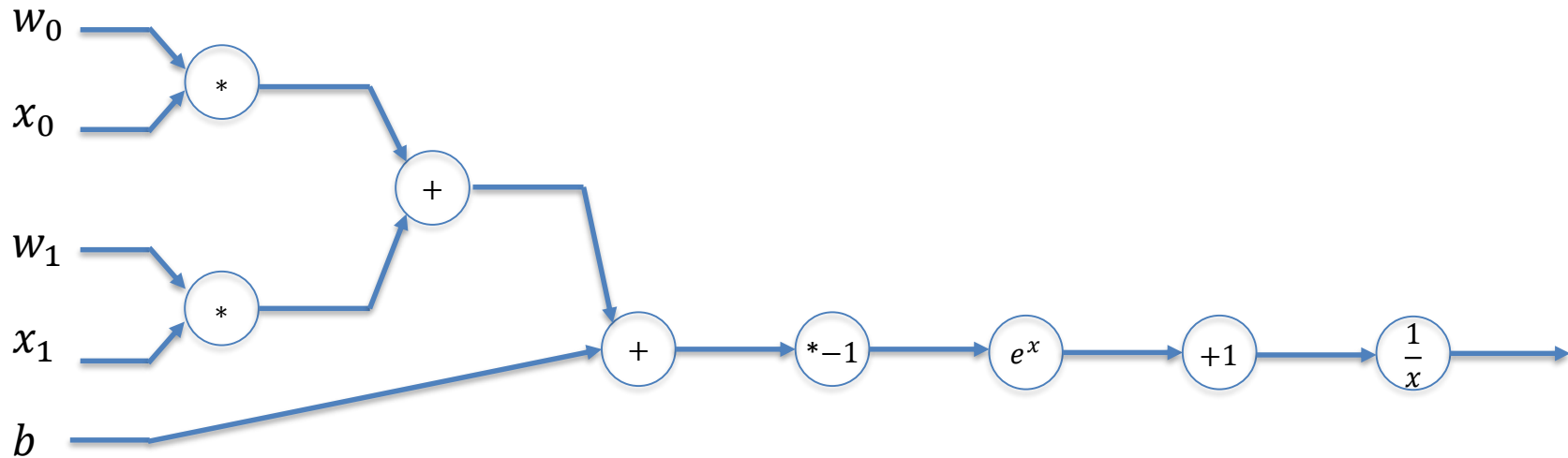


The Flow of Gradients



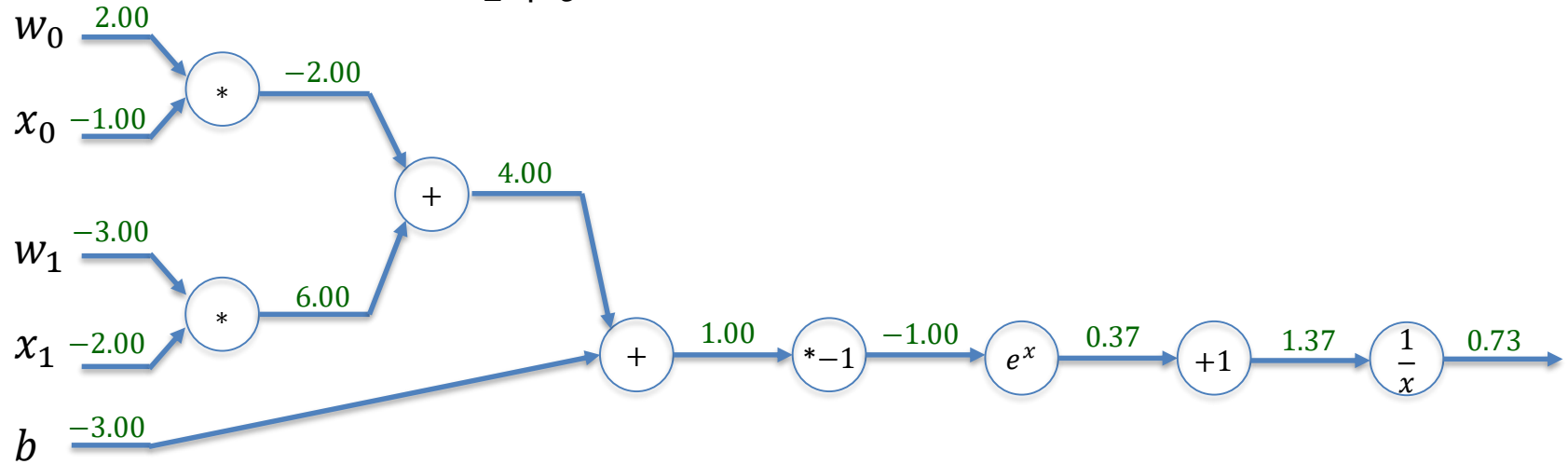
Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



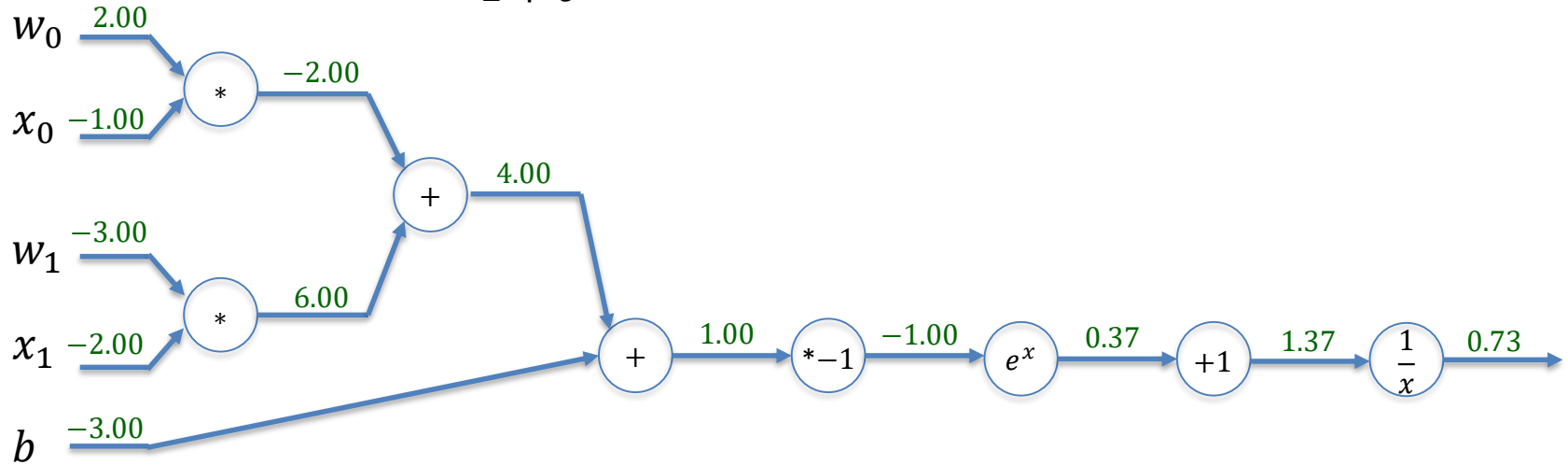
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$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

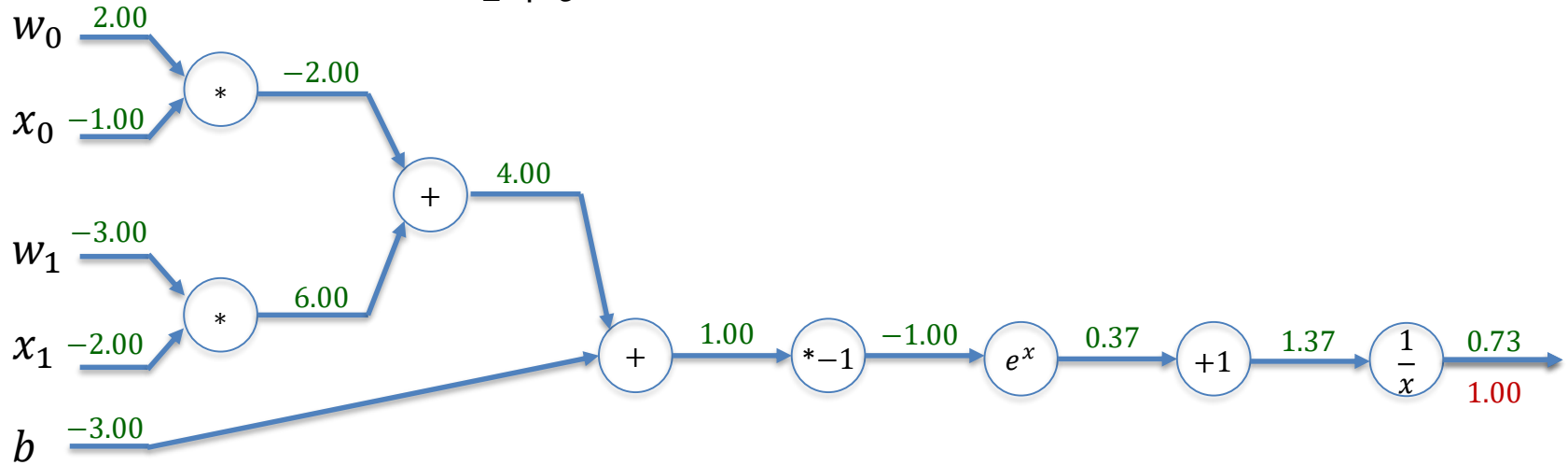
$$f(x) = \frac{1}{x} \quad \rightarrow \quad \frac{\partial f}{\partial x} = -\frac{1}{x^2}$$

$$f_a(x) = ax \quad \rightarrow \quad \frac{\partial f_a}{\partial x} = a$$

$$f_c(x) = c + x \quad \rightarrow \quad \frac{\partial f_c}{\partial x} = 1$$

Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

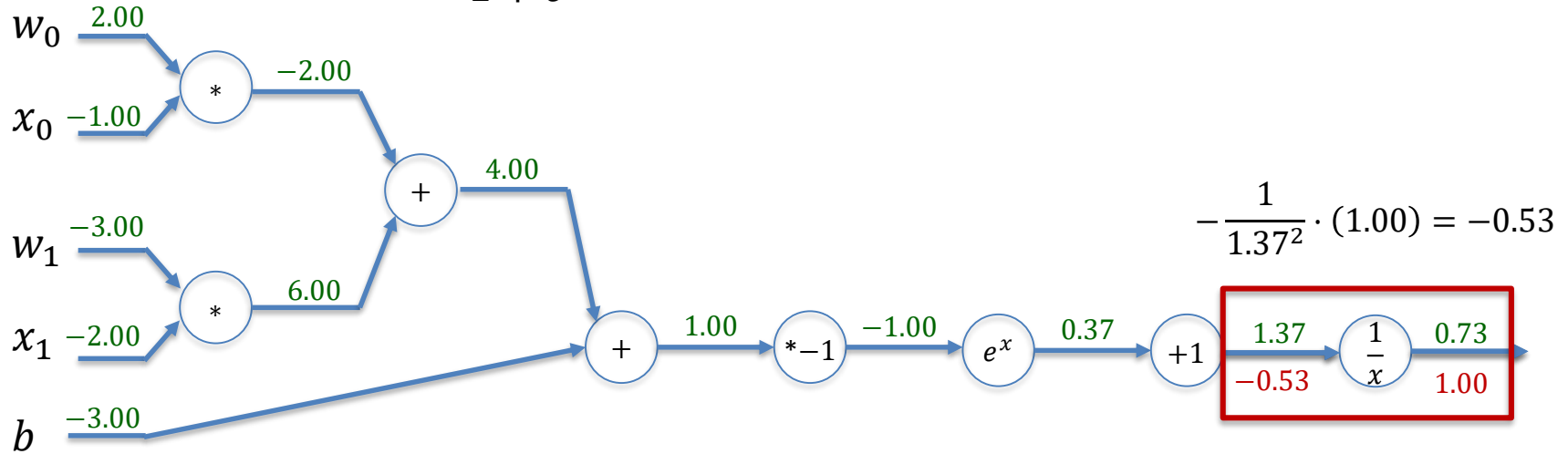
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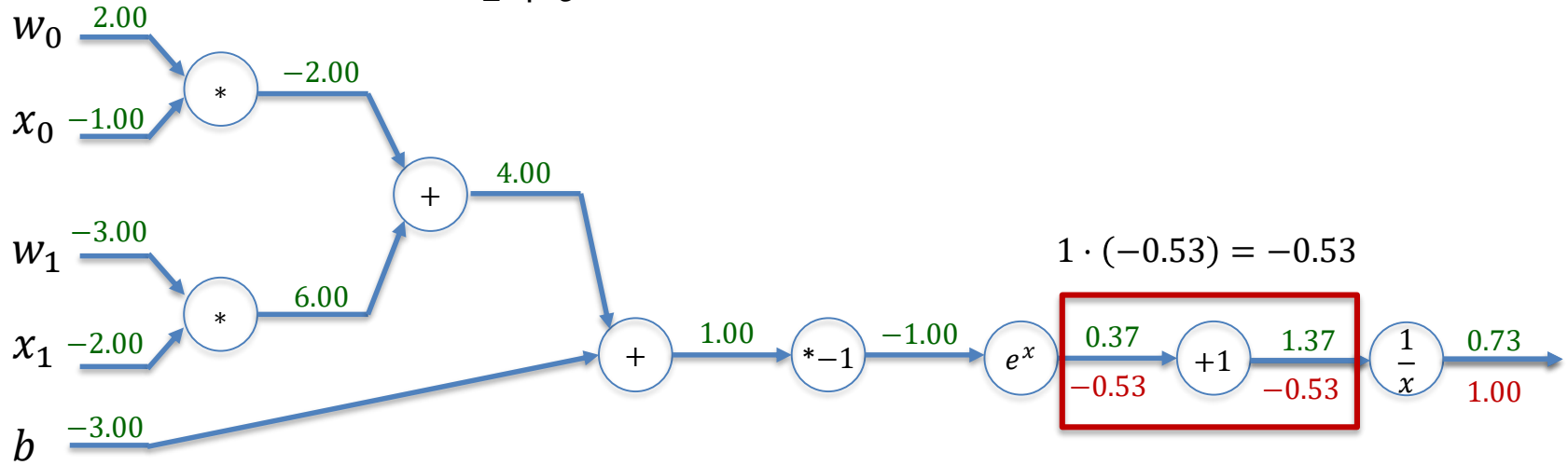
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Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$1 \cdot (-0.53) = -0.53$$

$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

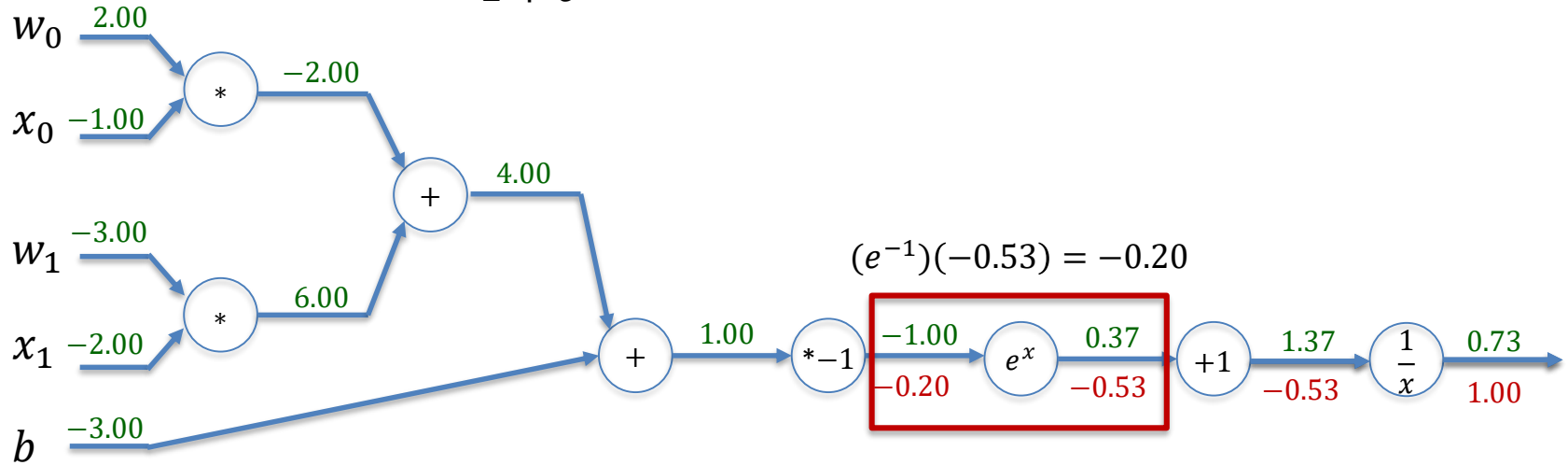
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$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

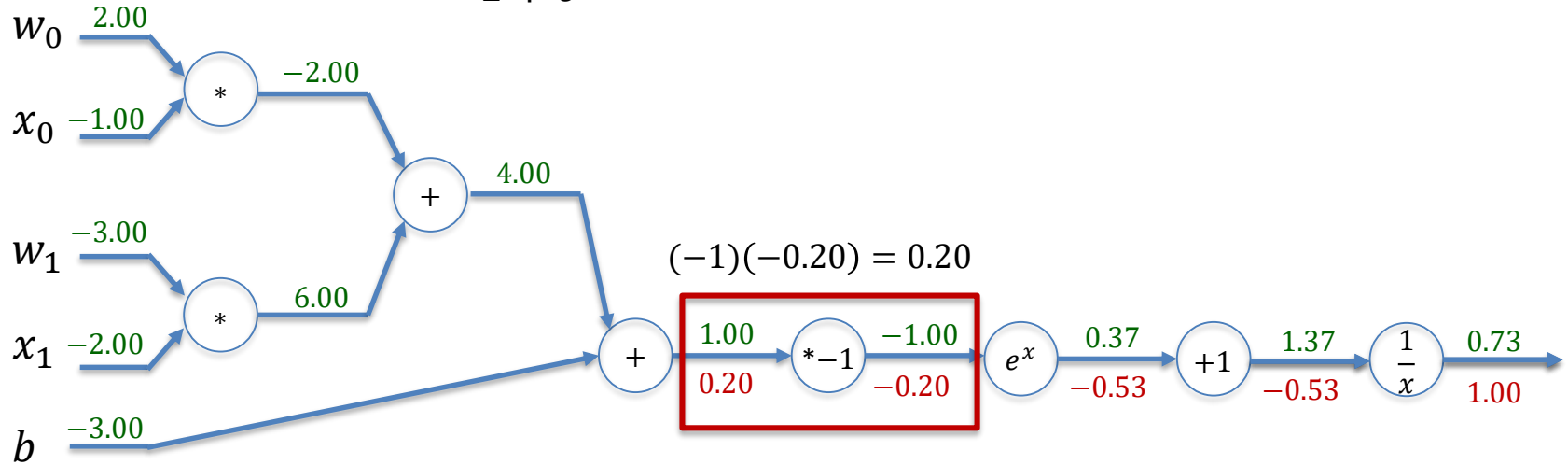
$$f(x) = \frac{1}{x} \quad \rightarrow \quad \frac{\partial f}{\partial x} = -\frac{1}{x^2}$$

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Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



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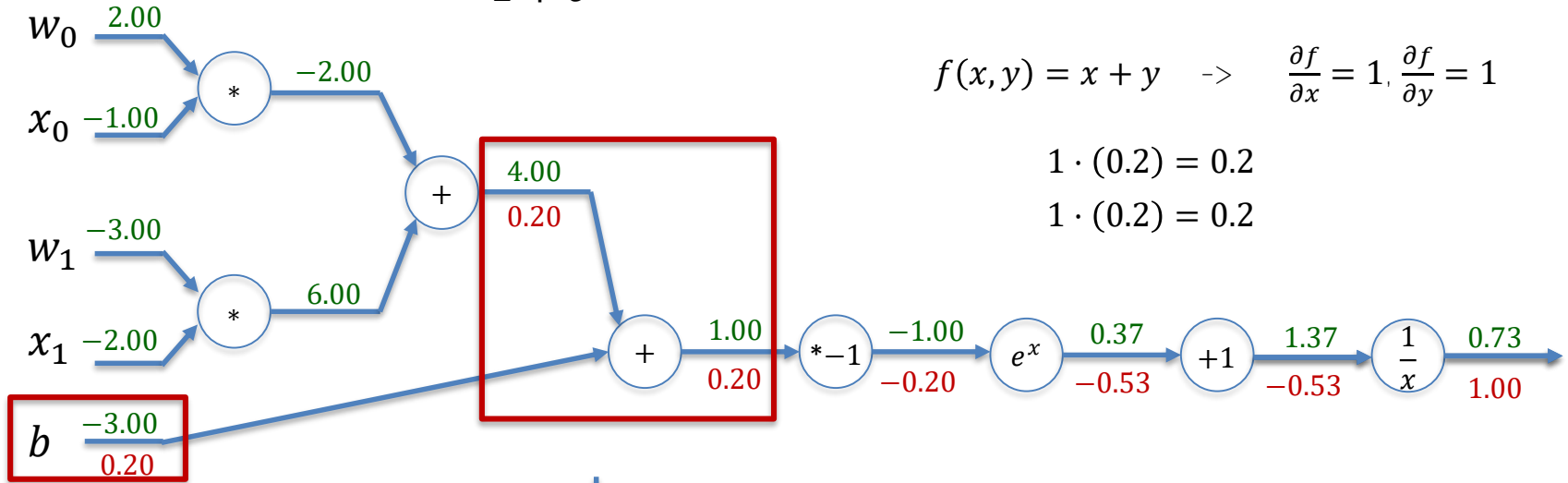
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$$f_a(x) = ax \quad \rightarrow \quad \frac{\partial f_a}{\partial x} = a$$

$$f_c(x) = c + x \quad \rightarrow \quad \frac{\partial f_c}{\partial x} = 1$$

Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x, y) = x + y \quad \rightarrow \quad \frac{\partial f}{\partial x} = 1, \quad \frac{\partial f}{\partial y} = 1$$

$$1 \cdot (0.2) = 0.2$$

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$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

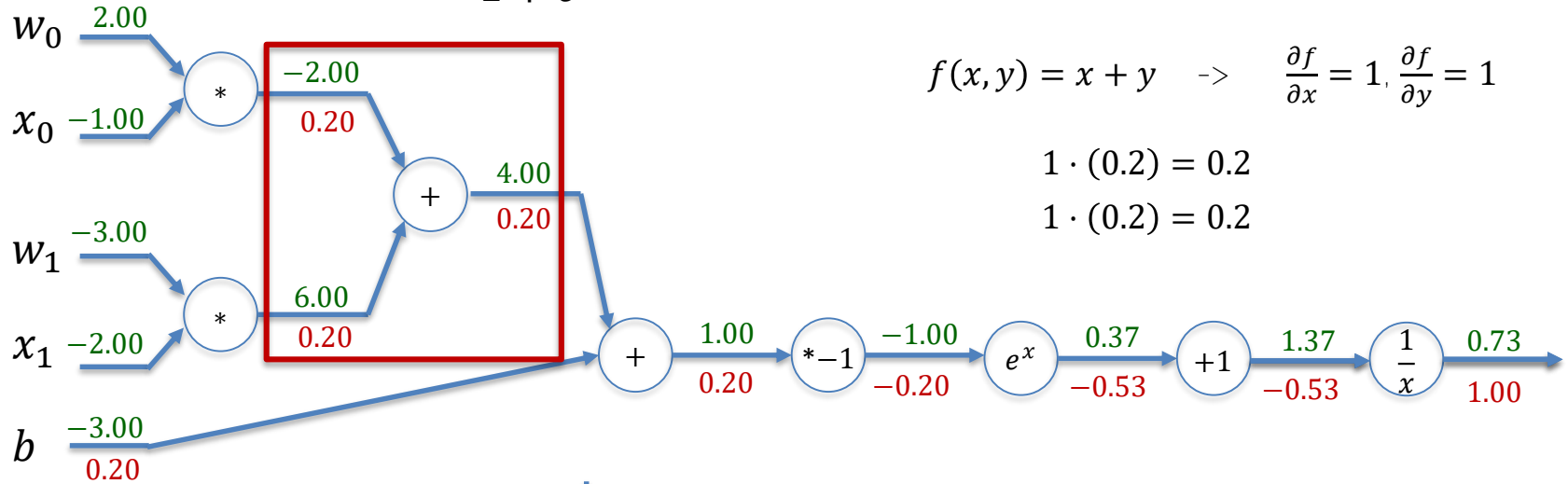
$$f(x) = \frac{1}{x} \quad \rightarrow \quad \frac{\partial f}{\partial x} = -\frac{1}{x^2}$$

$$f_a(x) = ax \quad \rightarrow \quad \frac{\partial f_a}{\partial a} = x$$

$$f_c(x) = c + x \quad \rightarrow \quad \frac{\partial f_c}{\partial c} = 1$$

Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x, y) = x + y \quad \rightarrow \quad \frac{\partial f}{\partial x} = 1, \quad \frac{\partial f}{\partial y} = 1$$

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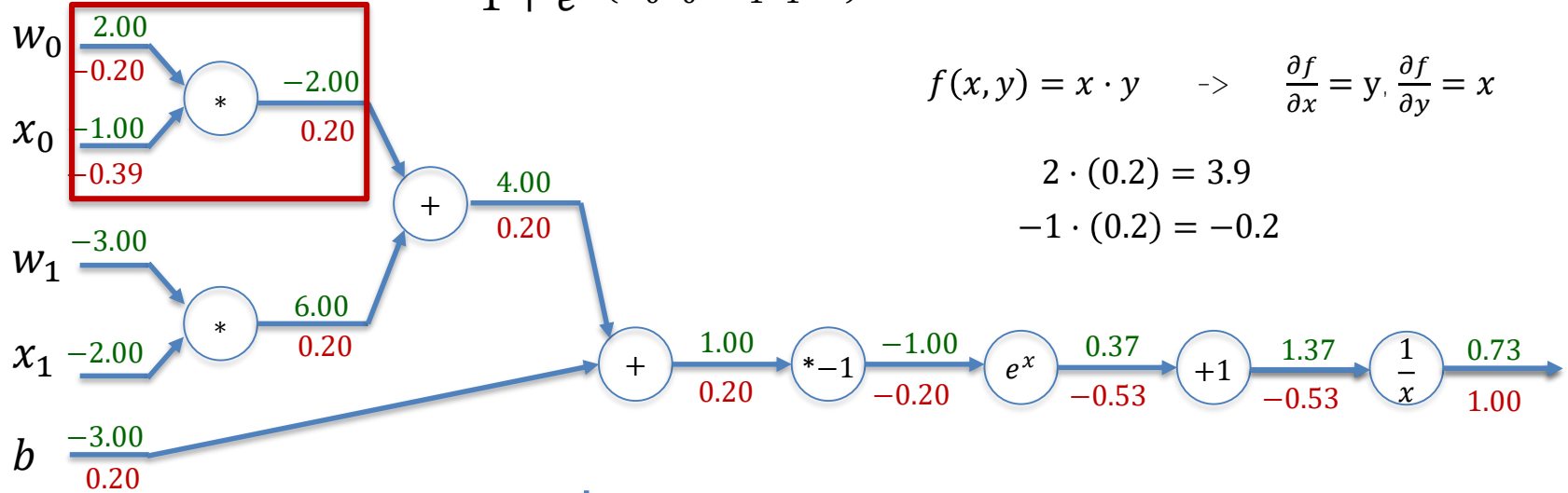
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$$f_a(x) = ax \quad \rightarrow \quad \frac{\partial f_a}{\partial x} = a$$

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Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x, y) = x \cdot y \quad \rightarrow \quad \frac{\partial f}{\partial x} = y, \quad \frac{\partial f}{\partial y} = x$$

$$2 \cdot (0.2) = 3.9$$

$$-1 \cdot (0.2) = -0.2$$

$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

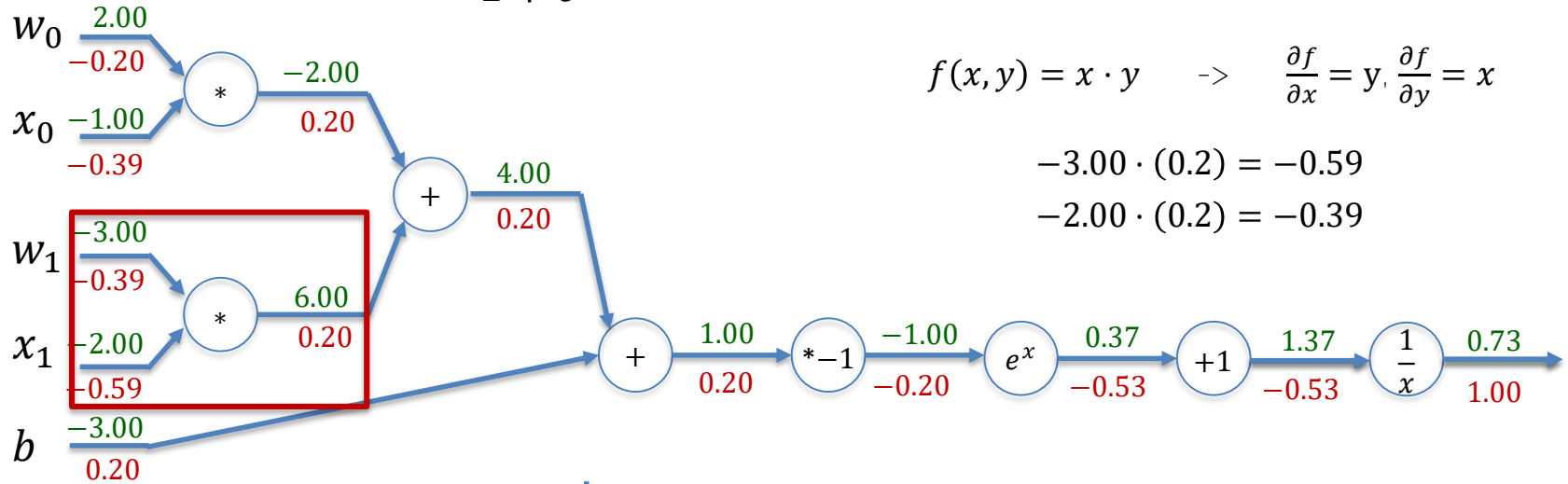
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Backprop

$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$f(x, y) = x \cdot y \quad \rightarrow \quad \frac{\partial f}{\partial x} = y, \quad \frac{\partial f}{\partial y} = x$$

$$-3.00 \cdot (0.2) = -0.59$$

$$-2.00 \cdot (0.2) = -0.39$$

$$f(x) = e^x \quad \rightarrow \quad \frac{\partial f}{\partial x} = e^x$$

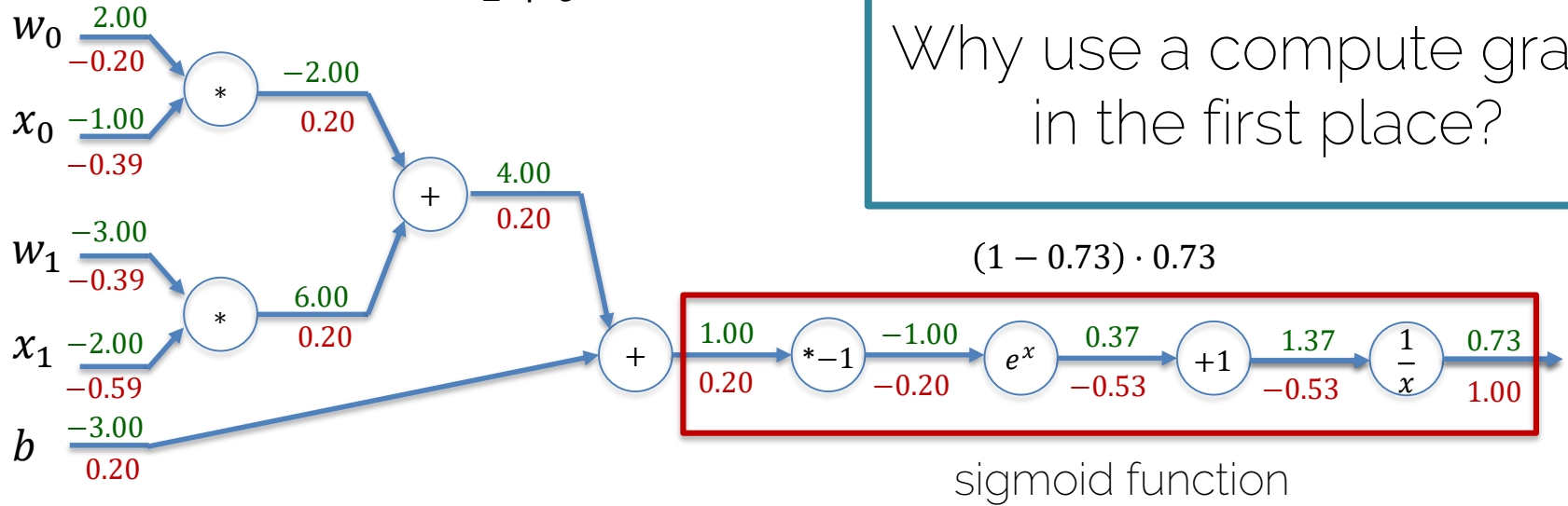
$$f(x) = \frac{1}{x} \quad \rightarrow \quad \frac{\partial f}{\partial x} = -\frac{1}{x^2}$$

$$f_a(x) = ax \quad \rightarrow \quad \frac{\partial f_a}{\partial x} = a$$

$$f_c(x) = c + x \quad \rightarrow \quad \frac{\partial f_c}{\partial x} = 1$$

Backprop

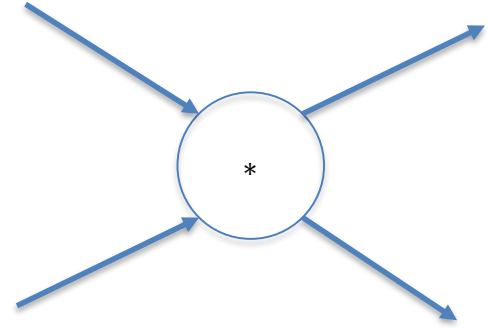
$$f(w_0, x_0, w_1, x_1, b) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + b)}}$$



$$\sigma(x) = \frac{1}{1+e^{-x}} \rightarrow \frac{\partial \sigma(x)}{\partial x} = \frac{e^{-x}}{(1+e^{-x})^2} = (1 - \sigma(x))\sigma(x)$$

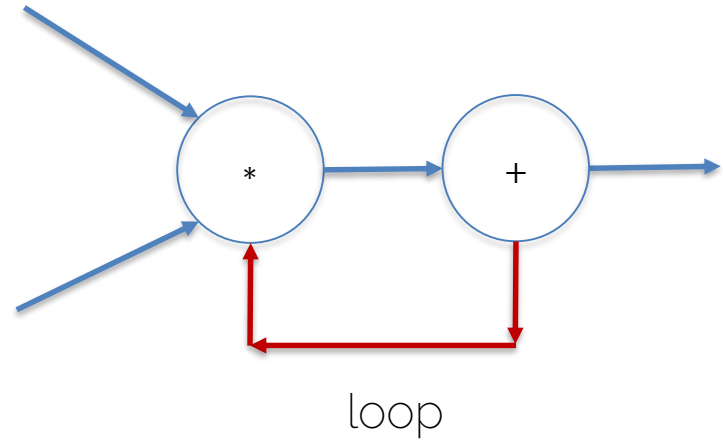
Backpropagation

What happens if there are multiple outputs in a compute node?

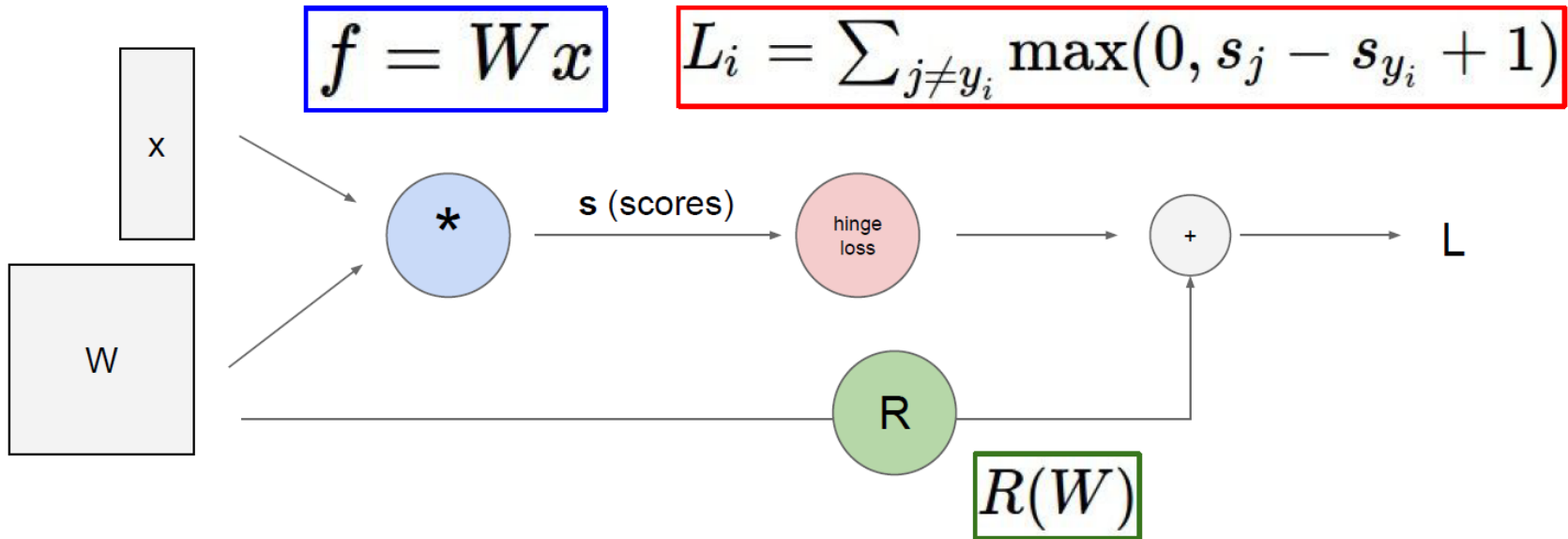


Backpropagation

What happens if there are loops in the graph?

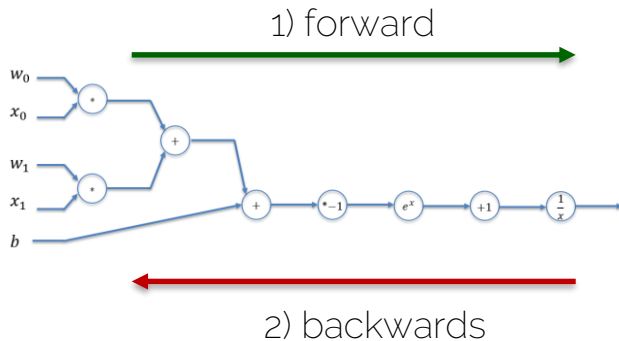


Computational Graph



Combining nodes:
Linear activation node + hinge loss + regularization

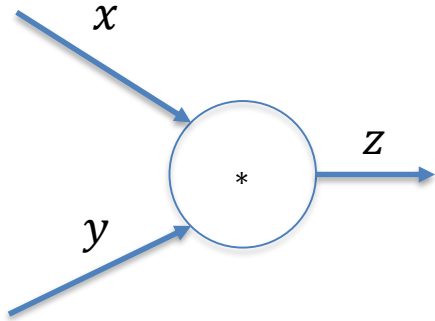
Implementation of Compute Graph



```
class ComputationalGraph(object):  
    #...  
    def forward(inputs):  
        #1. [pass inputs to input nodes]  
        #2. forward traverse the computational graph  
        for node in self.graph.nodes_topologically_sorted():  
            node.forward()  
            # forward intermediates / loss  
        return loss # final node returns loss  
    def backward():  
        for node in self.graph.nodes_topologically_sorted_reverse():  
            node.backward() #apply chainrule  
            # backward intermediate derivatives  
        return inputs_gradients
```

Implementation of Nodes

- Forward and backward pass of MulNode



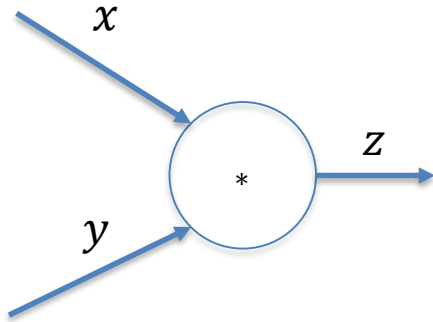
all values are scalars

```
class MulNode(object):  
    def forward(x,y):  
        z=x*y  
        return z  
    def backward(dz, x, y):  
        dx = y*dz # [dz/dx * dL/dz]  
        dy = x*dz # [dz/dy * dL/dz]  
        return [dx, dy]
```

Issue?

Implementation of Nodes

- Forward and backward pass of MulNode



all values are scalars

```
class MulNode(object):
    def forward(x,y):
        z = x*y
        self.x = x
        self.y = y
        return z
    def backward(dz):
        dx = self.y*dz # [dz/dx * dL/dz]
        dy = self.x*dz # [dz/dy * dL/dz]
        return [dx, dy]
```

Cache results of forward pass
-> faster runtime for backward pass

Torch: Layers (GitHub)

LayerNormalization.lua	Adding Layer Normalization	2 months ago
LeakyReLU.lua	Add THNN conversion of {ELU, LeakyReLU, LogSigmoid, LogSoftMax, Looku...	a year ago
Linear.lua	Fix shared function override for specific modules	4 months ago
Log.lua	add nn.Inc & nn.Scale	a year ago
LogSigmoid.lua	lazy init	a year ago
LogSoftMax.lua	Add THNN conversion of {ELU, LeakyReLU, LogSigmoid, LogSoftMax, Looku...	a year ago
LookupTable.lua	Fix shared function override for specific modules	4 months ago
MM.lua		
MSECriterion.lua		
MV.lua		
MapTable.lua		
MarginCriterion.lua		
MarginRankingCriterion.lua		
MaskedSelect.lua		
Max.lua		
Maxout.lua		
Mean.lua		
Min.lua		
MixtureTable.lua		
Module.lua		
Mul.lua		
MulConstant.lua		
MultiCriterion.lua		
Reshape.lua	Better __tostring__ and cleans formatting	a year ago
Select.lua	Adds negative dim arguments	11 months ago
SelectTable.lua	allow SelectTable to accept input that contains tables of things that...	2 months ago
Sequential.lua	Improve error handling	a year ago
Sigmoid.lua	Add THNN conversion of {RReLU, Sigmoid, SmoothL1Criterion,SoftMax, So...	a year ago
SmoothL1Criterion.lua	Add THNN conversion of {RReLU, Sigmoid, SmoothL1Criterion,SoftMax, So...	a year ago
SoftMarginCriterion.lua	SoftMarginCriterion	a year ago
SoftMax.lua	Add THNN conversion of {RReLU, Sigmoid, SmoothL1Criterion,SoftMax, So...	a year ago
SoftMin.lua	nn.clearState	a year ago
SoftPlus.lua	Add THNN conversion of {RReLU, Sigmoid, SmoothL1Criterion,SoftMax, So...	a year ago
SoftShrink.lua	Add THNN conversion of {oftShrink, Sqrt, Square, Tanh, Threshold}	a year ago
SoftSign.lua	nn.clearState	a year ago
SparseJacobian.lua	Fix various unused variables in nn	3 years ago
SparseLinear.lua	Fixing sparse linear race condition	a year ago
SpatialAdaptiveAveragePooling.lua	Add SpatialAdaptiveAveragePooling.	4 months ago
SpatialAdaptiveMaxPooling.lua	Indices for nn.	7 months ago
SpatialAutoCropMSECriterion.lua	fix local / global var leaks	4 months ago

Torch: MulConstant

```
1 local MulConstant, parent = torch.class('nn.MulConstant', 'nn.Module')
2
3 function MulConstant:__init(constant_scalar,ip)
4     parent.__init(self)
5     assert(type(constant_scalar) == 'number', 'input is not scalar!')
6     self.constant_scalar = constant_scalar
7
8     -- default for inplace is false
9     self.inplace = ip or false
10    if (ip and type(ip) ~= 'boolean') then
11        error('in-place flag must be boolean')
12    end
13 end
```

Init()

```
15 function MulConstant:updateOutput(input)
16     if self.inplace then
17         input:mul(self.constant_scalar)
18         self.output:set(input)
19     else
20         self.output:resizeAs(input)
21         self.output:copy(input)
22         self.output:mul(self.constant_scalar)
23     end
24     return self.output
25 end
```

Forward()

$$f(x) = aX$$

```
27 function MulConstant:updateGradInput(input, gradOutput)
28     if self.gradInput then
29         if self.inplace then
30             gradOutput:mul(self.constant_scalar)
31             self.gradInput:set(gradOutput)
32             -- restore previous input value
33             input:div(self.constant_scalar)
34         else
35             self.gradInput:resizeAs(gradOutput)
36             self.gradInput:copy(gradOutput)
37             self.gradInput:mul(self.constant_scalar)
38         end
39         return self.gradInput
40     end
41 end
```

Backward()

Caffee: Layers (GitHub)

absval_layer.cpp	dismantle layer headers	2 years ago
absval_layer.cu	dismantle layer headers	2 years ago
accuracy_layer.cpp		
argmax_layer.cpp		
base_conv_layer.cpp		
base_data_layer.cpp		
base_data_layer.cu		
batch_norm_layer.cpp		
batch_norm_layer.cu		
batch_reindex_layer.cpp		
batch_reindex_layer.cu		
bnll_layer.cpp		
bnll_layer.cu		
concat_layer.cpp		
concat_layer.cu		
contrastive_loss_layer.cpp		
contrastive_loss_layer.cu		
conv_layer.cpp		
conv_layer.cu		
cudnn_conv_layer.cpp		
cudnn_conv_layer.cu		
cudnn_lcn_layer.cpp		
cudnn_lcn_layer.cu		
cudnn_lm_layer.cpp		
cudnn_lm_layer.cu		
cudnn_pooling_layer.cpp		
cudnn_pooling_layer.cu		
cudnn_relu_layer.cpp		
cudnn_relu_layer.cu		
cudnn_sigmoid_layer.cpp		
cudnn_sigmoid_layer.cu		
cudnn_softmax_layer.cpp		
cudnn_softmax_layer.cu		
cudnn_tanh_layer.cpp		
pooling_layer.cpp	dismantle layer headers	2 years ago
pooling_layer.cu	dismantle layer headers	2 years ago
power_layer.cpp	dismantle layer headers	2 years ago
power_layer.cu	dismantle layer headers	2 years ago
prelu_layer.cpp	dismantle layer headers	2 years ago
prelu_layer.cu	dismantle layer headers	2 years ago
reduction_layer.cpp	dismantle layer headers	2 years ago
reduction_layer.cu	dismantle layer headers	2 years ago
relu_layer.cpp	dismantle layer headers	2 years ago
relu_layer.cu	dismantle layer headers	2 years ago
reshape_layer.cpp	dismantle layer headers	2 years ago
sigmoid_cross_entropy_loss_layer.cpp	dismantle layer headers	2 years ago
sigmoid_cross_entropy_loss_layer.cu	dismantle layer headers	2 years ago
sigmoid_layer.cpp	dismantle layer headers	2 years ago
sigmoid_layer.cu	dismantle layer headers	2 years ago
silence_layer.cpp	dismantle layer headers	2 years ago
silence_layer.cu	dismantle layer headers	2 years ago
slice_layer.cpp	dismantle layer headers	2 years ago

Caffe: Sigmoid_Layer

```
5 #include "caffe/layers/sigmoid_layer.hpp"
6 namespace caffe {
7
8 template <typename Dtype>
9 inline Dtype sigmoid(Dtype x) {
10     return 1. / (1. + exp(-x));
11 }
12
```

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

```
13 template <typename Dtype>
14 void SigmoidLayer<Dtype>::Forward_cpu(const vector<Blob<Dtype>*>& bottom,
15     const vector<Blob<Dtype>*>& top) {
16     const Dtype* bottom_data = bottom[0]->cpu_data();
17     Dtype* top_data = top[0]->mutable_cpu_data();
18     const int count = bottom[0]->count();
19     for (int i = 0; i < count; ++i) {
20         top_data[i] = sigmoid(bottom_data[i]);
21     }
22 }
23
```

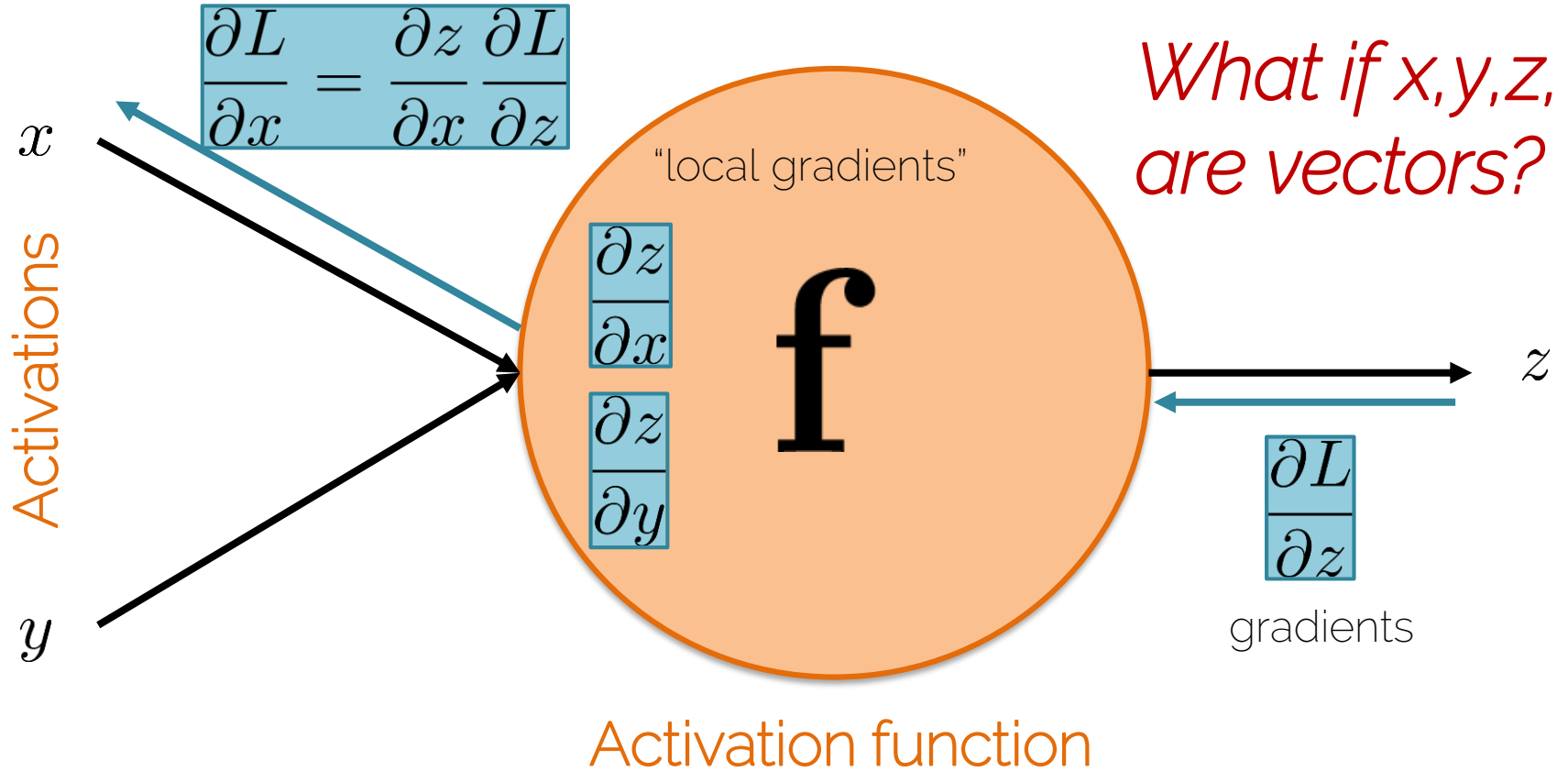
Forward()

```
24 template <typename Dtype>
25 void SigmoidLayer<Dtype>::Backward_cpu(const vector<Blob<Dtype>*>& top,
26     const vector<bool>& propagate_down,
27     const vector<Blob<Dtype>*>& bottom) {
28     if (propagate_down[0]) {
29         const Dtype* top_data = top[0]->cpu_data();
30         const Dtype* top_diff = top[0]->cpu_diff();
31         Dtype* bottom_diff = bottom[0]->mutable_cpu_diff();
32         const int count = bottom[0]->count();
33         for (int i = 0; i < count; ++i) {
34             const Dtype sigmoid_x = top_data[i];
35             bottom_diff[i] = top_diff[i] * sigmoid_x * (1. - sigmoid_x);
36         }
37     }
38 }
39
```

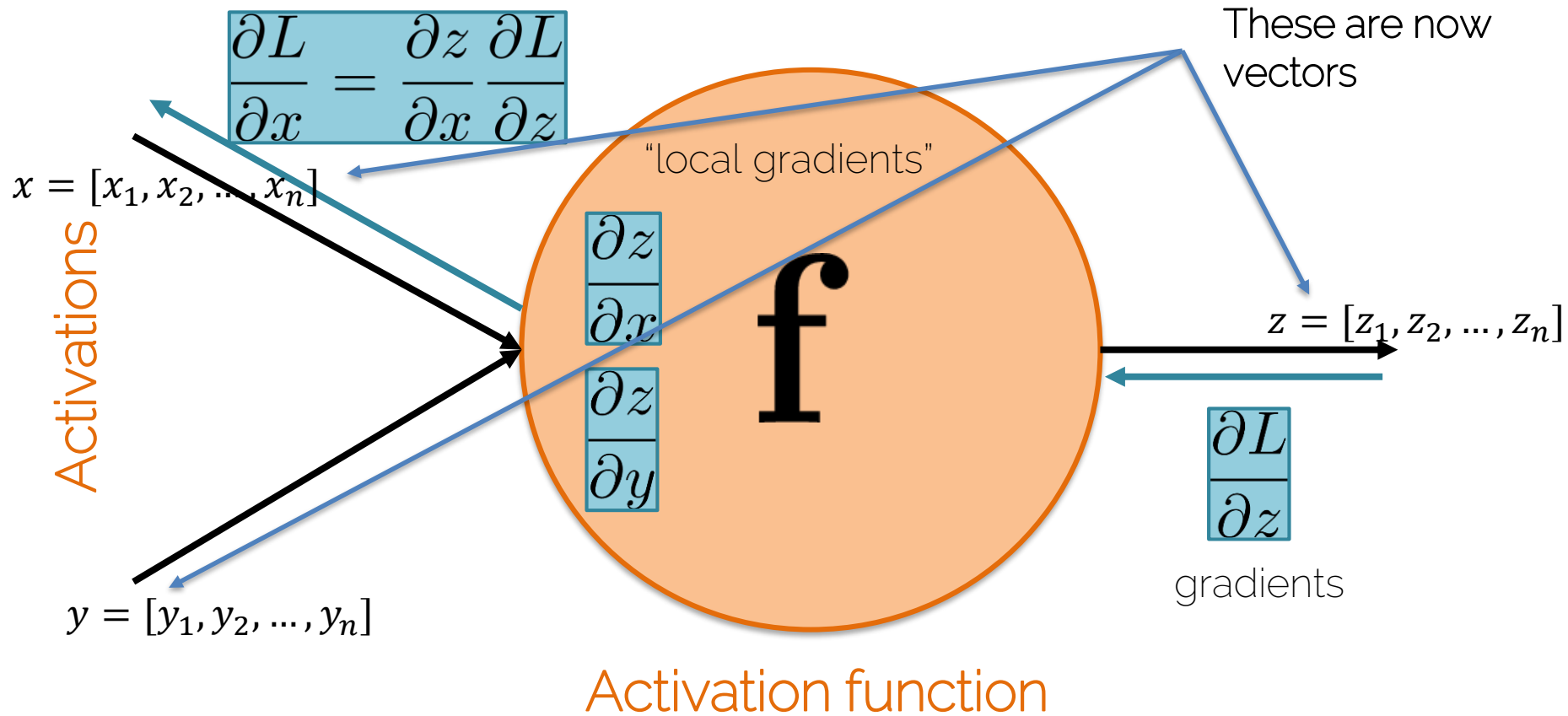
Backward()

$$\sigma'(x) = (1 - \sigma(x))\sigma(x)$$

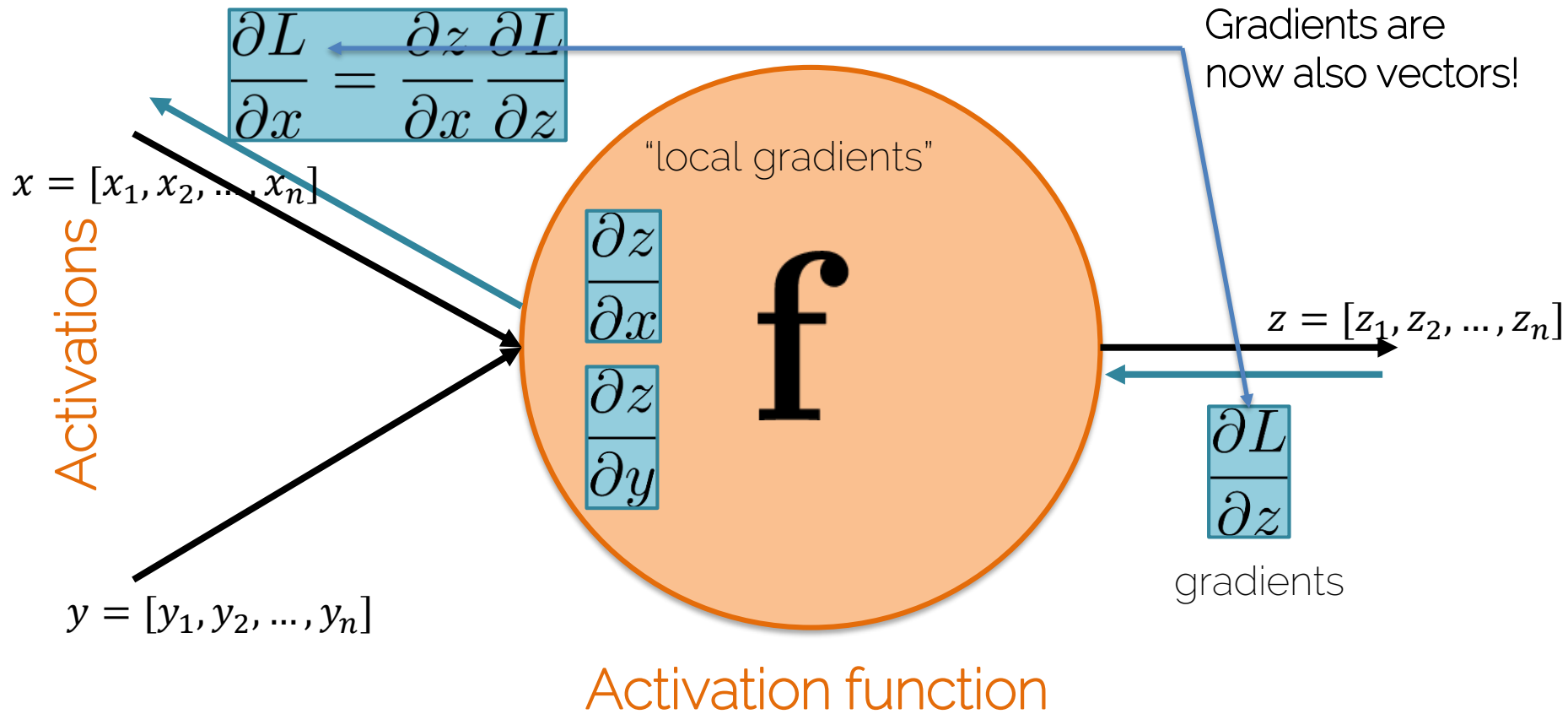
Vectorized Operations



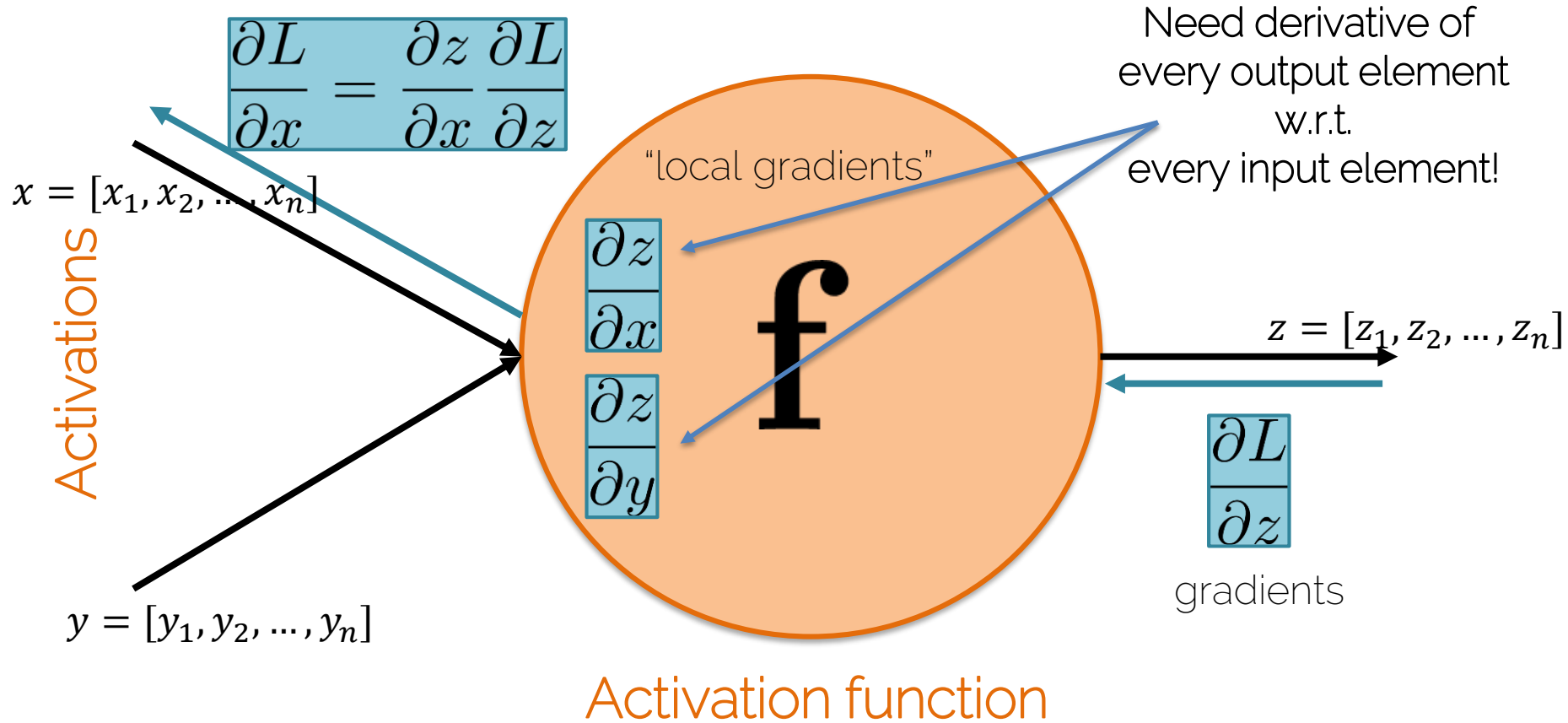
Vectorized Operations



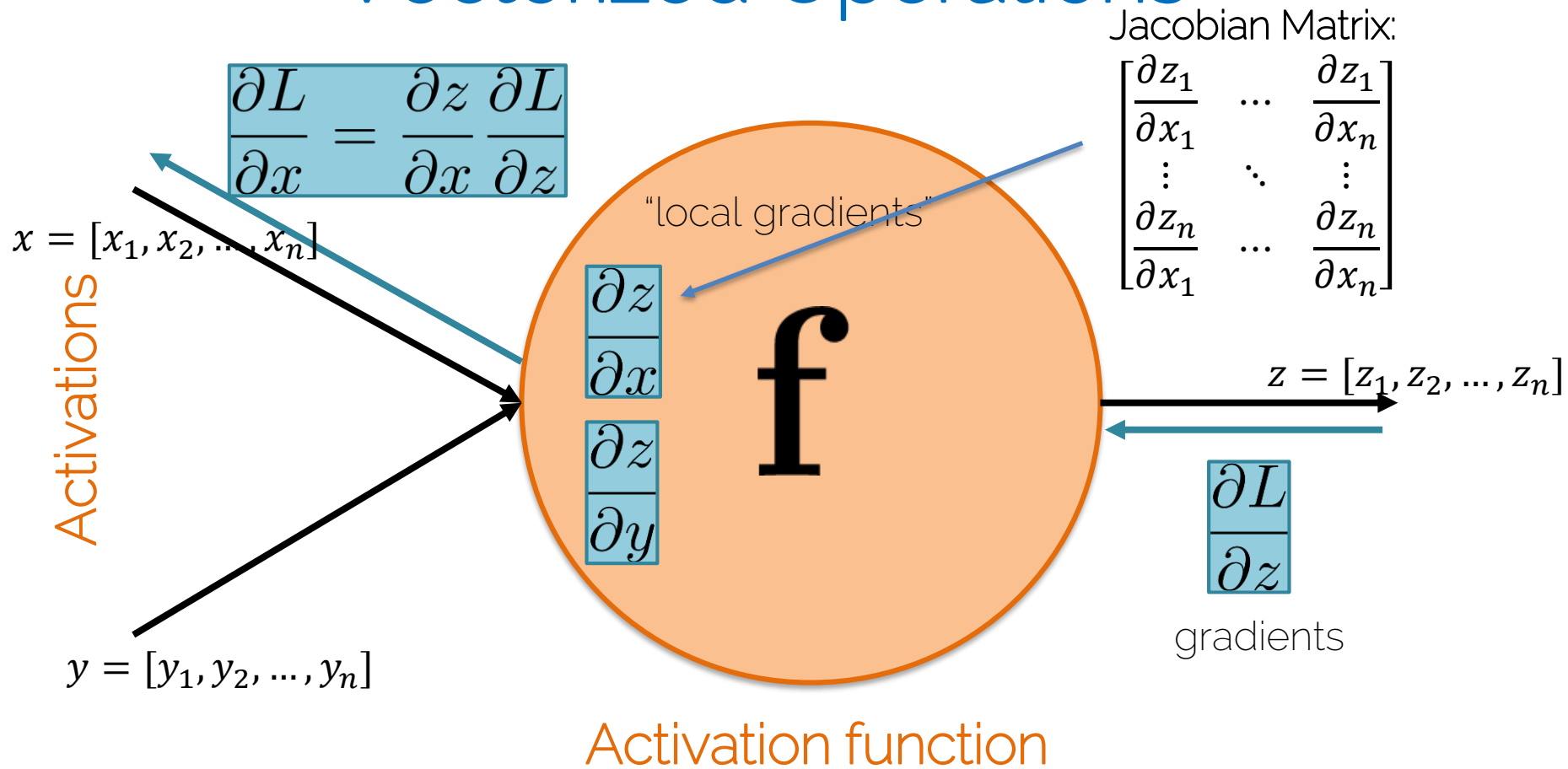
Vectorized Operations



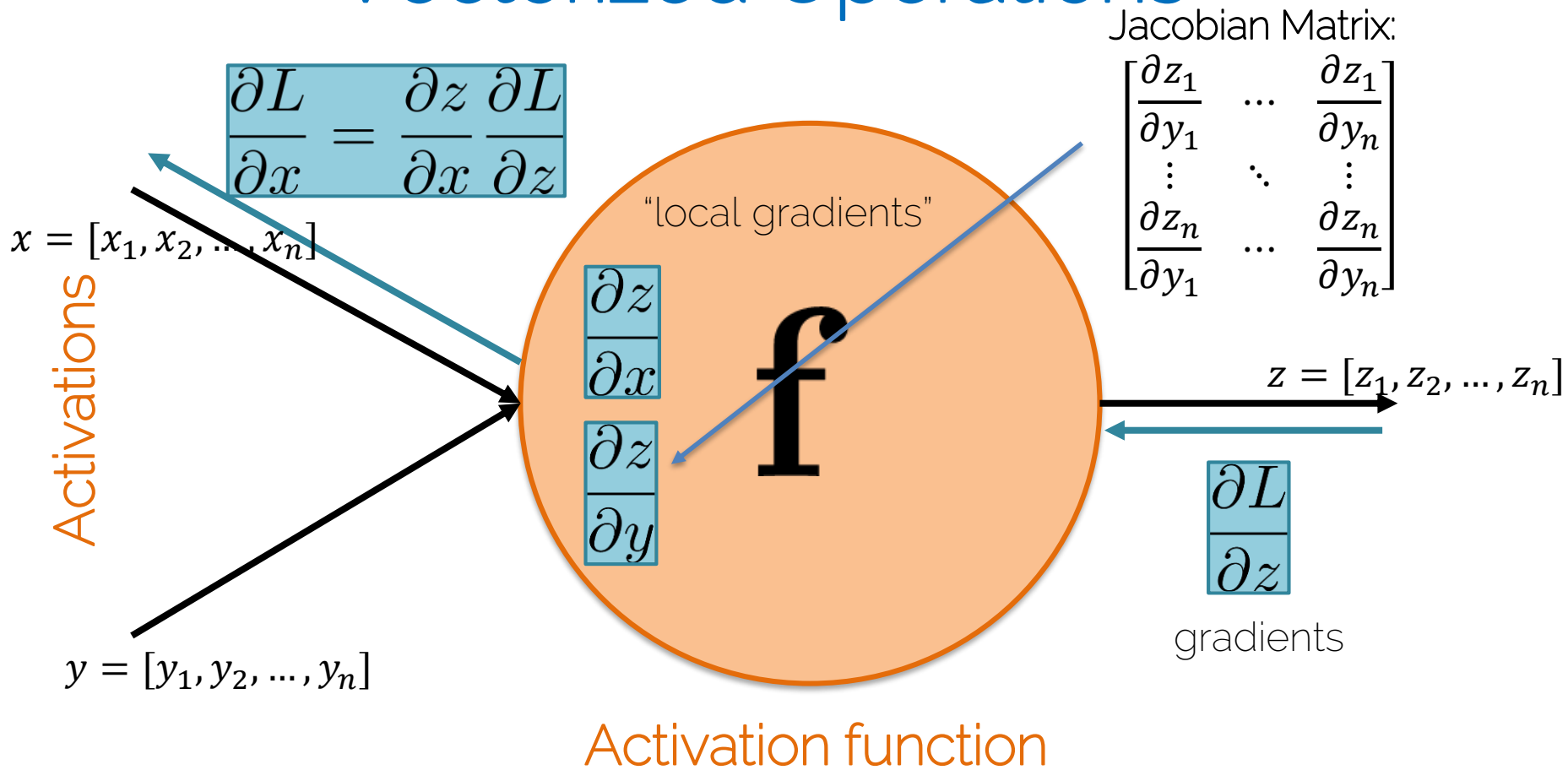
Vectorized Operations



Vectorized Operations



Vectorized Operations



Vectorized Operations

Assuming input and output $\in \mathbb{R}^{4096}$

Jacobian Matrix:

$$\begin{bmatrix} \frac{\partial z_1}{\partial y_1} & \dots & \frac{\partial z_1}{\partial y_n} \\ \frac{\partial z_2}{\partial y_1} & \dots & \frac{\partial z_2}{\partial y_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial z_n}{\partial y_1} & \dots & \frac{\partial z_n}{\partial y_n} \end{bmatrix}$$

$$x = [x_1, x_2, \dots, x_n]$$

$$x \in \mathbb{R}^{4096}$$

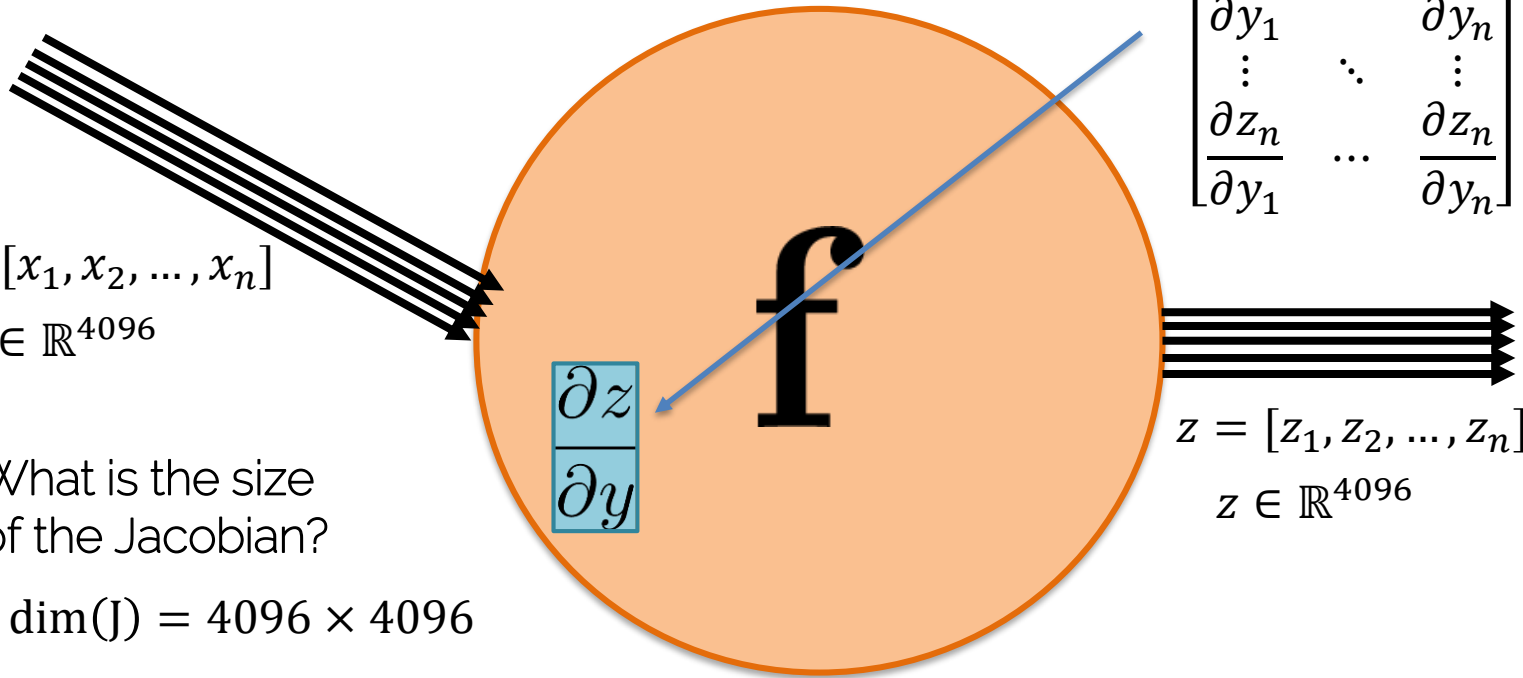
What is the size
of the Jacobian?

$$\dim(J) = 4096 \times 4096$$

$$\begin{bmatrix} \partial z \\ \partial y \end{bmatrix}$$

$$z = [z_1, z_2, \dots, z_n]$$

$$z \in \mathbb{R}^{4096}$$



Vectorized Operations

How efficient is that:

- $\dim(\mathbf{J}) = 4096 \times 4096 = 16.78 \text{ mio}$
- Assuming floats (i.e., 4 bytes / elem)
- $\rightarrow 64 \text{ MB}$

Typically, networks are run in batches:

- Assuming mini-batch size of 16
- $\rightarrow \dim(\mathbf{J}) = (16 \cdot 4096) \times (16 \cdot 4096) = 4295 \text{ mio}$
- $\rightarrow 16.384 \text{ MB} = 16 \text{ GB}$

Jacobian Matrix:

$$\begin{bmatrix} \frac{\partial z_1}{\partial y_1} & \dots & \frac{\partial z_1}{\partial y_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial z_n}{\partial y_1} & \dots & \frac{\partial z_n}{\partial y_n} \end{bmatrix}$$

How to handle this?

Administrative Things

- Slides available on this website

<http://vision.in.tum.de/teaching/ws2017/dl4cv/coursematerial>

- Password: DL4CVws17
- Please do not distribute!

Administrative Things

- First tutorial on November 2nd
 - Introduction to exam system
- Next Lecture on November 7th
 - Optimization and Regularization
 - More on neural networks 😊
- No tutorial this week!
- No more lecture this week!
- October 31st is Halloween (also Day of Reformation)
- Tentative date for the exam: **13th of February**

See you next week!