

Computer Vision Group Prof. Daniel Cremers



Robotic 3D Vision

Lecture 18: Dense Stereo Reconstruction

WS 2020/21 Dr. Niclas Zeller Artisense GmbH

What We Will Cover Today

- Stereo Rectification
- Dense Depth Reconstruction from Two and Multiple Views
 - Dense Correspondence Search
 - Regularization
- Depth Sensors
 - Structured light
 - Time-of-flight

Stereo Perception

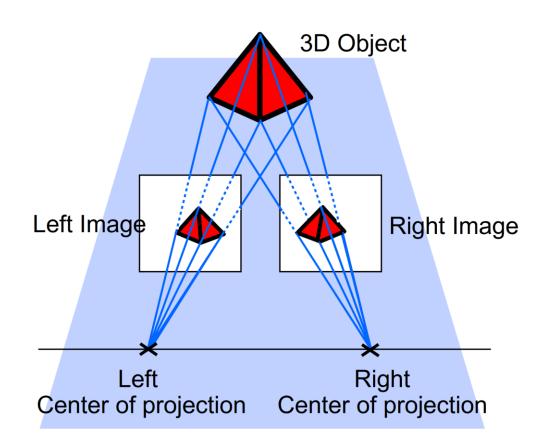


Image credit: D. Scaramuzza

Dense Depth from Two Views

- So far: triangulation of corresponding interest points between two images to find depth
- How can we obtain depth densely for all pixels in an image?
- Assume relative pose between the camera images known
- Assume intrinsic camera calibration known



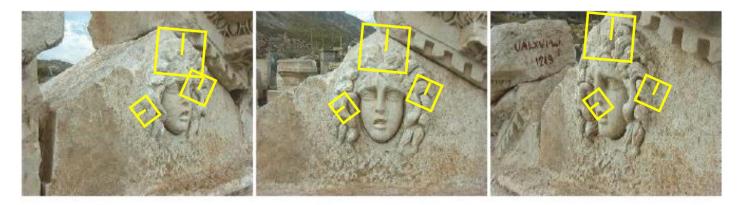






Image source: Scharstein et al., Middlebury stereo benchmark

Sparse 3D Reconstruction



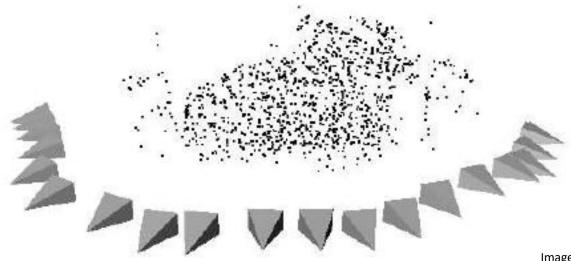
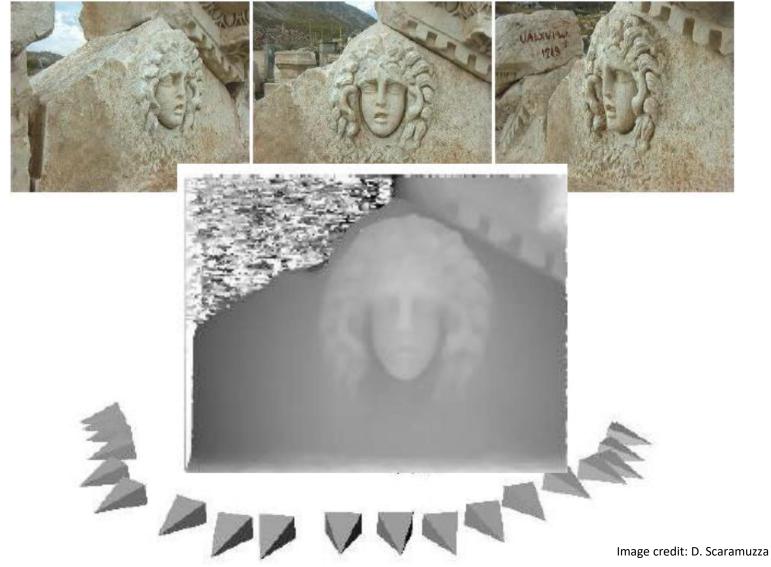
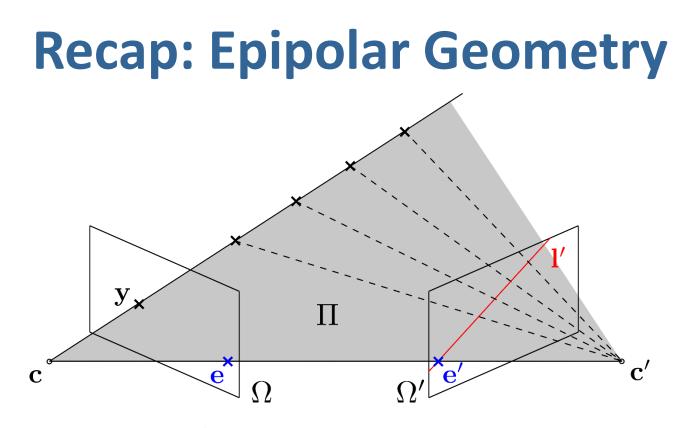


Image credit: D. Scaramuzza Dr. Niclas Zeller, Artisense GmbH

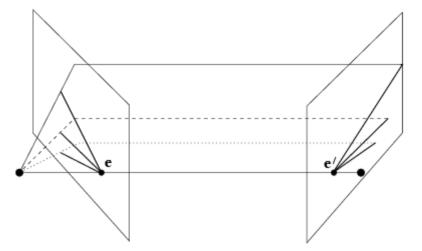
Dense 3D Reconstruction





- Camera centers ${f c}$, ${f c}'$ and image point ${f y}\in\Omega$ span the epipolar plane Π
- The ray from camera center c through point y projects as the epipolar line l' in image plane Ω'
- The intersections of the line through the camera centers with the image planes are called epipoles e , e^\prime

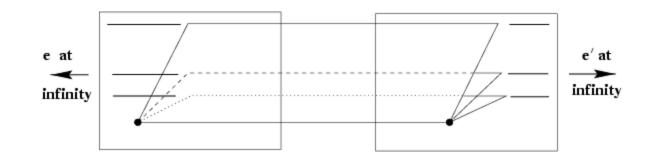
Epipolar Lines, Converging Cameras

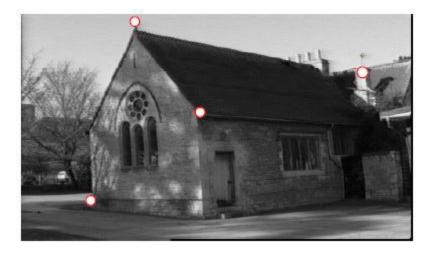


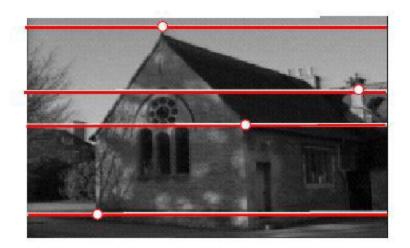




Epipolar Lines, Parallel Cameras

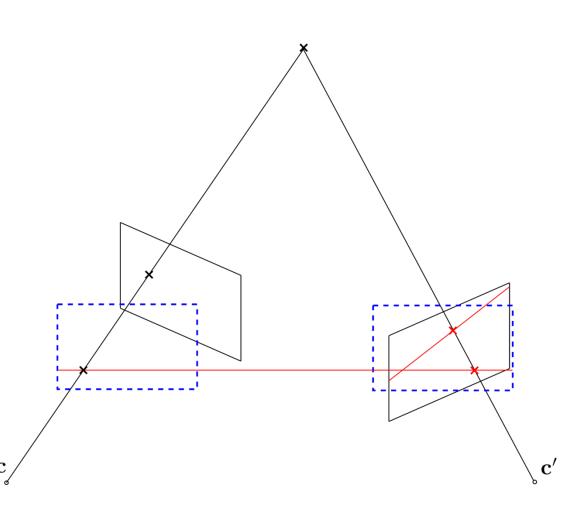


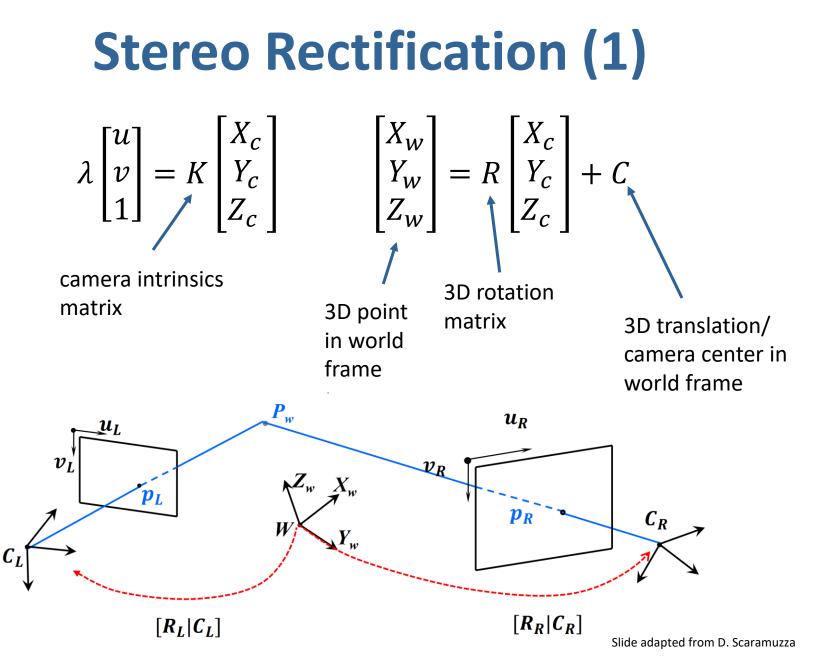




Stereo Image Rectification

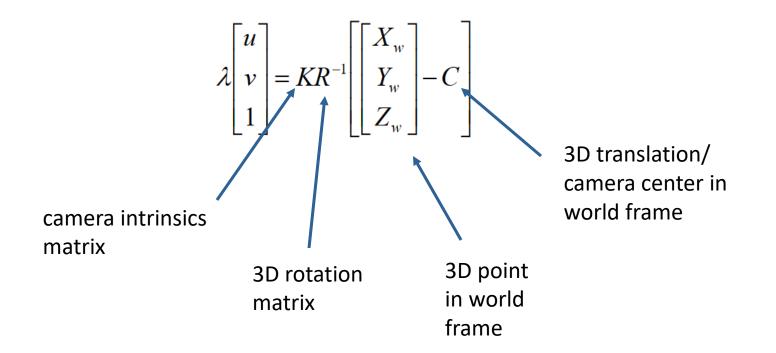
- Correspondence search is simplified, if epipolar lines are horizontal (or vertical)
- Idea: Rectify images
 - warp the images onto a common image plane
 - only horizontal or vertical translation between the "new" camera frames
 - Equal intrinsics





Stereo Rectification (1)

 In the following for convenience, we will write the perspective projection of a 3D point expressed in the world frame into the camera frame as

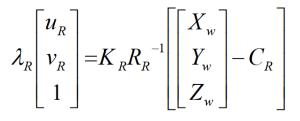


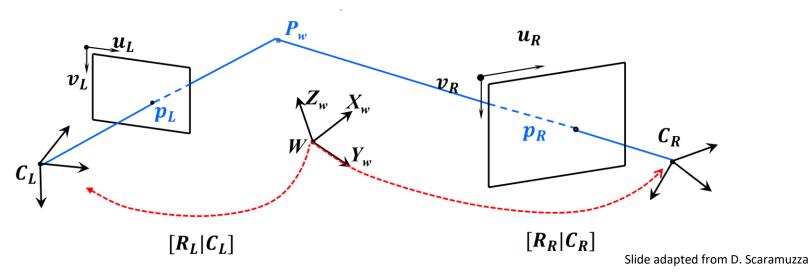
Stereo Rectification (2)

Left camera projection:

Right camera projection:

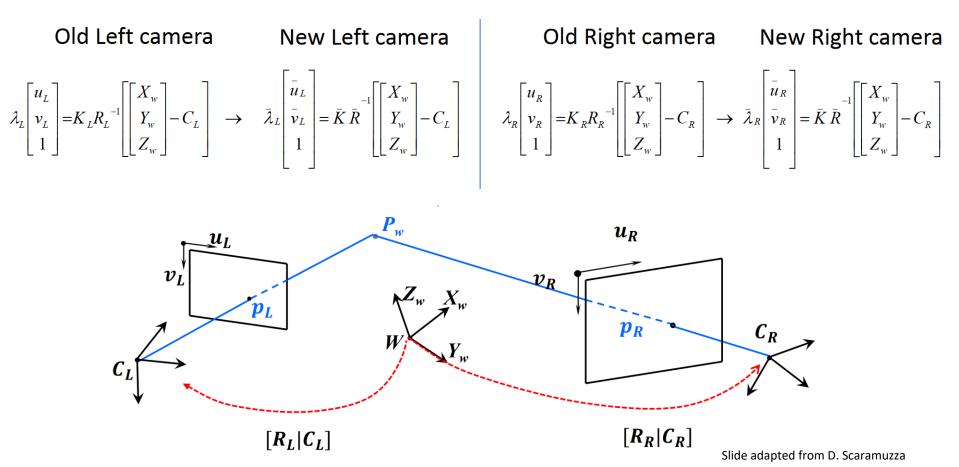
$$\lambda_{L} \begin{bmatrix} u_{L} \\ v_{L} \\ 1 \end{bmatrix} = K_{L} R_{L}^{-1} \begin{bmatrix} X_{w} \\ Y_{w} \\ Z_{w} \end{bmatrix} - C_{L}$$





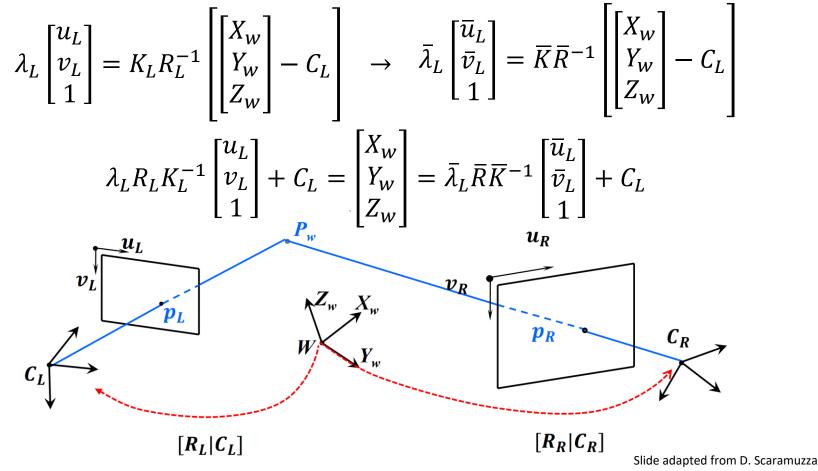
Stereo Rectification (3)

Goal: warp left and right images such that image planes coplanar and intrinsics are equal



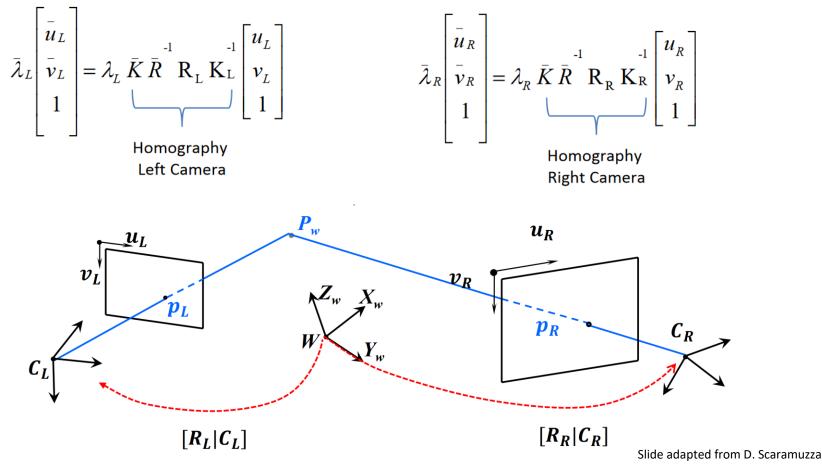
Stereo Rectification (3)

Solving for 3D point for each camera yields homographies Left camera:



Stereo Rectification (4)

Solving for 3D point for each camera yields homographies



Stereo Rectification (5)

- How to choose the new intrinsics and rotation ?
- Fusiello et al., A Compact Algorithm for Rectification of Stereo Pairs, Mach. Vision and Appl. 1999

• Choose
$$\overline{K} = (K_L + K_R)/2$$

$$\overline{R} = [\overline{r_1}, \overline{r_2}, \overline{r_3}]$$

where

 $\overline{r_1} = \frac{C_R - C_L}{\|C_R - C_L\|} \qquad \begin{array}{l} \text{Vector } C_R - C_L \text{ is supposed to be aligned with} \\ \text{the x-axis of the camera coordinate frame} \\ \overline{r_2} = r_3 \times \overline{r_1} \quad \text{, where } r_3 \text{ is the } 3^{\text{rd}} \text{ column of the rotation matrix of the left camera, i.e., } R_L \\ \overline{r_3} = \overline{r_1} \times \overline{r_2} \end{array}$

Slide adapted from D. Scaramuzza

Stereo Rectification Example

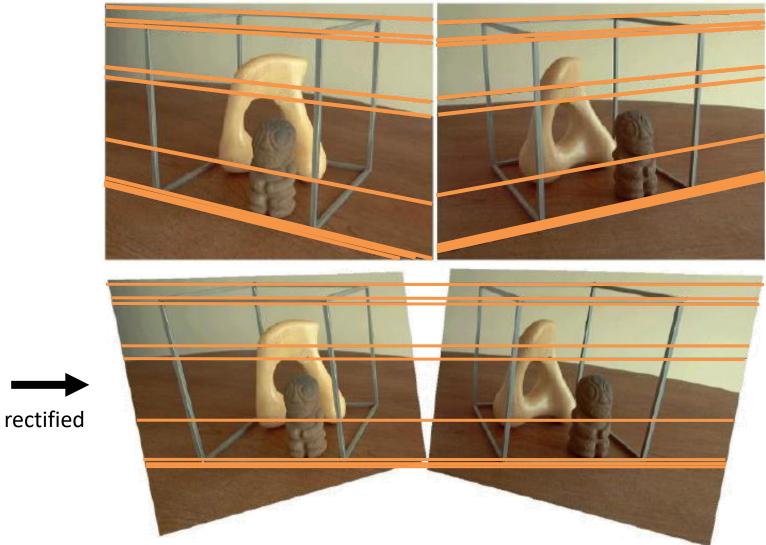
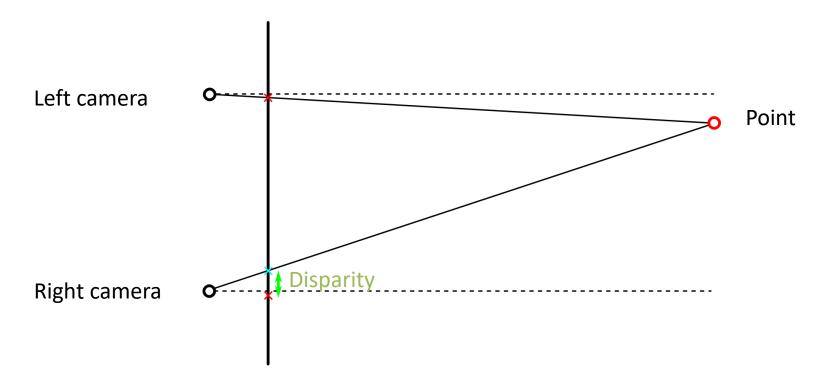


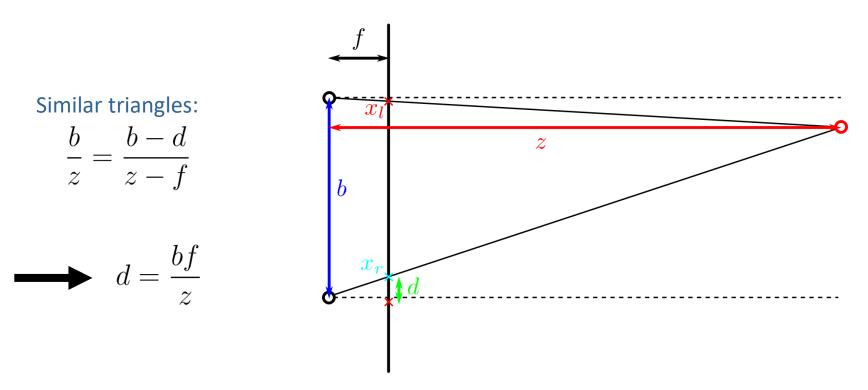
Image source: Loop and Zhang, 2001

Disparity

- Assume rectified stereo images
- Disparity: (horizontal) pixel difference of corresponding pixels between the two images

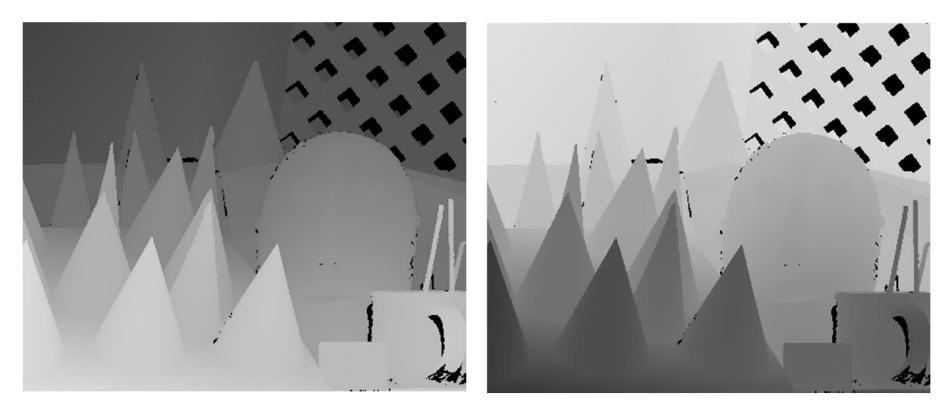


Relation of Disparity and Depth



- Disparity is inverse proportional to depth:
 - The larger the depth, the smaller the disparity
- Disparity is proportional to the baseline:
 - The larger the baseline, the larger the disparity
 - Larger baseline means also higher depth accuracy

Relation of Disparity and Depth

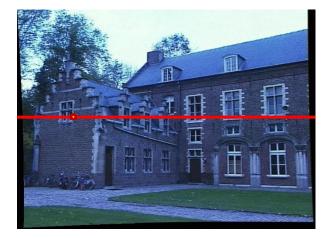


Disparity image

Depth image

Dense Stereo Depth Estimation

- For each pixel in left image:
 - Compare photoconsistency with every pixel on the corresponding epipolar line in the right image
 - Pick pixel with best similarity

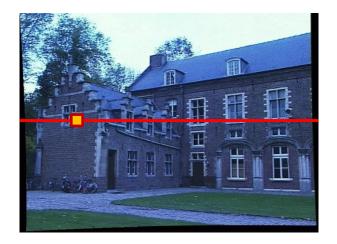


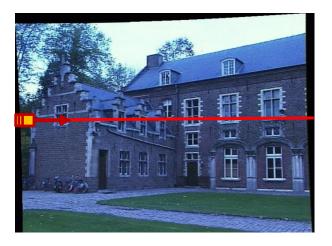


- Problems:
 - Noise
 - Intensity of a single pixel not very distinctive

Dense Stereo Depth Estimation

• Better idea: Compare patches (blocks)





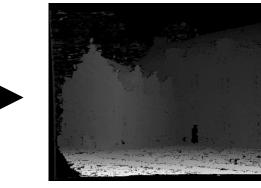
- New questions:
 - What are good patch correlation measures?
 - Patch size?
 - etc.

Block Matching Algorithm

- Input: Two images, intrinsics camera calibration, relative pose
- Output: Disparity image
- Algorithm:
 - Rectify images
 - For each pixel in left image:
 - Compute matching cost along epipolar line using patch comparison
 - Determine minimum in matching cost
 - with sub-pixel accuracy, e.g. using linear interpolation
 - Filter outliers







Patch Correlation Measures

• Sum-of-squared differences:

If we consider rectified left/right images we don't have to search along the y dimension $\Delta y = 0$

$$SSD(B, (\Delta x, \Delta y)) = \sum_{(x,y)\in B} \left(I^{l}(x,y) - I^{r}(x + \Delta x, y + \Delta y) \right)^{2}$$

• Sum-of-absolute differences:

$$SAD(B, (\Delta x, \Delta y)) = \sum_{(x,y)\in B} \left| I^l(x,y) - I^r(x + \Delta x, y + \Delta y) \right|$$

Less sensitive to outliers

Normalized Cross-Correlation:

$$\operatorname{NCC}(B, (\Delta x, \Delta y)) = \frac{\sum_{(x,y)\in B} I^{l}(x, y) I^{r}(x + \Delta x, y + \Delta y)}{\sqrt{\sum_{(x,y)\in B} I^{l}(x, y)^{2}} \sqrt{\sum_{(x,y)\in B} I^{r}(x + \Delta x, y + \Delta y)^{2}}}$$

Invariant to illumination changes

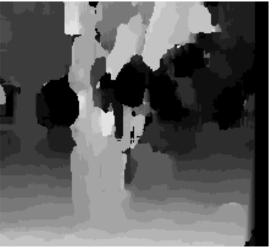
Block Size

- Common choices are 5x5, 11x11, ...
 - Smaller neighborhood: more details
 - Larger neighborhood: less noise
- Suppress pixels with low confidence (f.e. check ratio best match vs. second best match, examine local behavior of matching cost, etc.)





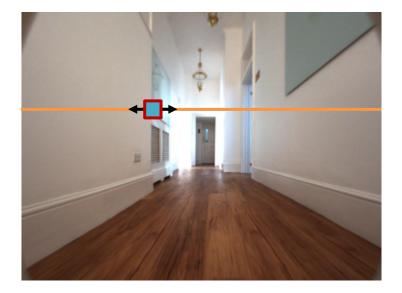
3x3 block-size



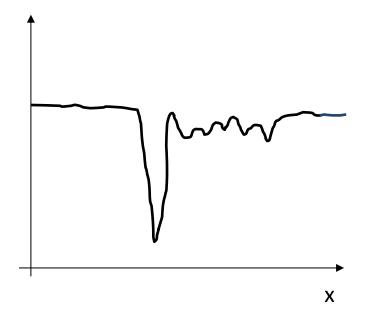
20x20 block-size

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Behavior of the Correspondence Measure

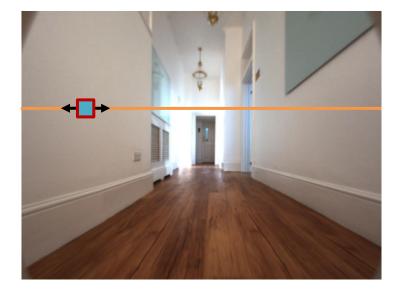


Matching cost

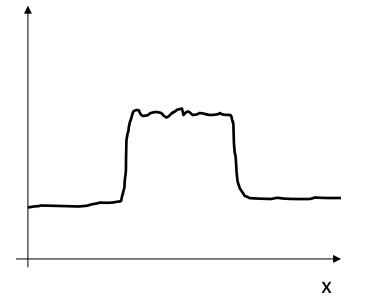


Images: Pinies et al., 2015

Behavior of the Correspondence Measure



Matching cost



Images: Pinies et al., 2015

Corresponding patches may differ !

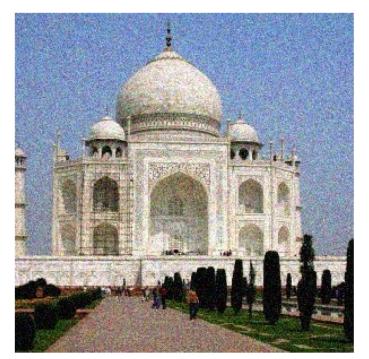


Image Noise (Camera-related)

Images: C. Gava

• Corresponding patches may differ !





Perspective Distortion (Viewpoint-related)

Images: R. Szeliski

• Corresponding patches may differ !





Occlusions (Viewpoint-related)

Images: Middlebury benchmark

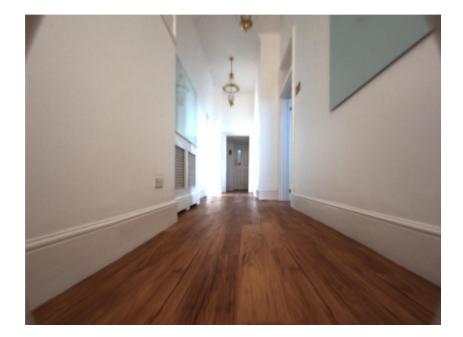
Corresponding patches may differ !



Specular Reflections (Viewpoint-related)

Images: Weinmann et al., ICCV 2013

• Correspondence can be ambiguous !



Low Texture (Scene-related)

Images: Pinies et al., 2015

• Correspondence can be ambiguous !



Repetitive Structure/Texture (Scene-related)

• Corresponding patches may differ !

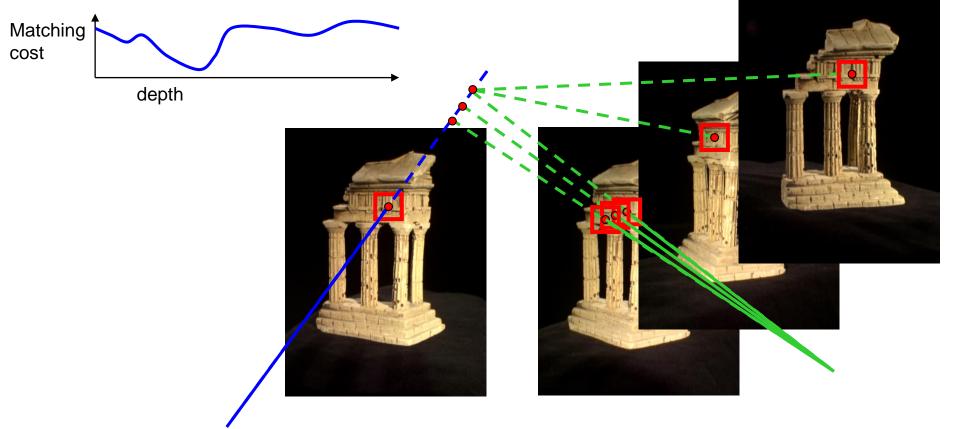


Motion blur (Scene-related)

Images: C. Gava

Dense Depth from Multiple Views

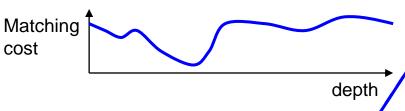
• Straightforward approach: extend two-view matching cost to sum over matching costs of an image towards multiple images



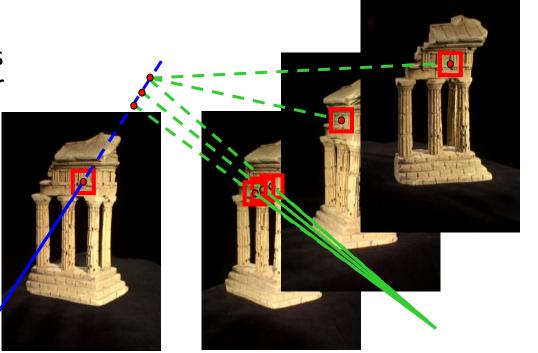
Slide adapted from R. Szeliski

Dense Depth from Multiple Views

- Straightforward approach: extend two-view matching cost to sum over matching costs of an image towards multiple images
- In general for multiple views images cannot be rectified anymore
- Disparity to depth relation is different for each image pair
- Matching cost is defined as a function of depth (or inv. depth)



Slide adapted from R. Szeliski

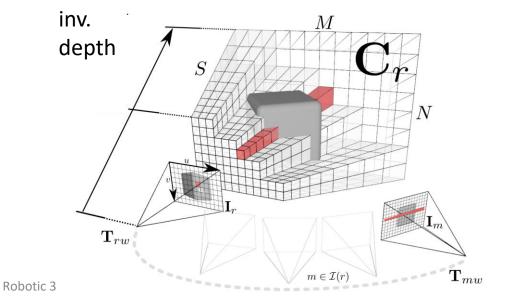


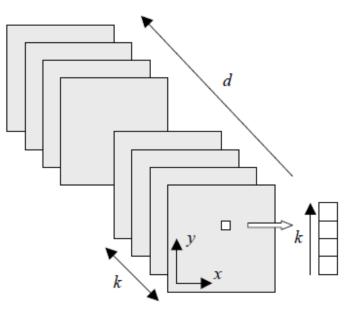
Disparity Space Image / Cost Volumes

 Sum of matching costs between reference and k images for discrete depth hypotheses in each pixel

$$C(\mathbf{y}, d) = \sum_{k} \rho(I_k(\omega(\mathbf{y}, d, \boldsymbol{\xi}_k)) - I_{ref}(\mathbf{y}))$$

Multi-view: inv. depth, "cost volume"

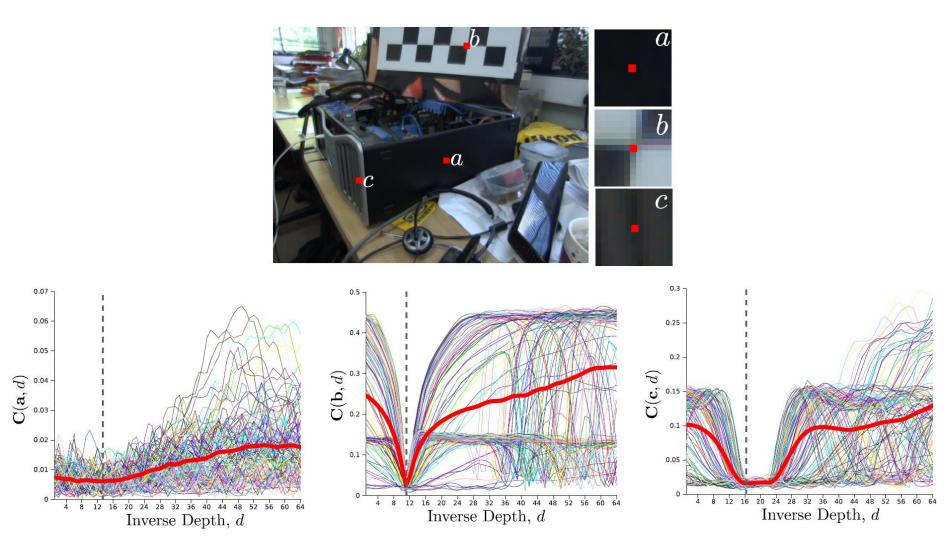




[Szeliski and Golland 1999]

Image from Newcombe et al., 2011 Dr. Niclas Zeller, Artisense GmbH

Multi-View Correspondence Measure

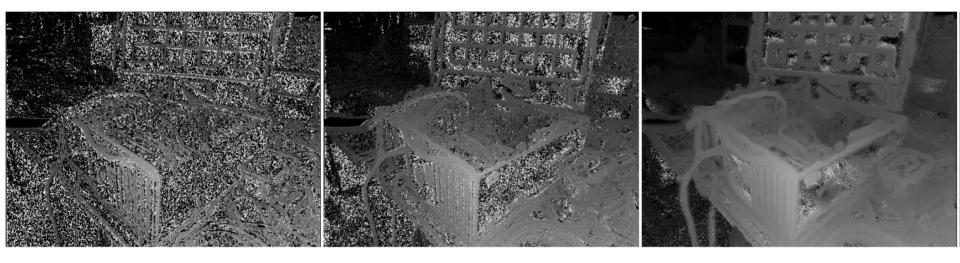


Images: R. Newcombe, 2014

Per-Pixel Max-Likelihood Solution

• Simply choosing the depth with best matching cost at each pixel may not provide a good solution

 $\operatorname{argmin}_d C(\mathbf{y}, d)$



2 comparison frames

10 comparison frames

30 comparison frames

• Quite some noise in regions with little texture

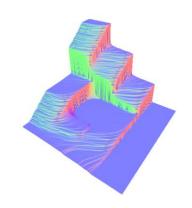
Regularization

- Neighboring pixels should not be treated independently from each others
- How can we incorporate prior knowledge about the observed 3D structures such as smoothness or planarity?
- Idea: add regularizing prior term to the optimization problem

Support Support the second state of the sec

$$E(u) = \int_{\mathbf{y}\in\Omega} \|u(\mathbf{y}) - z(\mathbf{y})\|_1 \, d\mathbf{y} + \lambda \, \int_{\mathbf{y}\in\Omega} \|\nabla u(\mathbf{y})\|_1 \, d\mathbf{y}$$

Staircasing!

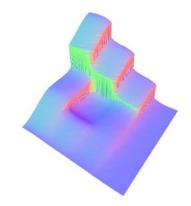


Images: R. Newcombe, 2014

Smoothness Regularizers

 Huber-norm regularizer as a trade-off between quadratic and L1

$$E(u) = \int_{\mathbf{y}\in\Omega} \|u(\mathbf{y}) - z(\mathbf{y})\|_{\delta_{\mathcal{F}}} \, d\mathbf{y} + \lambda \, \int_{\mathbf{y}\in\Omega} \|\nabla u(\mathbf{y})\|_{\delta_{\mathcal{R}}} \, d\mathbf{y}$$

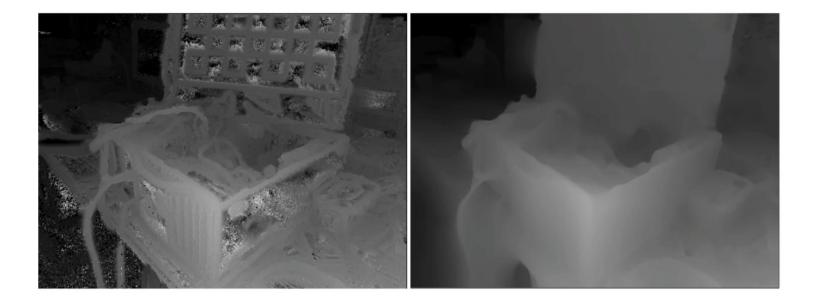


- Optimization is quite complex
 - There exist also discrete approximations
 - E.g. Semi-Global Matching

Images: R. Newcombe, 2014

Effect of Regularization

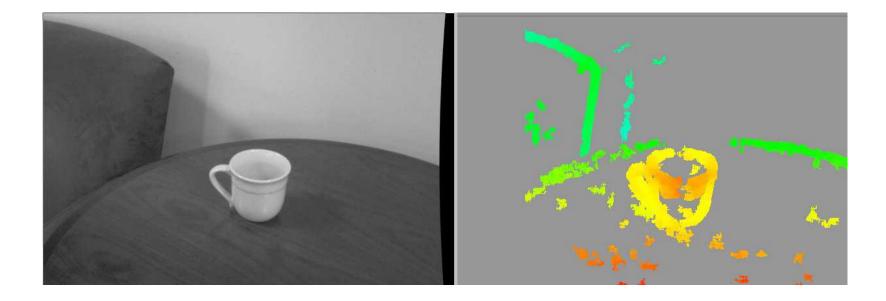
Data term: cost volume over L1-norm on photometric residuals Regularizer: Huber-norm on inverse depth gradient



Images: R. Newcombe et al., 2011

Active Depth Sensing

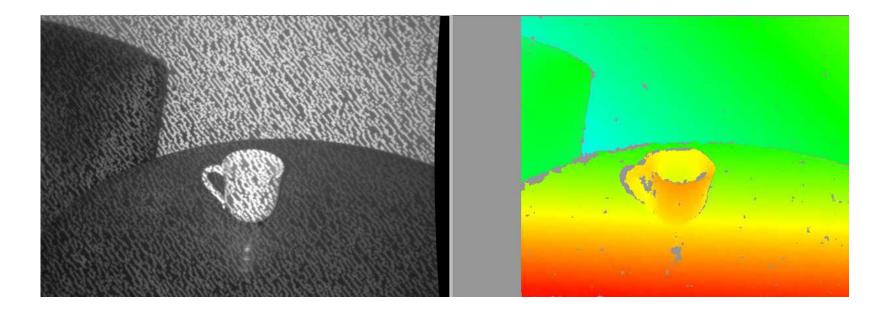
• What can we do about textureless scenes?



Images: J. Sturm

Active Depth Sensing

• Idea: Project light/texture



Images: J. Sturm

Depth Cameras

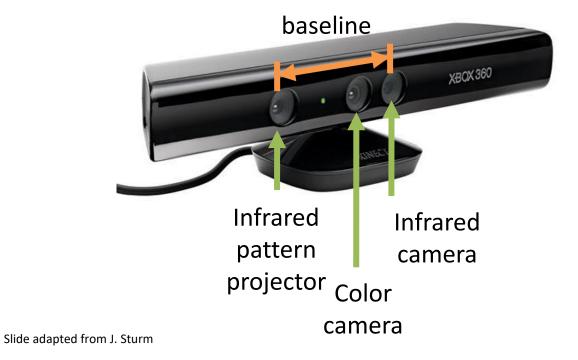


Time-of-Flight

Structured Light

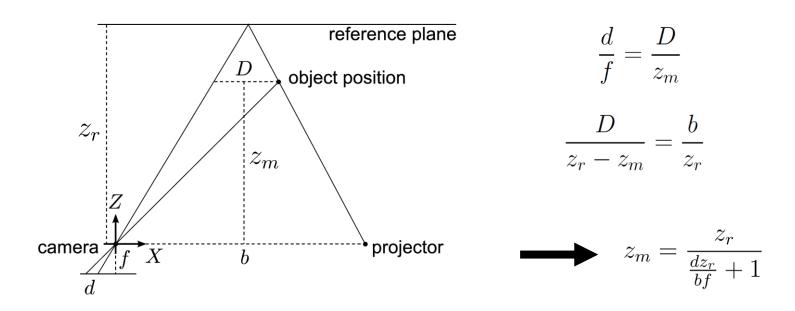
Structured Light Measurement Principle

- Project speckle pattern using infrared laser and diffraction element
- Measure infrared speckles using infrared camera
- Measure corresponding RGB image using color camera

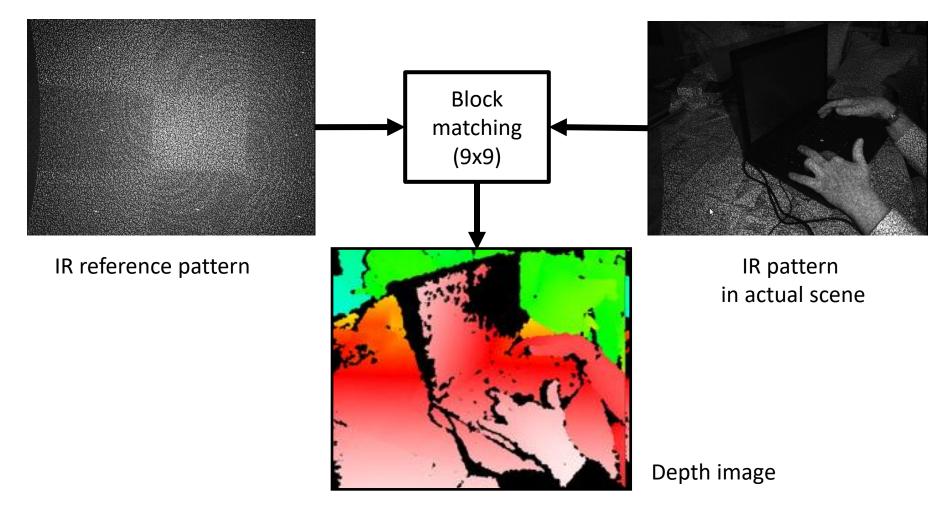


Structured Light Measurement Principle

Use known baseline and reference pattern for depth measurement



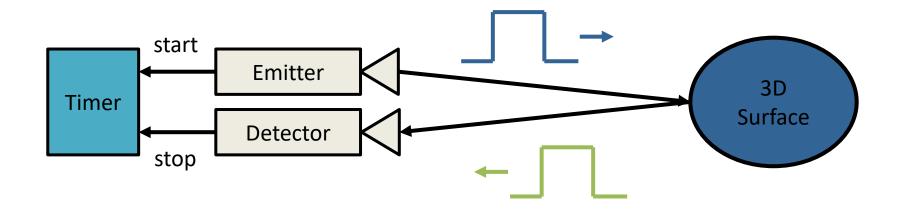
Structured Light Measurement Principle



Slide adapted from J. Sturm

Time-of-Flight Measurement Principle

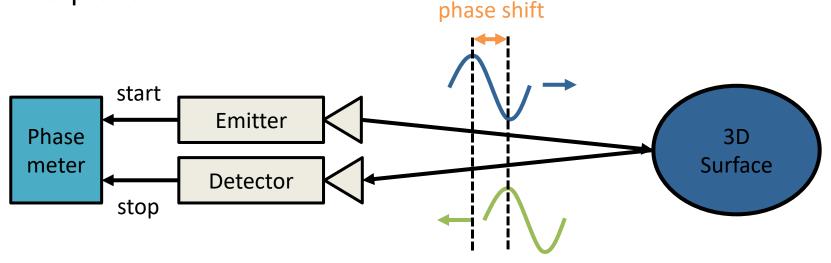
- Idea: emit timed IR pulse and measure its time of return
- Difficult to create pulses and measure time precisely



Slide adapted from N. Navab

Time-of-Flight Measurement Principle

- Idea: emit continous modulated IR wave signal and measure phase shift
- Signal periodicity creates phase ambiguities: use multiple frequencies



Slide adapted from N. Navab

Active vs. Passive Sensors

- Active Sensors
 - Surfaces do not need to be textured
 - Bring their own light, also work in low-light scenarios
 - But: Diffuse IR sunlight typically overrides emitted light
 - Difficulties for IR-absorbing or reflective materials
- Passive Sensors (e.g RGB-only)
 - Do not rely on measuring emitted light
 - Are not limited by the resolution of the projection pattern or ToF measurement principle
 - Distance
 - Multi-path noise (ToF)

Lessons Learned Today

- Stereo depth reconstruction from two and multiple views
 - Stereo rectification simplifies correspondence search for two views
 - Dense correspondence search using block matching
 - Correspondences can be ambiguous
 - Regularization with priors to help with noisy and ambiguous data terms
- Depth cameras
 - Structured light principle
 - Time-of-flight principle

Thanks for your attention!

Slides Information

- These slides have been initially created by Jörg Stückler as part of the lecture "Robotic 3D Vision" in winter term 2017/18 at Technical University of Munich.
- The slides have been revised by myself (Niclas Zeller) for the same lecture held in winter term 2020/21
- Acknowledgement of all people that contributed images or video material has been tried (please kindly inform me if such an acknowledgement is missing so it can be added).