

BAD-SLAM: Bundle Adjusted Direct RGB-D SLAM

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- 1. Motivation
- 2. First Contribution: BAD-SLAM algorithm
- 3. Interim report: Works but not good enough
- 4. Second Contribution: Better Datasets
- 5. Conclusion

Motivation - Indirect vs Direct Methods

Two previous approaches for Context: Indirect Methods (ORB-SLAM 2), Direct Methods (DVO-SLAM)





Motivation - Bundle Adjustment

- Optimization problem to jointly estimate optimal Pose(Trajectory) and optimal 3D coordinates
- e.g. Optimizing Reprojection error







Motivation - Many ways to compute RGB-D SLAM





Motivation – Authors Goal

- Goal:
 - Use fast direct Bundle Adjustment
 - Use dense RGB-D measurements
 - Perform RGB-D SLAM in real-time



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First Contribution: BAD-SLAM algorithm



Figure 2. Approach overview. KF stands for keyframe.

First Contribution: BAD-SLAM algorithm



Generic Front-end

Keyframe Selection: every 10th frame

Loop Closure Detection:

- Identifies keyframe m which is most similar with the last keyframe k
- If identified then Loop closure by Pose graph Optimization



First Contribution: BAD-SLAM algorithm



Figure 2. Approach overview. KF stands for keyframe.



Surfels - Surface Elements

Components:

 $\overrightarrow{n_s} \in \mathbb{R}^3$: Surfel normal

 $r_s \in \mathbb{R}$: Surfel radius

 $\overrightarrow{p_s} \in \mathbb{R}^3$: Center Point of Surfel

 T_G^k :Linear Transform from fixed world frame G to local keyframe k

 $d_s \in \mathbb{R}$: scalar visual descriptor

Z axis $\overrightarrow{n_s}$ p_{s} d_{s} Z axis T_G^k $\boldsymbol{T}_{G}^{k} = \begin{bmatrix} \boldsymbol{R} & \vec{H} \\ \vec{0}^{T} & 1 \end{bmatrix} \in \mathbb{SE}(3)$ G X axis



Cost function



https://upload.wikimedia.org/wikipedia/commons/c/c1/RhoFunctions.png



Photometric and Geometric Error

Photometric Error: (Color/Intensity)

$$r_{photo} = I_2\left(\pi\left(T(\overrightarrow{X_j})\right)\right) - I_1(x)$$

Geometric Error: (Depth)

$$\mathbf{r}_{geo} = Z_2\left(\pi\left(T(\overrightarrow{X_j})\right)\right) - Z_1(x)$$





Cost function - Geometric Residual





Cost function - Photometric Residual





Too many variables to optimize!





How do we optimize this Cost-function?

Solution:

- Alternating optimization
 - Most optimization variables separately updated or optimized
 - within each iteration the cost function is optimized by alternatingly fixing a set of variables



Optimization Algorithm (Bundle Adjustment)

- Divided Algorithm into 3 Parts
 - Creation of surfels (|S|)
 - Optimization of variables $(T_G^k; \overrightarrow{p_s}; \overrightarrow{n_s}; d_s; K)$
 - Cleanup and final update $(|S|; r_s)$

for all keyframes do Create missing surfels	
for $i \in [1, \text{max_iteration_count}]$ do Update surfel normals Optimize surfel positions and descriptors if i = 1 then Merge similar surfels	
Optimize keyframe poses Optimize camera intrinsics (optionally) if no keyframe moved then break	
 for all keyframes which moved in the last loop d Merge similar surfels Delete outlier surfels; Update surfel radii 	lo



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Part 1 – Surfel Creation 1





Part 1 – Surfel Creation 1









Computing initial n_s





Part 1 – Computing r_s

 $\vec{p} \in \mathbb{R}^2$







Part 1 – Surfel Creation 1

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Part 1 – Outlier Filter





Part 1 – Outlier Filter







Part 1 – Outlier Filter



Outlier if :

- $n_C < n_{min}$ or
- $n_V > n_C$
 - with $n_{min} = \min(3, 1 + \lfloor 0.2 |K \rfloor)$ $|K| \coloneqq number of Keyframes$



Optimization Algorithm (Bundle Adjustment)

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Part 2 – n_s Update

















New Parametrization:

$$\overrightarrow{p_{s,i+1}} \coloneqq \overrightarrow{p_{s,i}} + t \overrightarrow{n_s}$$

 $\min_{t, d_s} C(K, S)$

$$\begin{pmatrix} t \\ d_s \end{pmatrix}_{i+1} = \begin{pmatrix} t \\ d_s \end{pmatrix}_i - \underbrace{(J^T J)^{-1} J^T}_{M} \overline{r}^{T}$$
with $M \in \mathbb{R}^{2 \times 2}$

- Optimization of Cost-function:
 - Gauss-Newton method
 - Fix all variables but $\overrightarrow{p_s} \& d_s$
 - Each surfel is independent therefore for each surfel only need to compute 2x2-Matrix







- Due to Noisy measurements we have created unnecessary surfels
- How do we eliminate these?

- Solution:
 - Merge similar surfels at first iteration of BA scheme
 - Conditions: (given 2 Surfels: $s_1 \& s_2$)
 - Surfel normal: $\measuredangle(\overrightarrow{n_{s_1}}, \overrightarrow{n_{s_2}}) < 40^\circ$
 - Surfel position: $\|\overrightarrow{p_{s_1}} \overrightarrow{p_{s_2}}\| < 4 \cdot 0.8 \cdot \min(r_{s_1}, r_{s_2})$



























Part 2 – Camera Intrinsics K





Part 2 – Camera Intrinsics K

Assumption:

- Separate pinhole camera models for RGB and depth measurements
 - $\hat{\pi}_{D,k}(\dots) \rightarrow K_D$; $\pi_{I,k}(\dots) \rightarrow K_I$
- Additional model for depth deformation
 - $d_{true}(x, y) = d_{dist}(x, y) +$ $D_{\delta}(x, y) \exp(-\alpha_1 d_{dist}(x, y))$
 - Only optimize parameters $D_{\delta}(x, y)$ and α_1
- Optimization fast due to Hessian diagonal at parts corresponding to $D_{\delta}(x, y)$





Optimization Algorithm (Bundle Adjustment)

- Divided Algorithm into 3 Parts
 - Creation of surfels (|S|)
 - Optimization of variables $(T_G^k; \overrightarrow{p_s}; \overrightarrow{n_s}; d_s; K)$
 - Cleanup and final update $(|S|; r_s)$

: for all keyframes do Create missing surfels	
2: for $i \in [1, \max_iteration_count]$ do 3: Update surfel normals 4: Optimize surfel positions and descriptors 5: if $i = 1$ then Merge similar surfels 5: Optimize keyframe poses 7: Optimize camera intrinsics (optionally)	
if no keyframe moved then break	
 for all keyframes which moved in the last loop (Merge similar surfels Delete outlier surfels; Update surfel radii 	10



Part 3 – Delete Outlier Surfels









Part 3 – Delete Outlier Surfels



Outlier if :

 $n_C < n_{min} \text{ or } n_V > n_C$ with $n_{min} = \min(3, 1 + \lfloor 0.2 |K| \rfloor)$ $|K| \coloneqq number \text{ of Keyframes}$



Part 3 – Radius Update







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Part 3 – Radius Update

 $r_{s,new} = \min_i r_{s,i}$







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Interim report: Works but not good enough

Benchmark with TUM RGB-D dataset:

- Direct Methods (DVO-SLAM, BAD-SLAM) surpassed by indirect methods (ORB-SLAM 2)
- Assumption: Worse performance due to:
 - Rolling shutter
 - Asynchronous Frames (RGB images and Depth map)
 - Badly calibrated camera intrinsics
 - => To what extend is BAD-SLAM affected by distortions?

	fr1/desk	fr2/xyz	fr3/office	avg. rank
BundleFusion [7]	1.6 (1)	1.1 (3)	2.2 (4)	2.7 (2)
DVO SLAM [30]	2.1 (5)	1.8 (6)	3.5 (8)	6.3 (6)
ElasticFusion [69]	2.0 (4)	1.1 (3)	1.7 (2)	3.0 (4)
Kintinuous [68]	3.7 (8)	2.9 (9)	3.0 (6)	7.7 (8)
MRSMap [60]	4.3 (9)	2.0(7)	4.2 (9)	8.3 (9)
ORB-SLAM2 [44]	1.6 (1)	0.4 (1)	1.0 (1)	1.0 (1)
PSM SLAM [70]	1.6	-	3.1	-
RGB-D SLAM [9]	2.3 (6)	0.8(2)	3.2 (7)	5.0 (5)
VoxelHashing [47]	2.3 (6)	2.2 (8)	2.3 (5)	6.3 (6)
Ours (fixed intr.)	3.6	1.2	2.5	-
Ours	1.7 (3)	1.1 (3)	1.7(2)	2.7(2)

Table 2. ATE RMSE results in cm on TUM RGB-D datasets (rank in brackets). Ours achieves the second best average rank after ORB-SLAM2 and alongside BundleFusion. Results for other methods are as reported in [7], [70] and [44]. Our results without intrinsics and depth deformation optimization are clearly worse, showing that this is necessary for these datasets.

Interim report: How badly is BAD-SLAM affected?

Benchmark with synthetic Dataset:

- 4 Datasets out of TUM RGB-D dataset
 - Clean
 - Asynchronous
 - Rolling Shutter
 - Asynchronous + Rolling Shutter
- Observation:
 - effects degrade SLAM results
 - Not all effects have been modelled
- => Do we solve this issue by modelling every effect in Software?

	clean	async	rs	async & rs
	avg. med.	avg. med.	avg. med.	avg. med.
BundleFusion [7]	0.34 0.22	1.10 1.14	1.10 1.02	1.48 1.40
DVO SLAM [30]	0.32 0.23	2.33 0.72	5.10 1.37	4.94 1.39
ElasticFusion [69]	1.11 0.90	1.98 1.17	2.70 1.77	3.19 2.52
ORB-SLAM2 [44]	0.47 0.30	0.60 0.40	3.25 1.57	3.49 1.55
Ours	0.15 0.02	0.40 0.21	0.99 0.87	1.01 0.98

Table 3. ATE RMSE [cm] averages and medians for seven synthetic datasets per category. Asynchronous RGB-D frames (async) and rolling shutter (rs) both worsen the results.



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Second Contribution: Better Datasets

No, due to: High implementation effort High computational demand => high runtimes Possibility of degenerate cases Solution: Solve issue with better hardware.



Second Contribution: Better Datasets

- Synchronized, Global shutter RGB and depth sensors
- Infrared Emitter
- Vicon Markers and Vicon System for trajectory tracking (ground truth)
- Well calibrated System
 - Optional camera intrinsics optimization not necessary





Second Contribution: New Benchmark

- 61 training sets (with ground truth)
- 35 test sets (non-public ground truth)
 - Online Leaderboard
- Ground truth:
 - Majority with Vicon System
 - Minority with Structure-from-Motion
 - E.g. outdoor scenes (Bench)



Figure 1. Scene from our benchmark reconstructed in real-time with ca. 335'000 surfels, with keyframes and estimated trajectory.



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Conclusion: Final Results



Figure 6. Evaluation on our benchmark's training and test datasets. For a given threshold on the ATE RMSE (x-axis), the graphs show the number of datasets for which the method has a smaller error.



Figure 7. Complete SE(3) ATE RMSE evaluation results on the training (top) and test (bottom) datasets of our benchmark in cm. Each column visualizes the results for one dataset. We show three runs per dataset for non-deterministic methods.



Conclusion: What does BAD-SLAM show us?

- 1. A new fast direct bundle adjustment formulation
- 2. Direct methods are negatively affected by rolling shutter, asynchronous RGB and Depth measurements, calibration errors
- 3. Direct methods may perform significantly better on well calibrated Dataset than popularly chosen indirect methods (ORB-SLAM2)
- 4. Existing datasets only give partial picture of SLAM algorithm performance



References

[1] Thomas Schops, Torsten Sattler, Marc Pollefeys; BAD SLAM: Bundle Adjusted Direct RGB-D SLAM, In CVPR 2019

[2] Thomas Schops, Torsten Sattler, Marc Pollefeys; Supplementary Document for:

BAD SLAM: Bundle Adjusted Direct RGB-D SLAM, In CVPR 2019



Thank you for your attention! ③



Cost function – Depth error

$$\sigma_D = \delta \frac{d_m^2}{b f} \left| \left(T_g^k \, \overrightarrow{n_s} \right)^T \pi_k \left(T_g^k \, \overrightarrow{p_s} \right) \right|$$